

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Scenarios of Early Universe Cosmology

Philosophical and Physical Challenges

Robert Brandenberger
McGill University

September 23, 2011

Outline

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- 1 Introduction
 - Motivation
 - Review of Inflationary Cosmology
 - Problems of Inflationary Cosmology
 - Message and Preview
- 2 Overview of Alternatives
- 3 Realizing an Emergent Universe Scenario
- 4 Models for a Nonsingular Bounce
- 5 Cosmological Perturbations
 - General Theory
 - Application to Inflationary Cosmology
 - String Gas Cosmology and Structure Formation
 - Application to Matter Bounce Cosmology
- 6 Conclusions

Plan

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- 1 Introduction
 - Motivation
 - Review of Inflationary Cosmology
 - Problems of Inflationary Cosmology
 - Message and Preview
- 2 Overview of Alternatives
- 3 Realizing an Emergent Universe Scenario
- 4 Models for a Nonsingular Bounce
- 5 Cosmological Perturbations
 - General Theory
 - Application to Inflationary Cosmology
 - String Gas Cosmology and Structure Formation
 - Application to Matter Bounce Cosmology
- 6 Conclusions

Current Paradigm for Early Universe Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

The **Inflationary Universe Scenario** is the current paradigm of early universe cosmology.

It solves some conceptual problems of the previous paradigm, Standard Big Bang Cosmology:

- Solves **horizon problem**
- Solves **flatness problem**
- Solves **size/entropy problem**

Makes contact with **observations**: Provides a **causal mechanism** of generating **primordial cosmological perturbations** (Chibisov & Mukhanov, 1981).

Current Paradigm for Early Universe Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Current Paradigm for Early Universe Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Current Paradigm for Early Universe Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

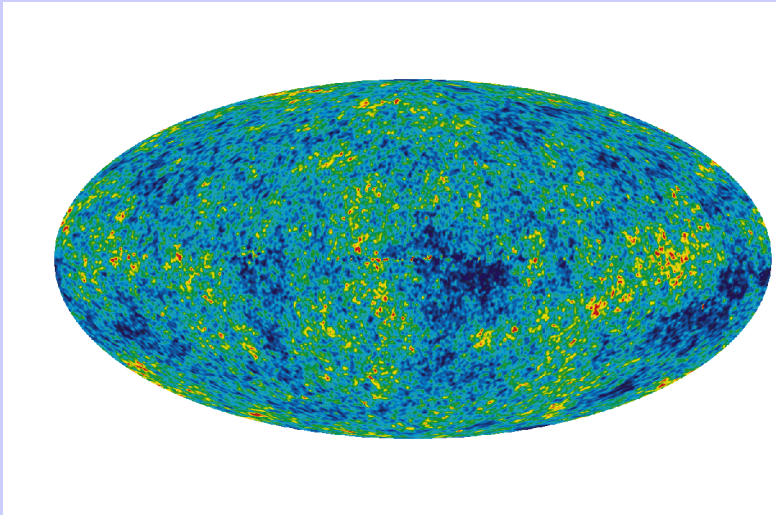
General

Inflation

String Gas

Bounce

Conclusions



Credit: NASA/WMAP Science Team

Alternatives

R. Brandenberger

Introduction

- Motivation
- Inflation
- Problems
- Message

Alternatives

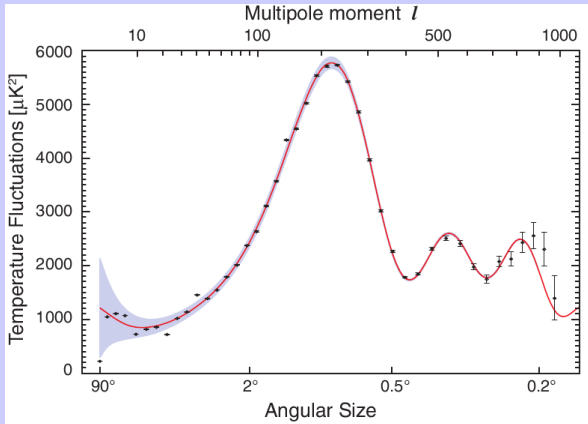
Emergent

Bounce

Perturbations

- General
- Inflation
- String Gas
- Bounce

Conclusions



Credit: NASA/WMAP Science Team

Challenges for the Current Paradigm

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- In spite of the phenomenological successes, the inflationary scenario suffers from several **conceptual problems**.
- These problems lead to **philosophical** and **physical challenges**.
- In light of these challenges it is important to search for alternative early universe scenarios which can address some of the problems of inflationary cosmology.
- Alternative A: **Emergent Universe Scenario** [as realized e.g. in **String Gas Cosmology**]
- Alternative B: **Matter Bounce**.
- These new paradigms can be **tested** in cosmological observations.

Challenges for the Current Paradigm

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Challenges for the Current Paradigm

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Challenges for the Current Paradigm

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

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Challenges for the Current Paradigm

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Challenges for the Current Paradigm

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Historical Digression

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

The successful match of inflationary cosmology with the angular power spectrum of CMB anisotropies is **NOT** a success unique to inflationary cosmology.

Sunyaev and Zel'dovich, and Peebles and Yu realized more than ten years before inflationary cosmology that **any** cosmological model which generates a scale-invariant spectrum of cosmological perturbations on super-Hubble scales will yield the acoustic oscillations in the spectrum of the CMB.

Historical Digression

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

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Historical Footnote

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

1970a485,...1,...28

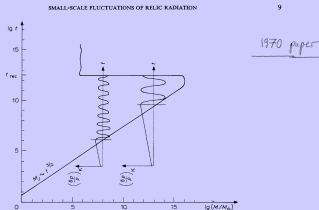


Fig. 1a. Diagram of gravitational instability in the "big-bang" model. The region of instability is located to the right of the line $M_J(t)$; the region of stability to the left. The two additional lines of the graph demonstrate the temporal evolution of density perturbations of matter: growth until the moment when the considered mass is smaller than the Jeans mass and oscillations thereafter. It is apparent that at the moment of recombination perturbations corresponding to different masses correspond to different phases.

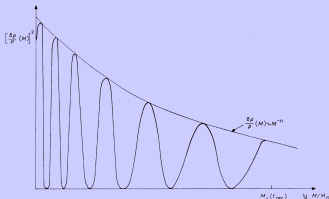


Fig. 1b. The dependence of the square of the amplitude of density perturbations of matter on scale. The fine line designates the usually assumed dependence $(\delta\rho/\rho) \sim M^{-2}$. It is apparent that fluctuations of relic radiation should depend on scale in a similar manner.

R. Sunyaev & Ya. Zeldovich, *Astrophysic and Space Science* 7

3-19 (1970)

Review of Inflationary Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Context:

- General Relativity
- Scalar Field Matter

$$\text{Metric : } ds^2 = dt^2 - a(t)^2 dx^2$$

Inflation:

- phase with $a(t) \sim e^{tH}$
- requires matter with $p \sim -\rho$
- requires a slowly rolling scalar field φ
- - in order to have a potential energy term
- - in order that the potential energy term dominates sufficiently long

Review of Inflationary Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Review of Inflationary Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Review of Inflationary Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Review of Inflationary Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Review of Inflationary Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Context:

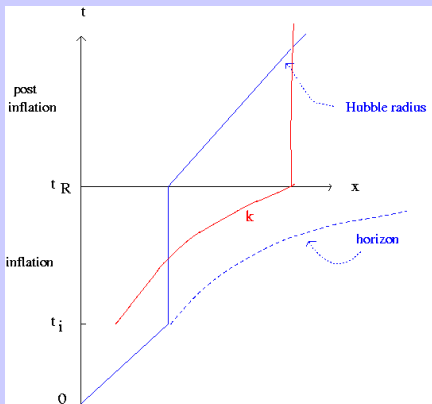
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Space-time sketch of inflationary cosmology



Note:

- $H = \frac{\dot{a}}{a}$
- curve labelled by k : wavelength of a fluctuation

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Hubble Radius vs. Horizon

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- **Hubble radius** $l_H(t) \equiv H^{-1}(t)$: local concept. Matter and gravitational fields **oscillate** on **sub-Hubble** scales, but are **frozen out** on super-Hubble scales. A microscopic structure formation mechanism can only work on sub-Hubble scales.
- **Horizon**: non-local concept. Zone of **causal** influence. Forward light cone starting at the initial time.

Hubble Radius vs. Horizon

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Hubble Radius vs. Horizon

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Hubble Radius vs. Horizon

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Hubble Radius vs. Horizon

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Hubble Radius vs. Horizon

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Successes of Inflation

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- inflation renders the universe large, homogeneous and spatially flat
- classical matter redshifts \rightarrow matter vacuum remains
- **quantum vacuum fluctuations: seeds for the observed structure** [Chibisov & Mukhanov, 1981]
- sub-Hubble \rightarrow locally causal

Conceptual Problems of Inflationary Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- Nature of the scalar field φ (the “inflaton”)
- Conditions to obtain inflation (initial conditions, slow-roll conditions, graceful exit and reheating)
- Amplitude problem
- Singularity problem
- Trans-Planckian problem
- Applicability of General Relativity
- Cosmological constant problem

Singularity Problem

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

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- Standard cosmology: Penrose-Hawking theorems → initial singularity → incompleteness of the theory.
- Inflationary cosmology: In scalar field-driven inflationary models the initial singularity persists [Borde and Vilenkin] → incompleteness of the theory.

Penrose-Hawking theorems:

- Ass: i) Einstein action, 2) weak energy conditions
 $\rho > 0, \rho + 3p \geq 0$
- → space-time is geodesically incomplete.

Singularity Problem

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

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Singularity Problem

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

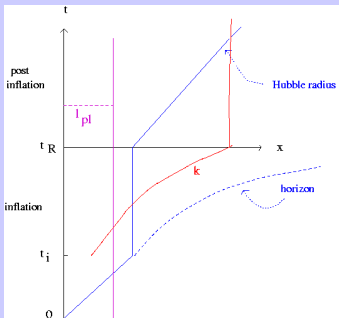
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Trans-Planckian Problem for Fluctuations



- **Success of inflation:** At early times scales are inside the Hubble radius \rightarrow causal generation mechanism is possible.
- **Problem:** If time period of inflation is more than $70H^{-1}$, then $\lambda_p(t) < l_{pl}$ at the beginning of inflation
- \rightarrow new physics **MUST** enter into the calculation of the fluctuations.

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

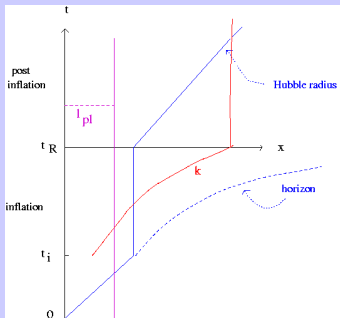
Inflation

String Gas

Bounce

Conclusions

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Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

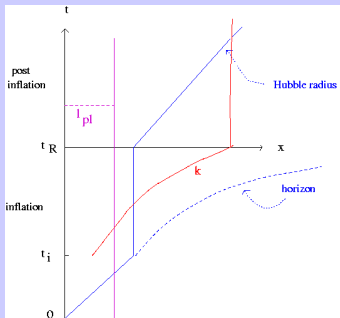
Inflation

String Gas

Bounce

Conclusions

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Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

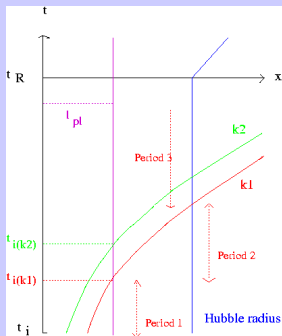
Bounce

Conclusions

Recent Reference: A. Linde, V. Mukhanov and A. Vikman,
arXiv:0912.0944

- It is not sufficient to show that the Hubble constant is smaller than the Planck scale.
- The frequencies involved in the analysis of the cosmological fluctuations are many orders of magnitude larger than the Planck mass. Thus, **“the methods used in [1] are inapplicable for the description of the .. process of generation of perturbations in this scenario.”**

Trans-Planckian Window of Opportunity



- If evolution in Period I is non-adiabatic, then scale-invariance of the power spectrum will be lost [J. Martin and RB, 2000]
- → Planck scale physics testable with cosmological observations!

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Applicability of GR

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- In all approaches to quantum gravity, the Einstein action is only the leading term in a low curvature expansion.
- Correction terms may become dominant at much lower energies than the Planck scale.
- Correction terms will dominate the dynamics at high curvatures.
- The energy scale of inflation models is typically $\eta \sim 10^{16} \text{GeV}$.
- $\rightarrow \eta$ too close to m_{pl} to trust predictions made using GR.

Cosmological Constant Problem

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

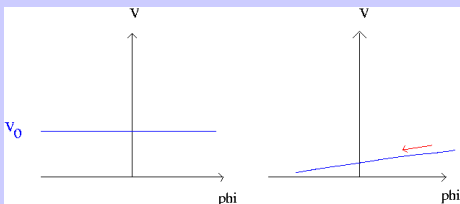
General

Inflation

String Gas

Bounce

Conclusions



- Quantum vacuum energy does not gravitate.
- Why should the almost constant $V(\varphi)$ gravitate?

$$\frac{V_0}{\Lambda_{obs}} \sim 10^{120}$$

Zones of Ignorance

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

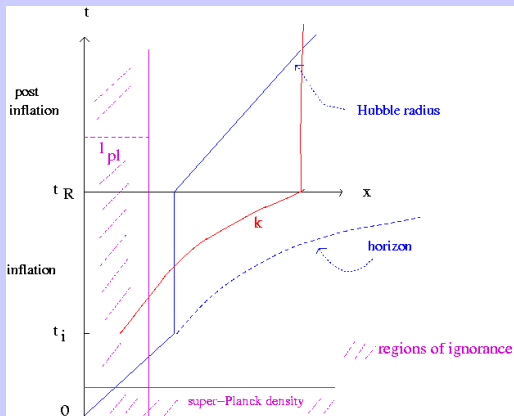
General

Inflation

String Gas

Bounce

Conclusions



Message

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- Current realizations of inflation have serious **conceptual problems**.
- These problems are both of **physical** (e.g cosmological constant problem, trans-Planckian problem for fluctuations) and **philosophical** (e.g. singularity problem - origin of time) nature.
- This motivates the search for **alternatives**.
- In these alternatives the **philosophical** issues appear in a different light.
- In these alternatives some of the **physical** problems are solved.
- The alternatives make **testable predictions** for cosmological observations.

Message

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Message

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Message

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Message

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Message

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Some other Issues

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- What about the **inflationary multiverse**?
- How does the **classicalization** occur?

Some other Issues

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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- How does the **classicalization** occur?

What about the string inflationary multiverse?

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Relies on two key assumptions

- 1. Landscape of **string vacua**.
- 2. **Stochastic inflation**: a way to populate these vacua.

However, keep in mind that:

- Non-perturbative string theory does **not** exist. Hence, we cannot talk about a **string vacuum**.
- In the context of large field inflation, the stochastic equation is **missing** terms which dominate.

Thus, the “string inflationary multiverse” is neither part of string theory nor a part of inflationary cosmology.

What about the string inflationary multiverse?

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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What about the string inflationary multiverse?

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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What about the string inflationary multiverse?

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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How do inhomogeneities become classical?

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Key conditions:

- **Squeezing** \rightarrow r.m.s. quantum expectation values obey classical equations, [A. Guth and S-Y. Pi, Phys.Rev. D32 (1985) 1899-1920]
- **Decoherence** of cosmological perturbations induced by the nonlinearities in the Einstein equations. Occurs as soon as fluctuations exit the Hubble radius. [P. Martineau, Class.Quant.Grav. 24 (2007) 5817-5834 ; C. Kiefer, I. Lohmar, D. Polarsky and A. Starobinsky, Class.Quant.Grav. 24 (2007) 1699-1718]

How do inhomogeneities become classical?

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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How do inhomogeneities become classical?

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Plan

Alternatives

R. Branden-
berger

Introduction

Motivation
Inflation
Problems
Message

Alternatives

Emergent

Bounce

Perturbations

General
Inflation
String Gas
Bounce

Conclusions

- 1 Introduction
 - Motivation
 - Review of Inflationary Cosmology
 - Problems of Inflationary Cosmology
 - Message and Preview
- 2 Overview of Alternatives
- 3 Realizing an Emergent Universe Scenario
- 4 Models for a Nonsingular Bounce
- 5 Cosmological Perturbations
 - General Theory
 - Application to Inflationary Cosmology
 - String Gas Cosmology and Structure Formation
 - Application to Matter Bounce Cosmology
- 6 Conclusions

Alternative Scenarios

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- **Nonsingular cosmologies with a matter-dominated phase of contraction**
- **Emergent universe scenario [e.g. string gas cosmology]**
- **Pre-Big-Bang scenario [Gasperini and Veneziano]**
- **Ekpyrotic universe scenario [Khoury, Ovrut, Steinhardt and Turok]**
- **Conformal cosmology [Rubakov et al.]**
- **Varying speed of light (VSL) scenario [Moffatt, Albrecht and Magueijo]**
-

Matter Bounce Scenario

F. Finelli and R.B., *Phys. Rev. D*65, 103522 (2002), D. Wands, *Phys. Rev. D*60 (1999)

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

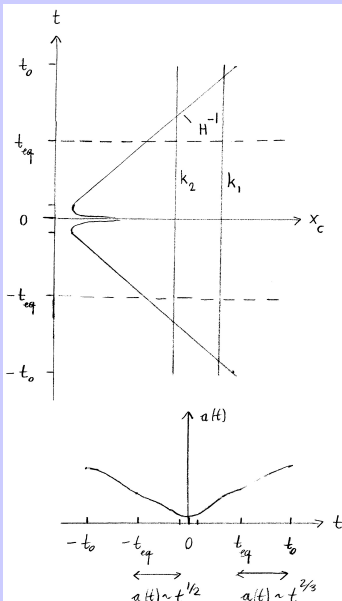
General

Inflation

String Gas

Bounce

Conclusions



Features of Matter Bounce Scenario

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- **No cosmological singularity!**
- No horizon problem [horizon \neq Hubble radius]
- Flatness problem mitigated
- No structure formation problem
- **No trans-Planckian problem** for fluctuations
- **Unstable against anisotropies!**

Features of Matter Bounce Scenario

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Features of Matter Bounce Scenario

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Features of Matter Bounce Scenario

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Features of Matter Bounce Scenario

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Features of Matter Bounce Scenario

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Emergent Universe Scenario

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

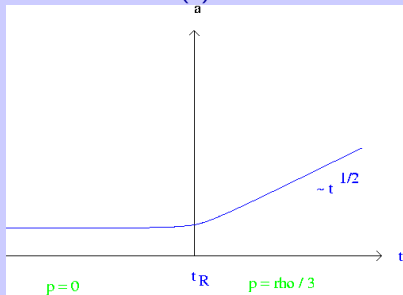
Inflation

String Gas

Bounce

Conclusions

We consider the following background dynamics for the scale factor $a(t)$:



Space-time sketch

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

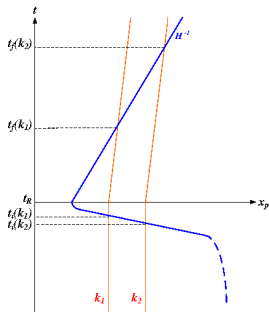
General

Inflation

String Gas

Bounce

Conclusions



Features of the Emergent Universe Scenario

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Features of the Emergent Universe Scenario

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- No cosmological singularity!
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 - Flatness problem mitigated
 - No structure formation problem
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Features of the Emergent Universe Scenario

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- No cosmological singularity!
- No horizon problem [horizon \neq Hubble radius]
- Flatness problem mitigated
 - No structure formation problem
 - No trans-Planckian problem for fluctuations
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Features of the Emergent Universe Scenario

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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- Flatness problem mitigated
- No structure formation problem
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Features of the Emergent Universe Scenario

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Features of the Emergent Universe Scenario

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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- No structure formation problem
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Plan

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- 1 Introduction
 - Motivation
 - Review of Inflationary Cosmology
 - Problems of Inflationary Cosmology
 - Message and Preview
- 2 Overview of Alternatives
- 3 Realizing an Emergent Universe Scenario**
- 4 Models for a Nonsingular Bounce
- 5 Cosmological Perturbations
 - General Theory
 - Application to Inflationary Cosmology
 - String Gas Cosmology and Structure Formation
 - Application to Matter Bounce Cosmology
- 6 Conclusions

Example: String Gas Cosmology

R.B. and C. Vafa, *Nucl. Phys. B*316:391 (1989)

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Idea: make use of the **new symmetries** and **new degrees of freedom** which string theory provides to construct a new theory of the very early universe.

Assumption: Matter is a gas of fundamental strings

Assumption: Space is compact, e.g. a torus.

Key points:

- **New degrees of freedom:** string oscillatory modes
- Leads to a **maximal temperature** for a gas of strings, the Hagedorn temperature
- **New degrees of freedom:** string winding modes
- Leads to a **new symmetry:** physics at large R is equivalent to physics at small R

Example: String Gas Cosmology

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Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

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Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

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T-Duality

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

T-Duality

- Momentum modes: $E_n = n/R$
- Winding modes: $E_m = mR$
- Duality: $R \rightarrow 1/R$ $(n, m) \rightarrow (m, n)$
- Mass spectrum of string states unchanged
- Symmetry of vertex operators
- Symmetry at non-perturbative level \rightarrow existence of D-branes

Adiabatic Considerations

R.B. and C. Vafa, *Nucl. Phys. B*316:391 (1989)

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

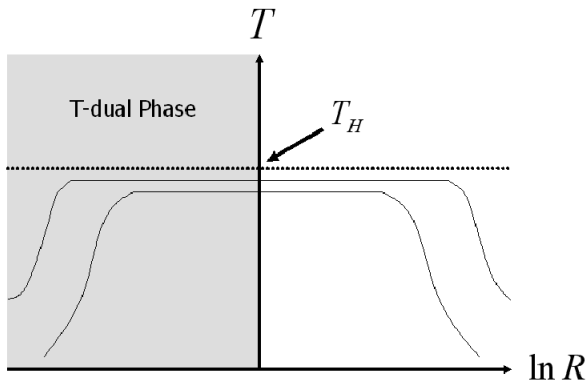
Inflation

String Gas

Bounce

Conclusions

Temperature-size relation in string gas cosmology



Singularity Problem in Standard and Inflationary Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

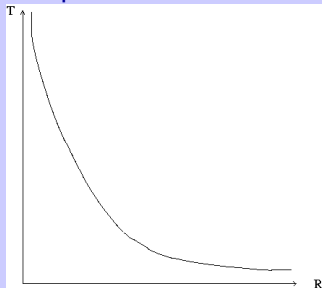
Inflation

String Gas

Bounce

Conclusions

Temperature-size relation in standard cosmology



Dynamics

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

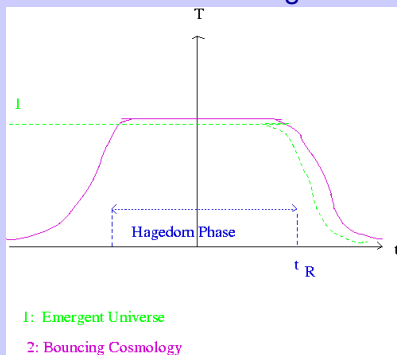
Inflation

String Gas

Bounce

Conclusions

Assume some action gives us $R(t)$



Dynamics II

Alternatives

R. Branden-
berger

Introduction

Motivation
Inflation
Problems
Message

Alternatives

Emergent

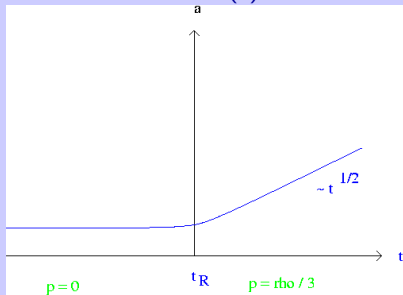
Bounce

Perturbations

General
Inflation
String Gas
Bounce

Conclusions

We will thus consider the following background dynamics for the scale factor $a(t)$:



Dimensionality of Space in SGC

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

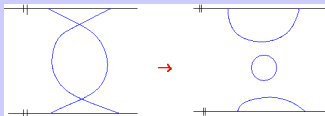
Inflation

String Gas

Bounce

Conclusions

- Begin with all 9 spatial dimensions small, initial temperature close to T_H \rightarrow winding modes about all spatial sections are excited.
- Expansion of any one spatial dimension requires the annihilation of the winding modes in that dimension.



- Decay only possible in three large spatial dimensions.
- \rightarrow **dynamical explanation of why there are exactly three large spatial dimensions.**

Note: this argument assumes constant dilaton [R. Danos, A. Frey and A. Mazumdar]

Moduli Stabilization in SGC

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Size Moduli [S. Watson, 2004; S. Patil and R.B., 2004, 2005]

- winding modes prevent expansion
- momentum modes prevent contraction
- $\rightarrow V_{\text{eff}}(R)$ has a minimum at a finite value of R , $\rightarrow R_{\text{min}}$
- in heterotic string theory there are **enhanced symmetry states** containing both momentum and winding which are massless at R_{min}
- $\rightarrow V_{\text{eff}}(R_{\text{min}}) = 0$
- \rightarrow **size moduli stabilized** in Einstein gravity background

Shape Moduli [E. Cheung, S. Watson and R.B., 2005]

- enhanced symmetry states
- \rightarrow harmonic oscillator potential for θ
- \rightarrow **shape moduli stabilized**

Dilaton stabilization in SGC

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- The only remaining modulus is the dilaton
- Make use of **gaugino condensation** to give the dilaton a potential with a unique minimum
- → dilaton is stabilized
- Dilaton stabilization is consistent with size stabilization [R. Danos, A. Frey and R.B., 2008]

Plan

Alternatives

R. Brandenberger

Introduction

Motivation
Inflation
Problems
Message

Alternatives

Emergent

Bounce

Perturbations

General
Inflation
String Gas
Bounce

Conclusions

- 1 Introduction
 - Motivation
 - Review of Inflationary Cosmology
 - Problems of Inflationary Cosmology
 - Message and Preview
- 2 Overview of Alternatives
- 3 Realizing an Emergent Universe Scenario
- 4 Models for a Nonsingular Bounce**
- 5 Cosmological Perturbations
 - General Theory
 - Application to Inflationary Cosmology
 - String Gas Cosmology and Structure Formation
 - Application to Matter Bounce Cosmology
- 6 Conclusions

Overview

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

In order to obtain a bouncing cosmology it is necessary to:

- either **modify the gravitational action**
- or **introduce a new form of matter which violates the NEC (null energy condition).**
- or invoke **quantum effects** as in Loop Quantum Cosmology.

It is well motivated to consider models which go beyond the standard coupling of General Relativity to matter obeying the NEC - any approach to quantizing gravity yields terms in the effective action for the metric and matter fields which contain higher derivatives.

Ref: M. Novello and S. Perez Bergliaffa, Phys. Rep. **463**, 127 (2008).

Overview

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Some Constructions

Alternatives

R. Brandenberger

Introduction

Motivation
Inflation
Problems
Message

Alternatives

Emergent

Bounce

Perturbations

General
Inflation
String Gas
Bounce

Conclusions

- **String Gas Bounce** [R.B., S. Patil et al, in preparation]
- Quintom Bounce [Y. Cai, T. Qiu, Y. Piao, R.B. and X. Zhang, 2008]
- **Ghost Condensate Bounce** [C. Lin, R.B. and L. Perreault Levasseur, 2010]
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- Non-Local Gravitational Action [T. Biswas, A. Mazumdar and W. Siegel, 2006]
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Some Constructions

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Some Constructions

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Some Constructions

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- **String Gas Bounce** [R.B., S. Patil et al, in preparation]
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Bounce from String Gases

R.B. and C. Vafa, *Nucl. Phys. B316:391 (1989)*

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

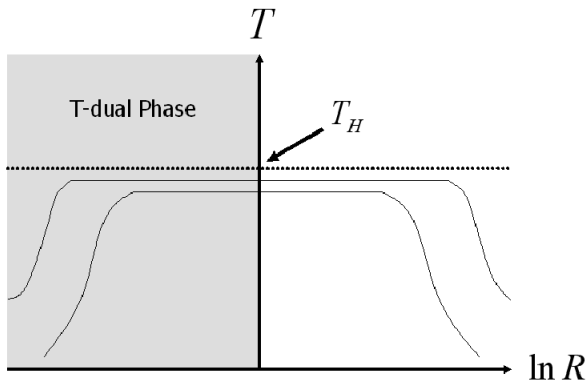
Inflation

String Gas

Bounce

Conclusions

Temperature-size relation in string gas cosmology



Bouncing Trajectory

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

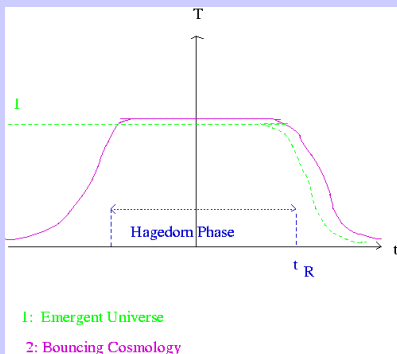
General

Inflation

String Gas

Bounce

Conclusions



Concrete Realization In the context of low energy effective action for Type IIB superstring theory coupled to string gas [R.B., C. Kounnas, H. Partouche and S. Patil, in prep.].

Example changing the gravitational action

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Hořava-Lifshitz bounce (R.B., 2009)

- Replace Einstein gravity by **Hořava-Lifshitz gravity**.
- Extra spatial derivative terms in the gravitational action act like matter which violates the NEC.

Example changing matter

Alternatives

R. Branden-
berger

Introduction

Motivation
Inflation
Problems
Message

Alternatives

Emergent

Bounce

Perturbations

General
Inflation
String Gas
Bounce

Conclusions

Ghost condensate bounce (C. Lin, R.B. and L. Perreault Levasseur, 2010)

- Introduce new matter field which has negative (ghost) sign of the kinetic action.
- Kinetic operator condenses.
- Condensate has negative gravitational energy.
- Theory ghost-free about the condensate.

Plan

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- 1 Introduction
 - Motivation
 - Review of Inflationary Cosmology
 - Problems of Inflationary Cosmology
 - Message and Preview
- 2 Overview of Alternatives
- 3 Realizing an Emergent Universe Scenario
- 4 Models for a Nonsingular Bounce
- 5 **Cosmological Perturbations**
 - General Theory
 - Application to Inflationary Cosmology
 - String Gas Cosmology and Structure Formation
 - Application to Matter Bounce Cosmology
- 6 Conclusions

Theory of Cosmological Perturbations: Basics

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Cosmological fluctuations connect early universe theories with observations

- Fluctuations of **matter** → large-scale structure
- Fluctuations of **metric** → CMB anisotropies
- N.B.: Matter and metric fluctuations are coupled

Key facts:

- 1. Fluctuations are small today on large scales
- → fluctuations were very small in the early universe
- → can use **linear perturbation theory**
- 2. Sub-Hubble scales: matter fluctuations dominate
- Super-Hubble scales: metric fluctuations dominate

Theory of Cosmological Perturbations: Basics

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Theory of Cosmological Perturbations: Basics

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Cosmological fluctuations connect early universe theories with observations

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- Super-Hubble scales: metric fluctuations dominate

Quantum Theory of Linearized Fluctuations

V. Mukhanov, H. Feldman and R.B., *Phys. Rep.* 215:203 (1992)

Step 1: Metric including fluctuations

$$ds^2 = a^2[(1 + 2\Phi)d\eta^2 - (1 - 2\Phi)d\mathbf{x}^2]$$

$$\varphi = \varphi_0 + \delta\varphi$$

Note: Φ and $\delta\varphi$ related by Einstein constraint equations

Step 2: Expand the action for matter and gravity to second order about the cosmological background:

$$S^{(2)} = \frac{1}{2} \int d^4x ((v')^2 - v_{,i}v^{,i} + \frac{z''}{z}v^2)$$

$$v = a(\delta\varphi + \frac{z}{a}\Phi)$$

$$z = a\frac{\varphi_0'}{\mathcal{H}}$$

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

where

$$v \sim a\zeta$$

where ζ is the curvature fluctuation in co-moving coordinates.

Step 3: Resulting equation of motion (Fourier space)

$$v_k'' + \left(k^2 - \frac{z''}{z}\right)v_k = 0$$

Features:

- **oscillations** on sub-Hubble scales
- **squeezing** on super-Hubble scales $v_k \sim z$

Quantum vacuum initial conditions:

$$v_k(\eta_i) = (\sqrt{2k})^{-1}$$

Application to Inflationary Cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

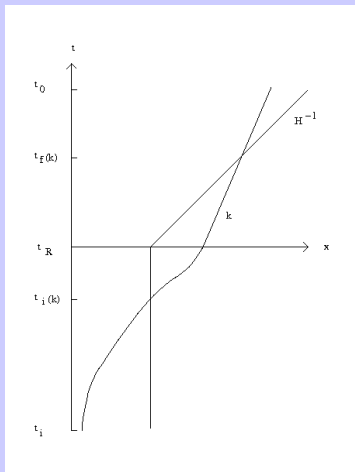
General

Inflation

String Gas

Bounce

Conclusions



N.B. Perturbations originate as quantum vacuum fluctuations.

Origin of Scale-Invariance

Heuristic analysis [W. Press, 1980]: time-translation symmetry of de Sitter phase \rightarrow scale-invariance of spectrum.

Mathematical analysis [Mukhanov and Chibisov, 1982]:

$$\begin{aligned}\mathcal{P}_\zeta(k, t) &\propto \mathcal{P}_\nu(k, t) \\ &\sim k^3 \left(\frac{a(t)}{a(t_H(k))} \right)^2 |v_k(t_H(k))|^2 \\ &\sim k^3 \eta_H(k)^2 |v_k(t_H(k))|^2 \\ &\sim k^0\end{aligned}$$

using $a(\eta) \sim \eta^{-1}$ in the de Sitter phase and $\eta_H(k) \sim k^{-1}$.

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Background for string gas cosmology

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

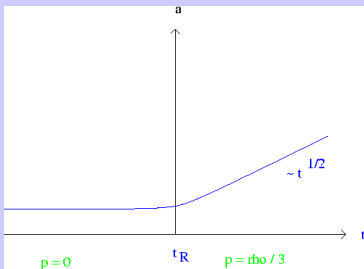
General

Inflation

String Gas

Bounce

Conclusions



Structure formation in string gas cosmology

A. Nayeri, R.B. and C. Vafa, *Phys. Rev. Lett.* 97:021302 (2006)

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

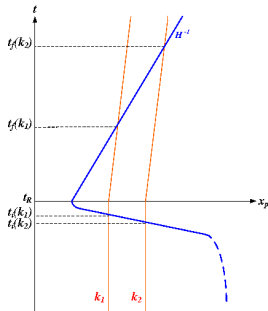
General

Inflation

String Gas

Bounce

Conclusions



N.B. Perturbations originate as thermal string gas fluctuations.

Method

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- Calculate matter correlation functions in the Hagedorn phase (neglecting the metric fluctuations)
- For fixed k , convert the matter fluctuations to metric fluctuations at Hubble radius crossing $t = t_i(k)$
- Evolve the metric fluctuations for $t > t_i(k)$ using the usual theory of cosmological perturbations

Extracting the Metric Fluctuations

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Ansatz for the metric including cosmological perturbations and gravitational waves:

$$ds^2 = a^2(\eta) \left((1 + 2\Phi) d\eta^2 - [(1 - 2\Phi)\delta_{ij} + h_{ij}] dx^i dx^j \right).$$

Inserting into the perturbed Einstein equations yields

$$\langle |\Phi(k)|^2 \rangle = 16\pi^2 G^2 k^{-4} \langle \delta T^0_0(k) \delta T^0_0(k) \rangle,$$

$$\langle |h(k)|^2 \rangle = 16\pi^2 G^2 k^{-4} \langle \delta T^i_j(k) \delta T^i_j(k) \rangle.$$

Power Spectrum of Cosmological Perturbations

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

Key ingredient: For **thermal fluctuations**:

$$\langle \delta\rho^2 \rangle = \frac{T^2}{R^6} C_V.$$

Key ingredient: For **string thermodynamics** in a compact space

$$C_V \approx 2 \frac{R^2 / \ell_s^3}{T(1 - T/T_H)}.$$

Power Spectrum of Cosmological Perturbations

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Power spectrum of cosmological fluctuations

$$\begin{aligned} P_{\Phi}(k) &= 8G^2 k^{-1} \langle |\delta\rho(k)|^2 \rangle \\ &= 8G^2 k^2 \langle (\delta M)^2 \rangle_R \\ &= 8G^2 k^{-4} \langle (\delta\rho)^2 \rangle_R \\ &= 8G^2 \frac{T}{\ell_s^3} \frac{1}{1 - T/T_H} \end{aligned}$$

Key features:

- **scale-invariant** like for inflation
- **slight red tilt** like for inflation

Power spectrum of cosmological fluctuations

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 P_{\Phi}(k) &= 8G^2 k^{-1} \langle |\delta\rho(k)|^2 \rangle \\
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Spectrum of Gravitational Waves

R.B., A. Nayeri, S. Patil and C. Vafa, *Phys. Rev. Lett.* (2007)

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

$$\begin{aligned}P_h(k) &= 16\pi^2 G^2 k^{-1} \langle |T_{ij}(k)|^2 \rangle \\ &= 16\pi^2 G^2 k^{-4} \langle |T_{ij}(R)|^2 \rangle \\ &\sim 16\pi^2 G^2 \frac{T}{\ell_s^3} (1 - T/T_H)\end{aligned}$$

Key ingredient for **string thermodynamics**

$$\langle |T_{ij}(R)|^2 \rangle \sim \frac{T}{\ell_s^3 R^4} (1 - T/T_H)$$

Key features:

- scale-invariant (like for inflation)
- **slight blue tilt** (unlike for inflation)

Requirements

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- Static Hagedorn phase (including static dilaton) → new physics required.
- $C_V(R) \sim R^2$ obtained from a thermal gas of strings provided there are winding modes which dominate.
- Cosmological fluctuations in the IR are described by Einstein gravity.

Note: Specific higher derivative toy model: T. Biswas, R.B., A. Mazumdar and W. Siegel, 2006

Is B-mode Polarization the Holy Grail of Inflation?

R.B., arXiv:1104.3581 [astro-ph.CO].

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- Cosmic strings produce direct B-mode polarization [R. Danos, R.B. and G. Holder, 2010].
- → gravitational waves not the only source of primordial B-mode polarization.
- Cosmic string loop oscillations produce a scale-invariant spectrum of primordial gravitational waves with a contribution to $\delta T/T$ which is comparable to that induced by scalar fluctuations (see e.g. A. Albrecht, R.B. and N. Turok, 1986).
- → a detection of gravitational waves through B-mode polarization is more likely to be a sign of something different than inflation.

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Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Is B-mode Polarization the Holy Grail of Inflation? II

R.B., A. Nayeri, S. Patil and C. Vafa, hep-th/0604126.

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- N.B. **String Gas Cosmology** produces a spectrum of gravitational waves with an amplitude larger than in many single field inflation models and with a small **blue tilt**.
- Inflationary cosmology must produce a red tilt.
- Observing a blue tilt of the gravitational wave spectrum would falsify inflationary cosmology.
- B-mode polarization may be the holy grail of early universe cosmology, but not of inflation.

Is B-mode Polarization the Holy Grail of Inflation? II

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Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- N.B. **String Gas Cosmology** produces a spectrum of gravitational waves with an amplitude larger than in many single field inflation models and with a small **blue tilt**.
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Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Application to the Matter Bounce Scenario

F. Finelli and R.B., *Phys. Rev. D*65, 103522 (2002), D. Wands, *Phys. Rev. D*60 (1999)

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

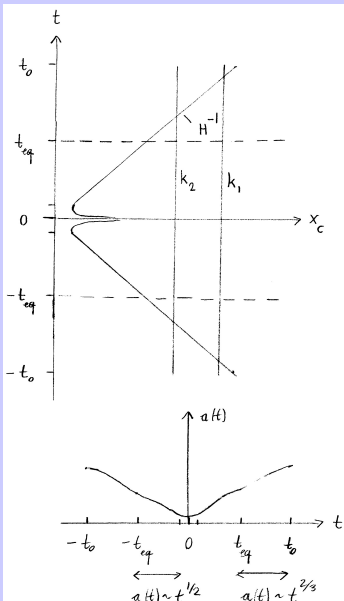
General

Inflation

String Gas

Bounce

Conclusions



Overview of the Matter Bounce

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- Fluctuations originate as **quantum vacuum perturbations** on sub-Hubble scales in the contracting phase.
- **Adiabatic** fluctuation mode acquires a **scale-invariant spectrum** of curvature perturbations on super-Hubble scales.
- **Horizon problem**: absent.
- **Anisotropy problem**: weak point.
- **Size and entropy problems**: not present if we assume that the universe begins cold and large.

Overview of the Matter Bounce

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- Fluctuations originate as **quantum vacuum perturbations** on sub-Hubble scales in the contracting phase.
- **Adiabatic** fluctuation mode acquires a **scale-invariant spectrum** of curvature perturbations on super-Hubble scales.
 - **Horizon problem**: absent.
 - **Anisotropy problem**: weak point.
 - **Size and entropy problems**: not present if we assume that the universe begins cold and large.

Overview of the Matter Bounce

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Origin of Scale-Invariant Spectrum

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- The initial vacuum spectrum is blue:

$$P_{\zeta}(k) = k^3 |\zeta(k)|^2 \sim k^2$$

- The curvature fluctuations grow on super-Hubble scales in the contracting phase:

$$v_k(\eta) = c_1 \eta^2 + c_2 \eta^{-1},$$

- For modes which exit the Hubble radius in the **matter phase** the resulting spectrum is scale-invariant:

$$\begin{aligned} P_{\zeta}(k, \eta) &\sim k^3 |v_k(\eta)|^2 a^{-2}(\eta) \\ &\sim k^3 |v_k(\eta_H(k))|^2 \left(\frac{\eta_H(k)}{\eta}\right)^2 \sim k^{3-1-2} \\ &\sim \text{const}, \end{aligned}$$

Bispectrum of the Matter Bounce Scenario

Y. Cai, W. Xue, R.B. and X. Zhang, *JCAP* 0905:011 (2009)

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

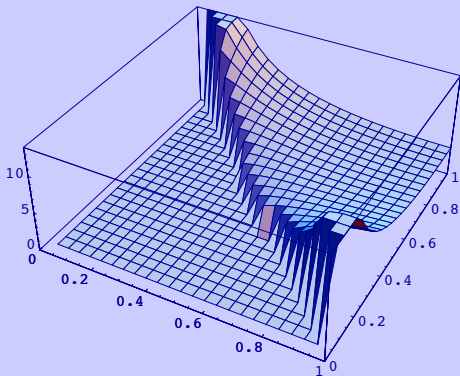
General

Inflation

String Gas

Bounce

Conclusions



Challenges for the Matter Bounce Scenario

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- Obtaining a matter bounce in a model free of ghosts and other unwanted degrees of freedom.
- **Instability to anisotropic stress.**
- Initial conditions for fluctuations?

Cyclic Cosmology - Never Cyclic

R.B. , Phys.Rev. D80 (2009) 023535

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- Consider a 4-d cyclic background cosmology.
- Curvature fluctuations grow both in the contracting and in the expanding phase.
- Fluctuations break the cyclicity (related to Tolman's entropy problem).
- Index of the spectrum of cosmological perturbations changes by -2 from cycle to cycle.
- 4-d cyclic cosmology is not predictive.

Cyclic Cosmology - Never Cyclic

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Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Cyclic Cosmology - Never Cyclic

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Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- Consider a 4-d cyclic background cosmology.
- Curvature fluctuations grow both in the contracting and in the expanding phase.
- Fluctuations break the cyclicity (related to Tolman's entropy problem).
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Cyclic Cosmology - Never Cyclic

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Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Plan

Alternatives

R. Branden-
berger

Introduction

Motivation
Inflation
Problems
Message

Alternatives

Emergent

Bounce

Perturbations

General
Inflation
String Gas
Bounce

Conclusions

- 1 Introduction
 - Motivation
 - Review of Inflationary Cosmology
 - Problems of Inflationary Cosmology
 - Message and Preview
- 2 Overview of Alternatives
- 3 Realizing an Emergent Universe Scenario
- 4 Models for a Nonsingular Bounce
- 5 Cosmological Perturbations
 - General Theory
 - Application to Inflationary Cosmology
 - String Gas Cosmology and Structure Formation
 - Application to Matter Bounce Cosmology
- 6 Conclusions

Conclusions

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- **Inflationary cosmology** suffers from several conceptual problems.
- These problems motivate the investigation of **alternatives**.
- Alternative A: **Emergent Universe** scenario, realized in the context of **String Gas Cosmology** — Based on fundamental principles of superstring theory.
- Alternative B: **Matter bounce** — Based on string gases, Hořava-Lifshitz gravity or on ghost condensate construction.
- The problem of time takes a different form in both alternative scenarios.

Conclusions

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Conclusions

Alternatives

R. Branden-
berger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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Conclusions II

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

- These alternatives are consistent with current observations.
- In A: Thermal fluctuations of a gas of strings \rightarrow scale-invariant spectrum of cosmological perturbations.
- In B: Vacuum fluctuations exiting Hubble radius in a matter-dominated phase of contraction lead to a scale-invariant spectrum of adiabatic perturbations.
- Both alternatives make testable predictions for future observations.
 - in A: Blue spectrum of gravitational waves.
 - in B: specific shape of the bispectrum.

Conclusions II

Alternatives

R. Brandenberger

Introduction

Motivation

Inflation

Problems

Message

Alternatives

Emergent

Bounce

Perturbations

General

Inflation

String Gas

Bounce

Conclusions

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