

Evolution of Diversity and Cooperation

3 / 3

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The logo for UIMP (Universidad Internacional Menéndez Pelayo), consisting of the letters "UIMP" in a bold, red, serif font, with "Universidad Internacional Menéndez Pelayo" in a smaller, black, sans-serif font below it.

UIMP
Universidad Internacional
Menéndez Pelayo

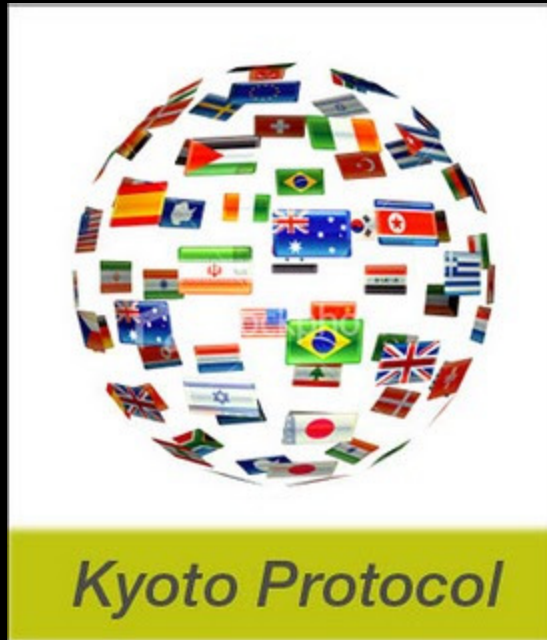
The logo for Fis y Mat, with the letters "F", "i", "s", "y", "M", "a", "t" in a red, sans-serif font, where the "y" is white and set within a red square.

Fis y Mat



Luis Santaló School, 15th of July, 2013

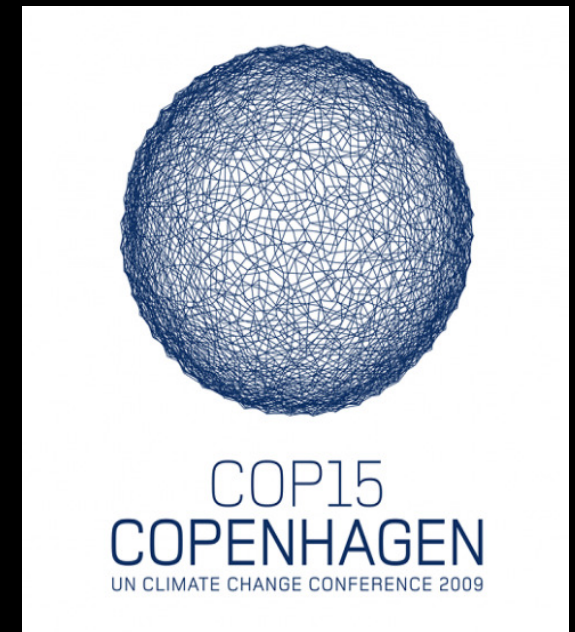
the challenge of minimizing climate change
cooperation between ALL countries@once ?



1997
(decided)



2005
(into action)
(191)



2009

failure of global summits has been attributed to:

- ⊙ overall perception of risk is too small
- ⊙ no institution to monitor and sanction those not abiding

the challenge of minimizing climate change
cooperation between SOME countries or SOME peoples ?

Indigenous Peoples' Global Summit on Climate Change

Anchorage, April 2009



The Anchorage Declaration

Regional messages

The Anchorage Declaration

Dialogues with other sectors

Recurring themes

Tiquipaya, Bolivia
April 2010



World People's Conference on Climate Change and the
Rights of Mother Earth

Building the People's World Movement for Mother Earth

the challenge of minimizing climate change

cooperation between individuals ?

cooperation between ALL countries ?

cooperation between SOME countries ?

cooperation between SOME peoples ?

cooperation between regions ?

certainly ! **COOPERATION**

per capita CO₂ emmisions

france / sweden

x

UK / japan

2x

USA

3x

the challenge of minimizing climate change

the **cooperation** we need to consider involves **collective action**
public goods games (N-person games)

france / sweden

x

UK / japan

2x

USA

3x

tragedy of the commons



N-person games typify the theoretical framework that captures the ***tragedy of the commons***

how to escape it ?

a game experiment on climate change

[Milinski *et al.*, PNAS 195 (2008) 2291

6 players, 10 rounds

each player : 40 €

contribution in each round : 0 (selfish), 2 (fair) or 4 (altruistic)

cost for saving the planet : 120 €

if \sum contributions \geq 120 €, **planet is saved and each gets away with money left**

if \sum contributions $<$ 120 €, **planet is saved with 10% prob., else all loose everything**

	<i>per capita CO₂ emissions</i>	<i>strategy</i>
france / sweden	x	<i>altruistic</i>
UK / japan	2x	<i>fair</i>
USA	3x	<i>selfish</i>

a game experiment on climate change

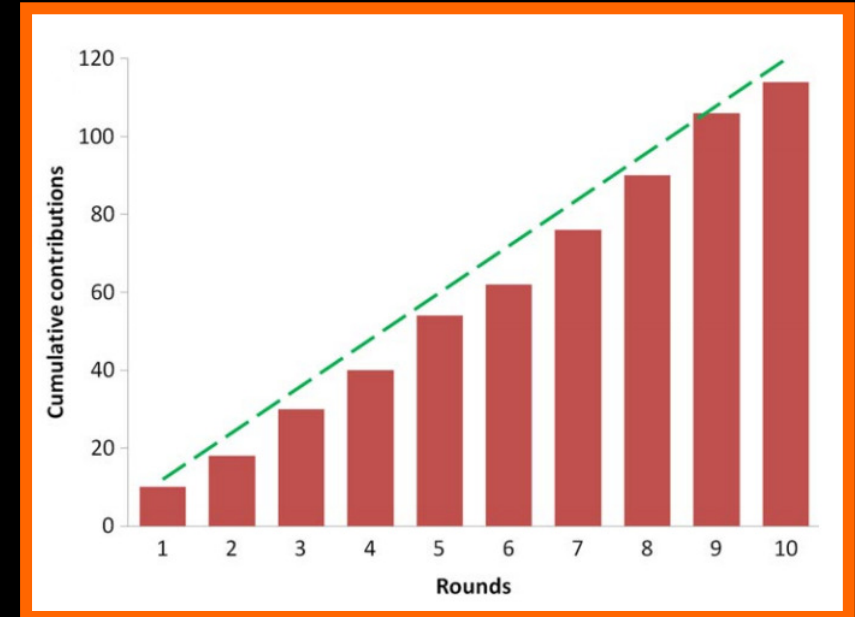
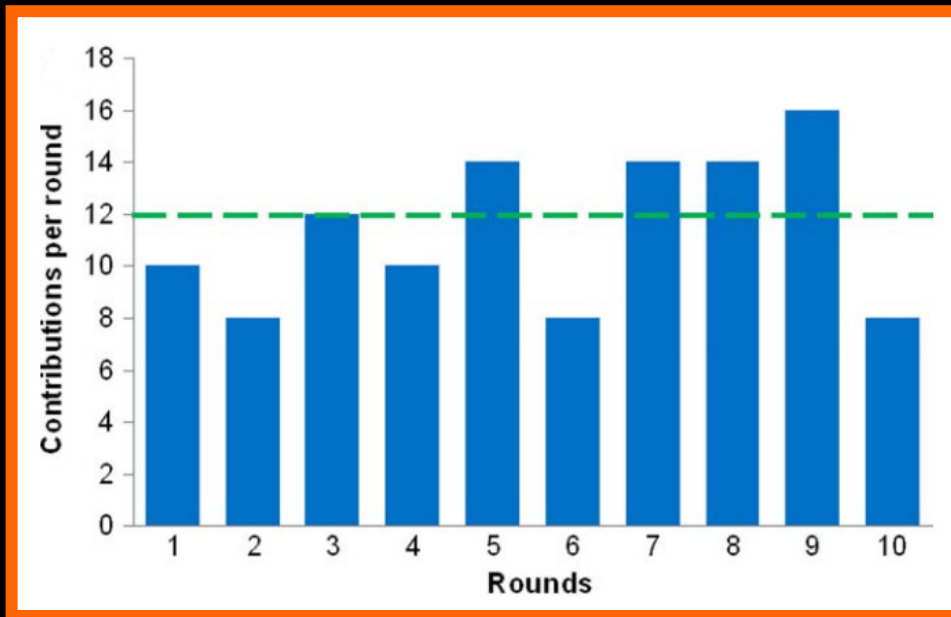
[Milinski *et al.*, *PNAS* 195 (2008) 2291

(one) NASH equilibrium : each player contributes 2€ per round

RESULTS : 50% of times planet was saved !!!

50% of times average contribution = 113 € < 120 €

example of a failed attempt :



did altruists feel they had contributed enough ?

what was in the mind of the free riders ?

these experiments portray, once more, among other things, the **bounded rationality** of human participants.

more economic experiments on climate change

[Milinski et al., PNAS 105 (2008) 2291]
[Tavoni et al., PNAS 108 (2011) 11825]
[Barrett & Dannenberg, PNAS 109 (2012) 17375]

results

- ◎ **risk** plays a very important role

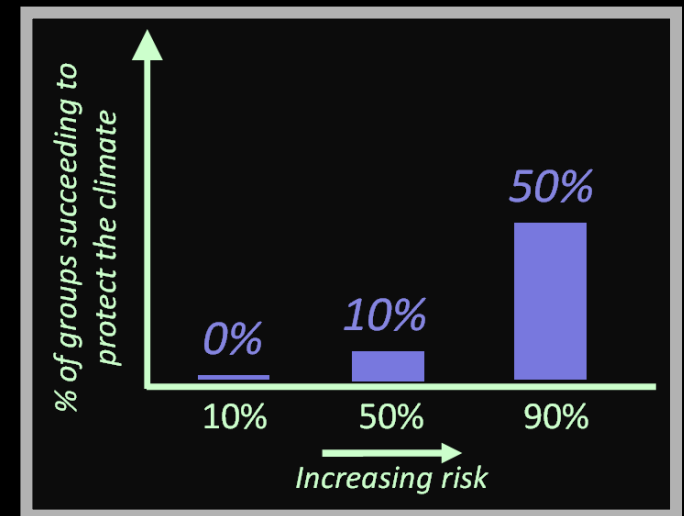
[Milinski et al., PNAS 105 (2008) 2291]

- ◎ pre-play communication helps coordinating to meet **M**

[Tavoni et al., PNAS 108 (2011) 11825]

- ◎ uncertainty in **M** may destroy cooperation

[Barrett & Dannenberg, PNAS 109 (2012) 17375]



message from the game experiments on climate change

perceived risk of disaster  *cooperation* 
rationality of players is not an argument
individuals revise their strategy along the way

drawbacks from the game experiments on climate change

small groups . . . and only 1 group size . . .

finite & small time horizon for investments

repeated game with fixed number of rounds . . .

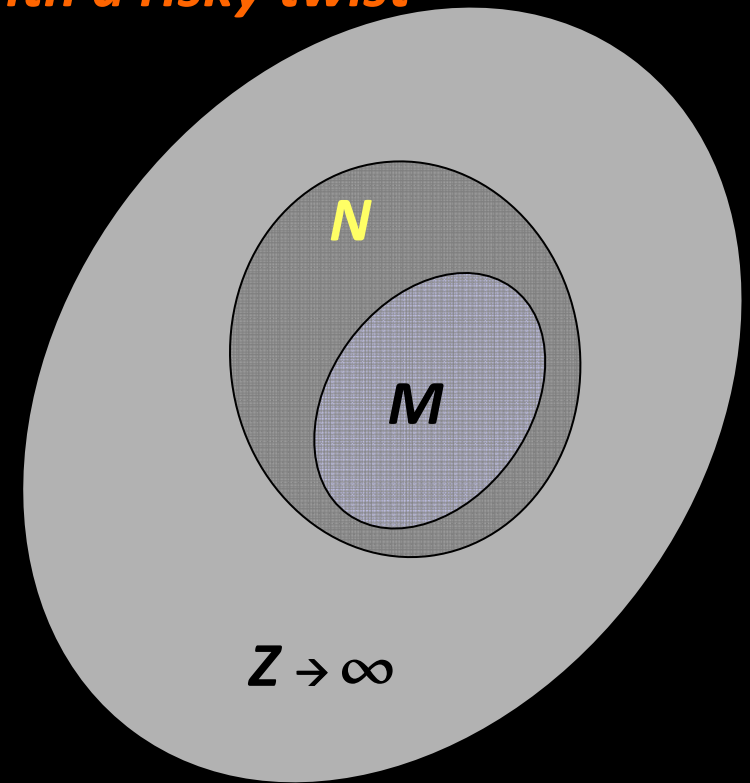
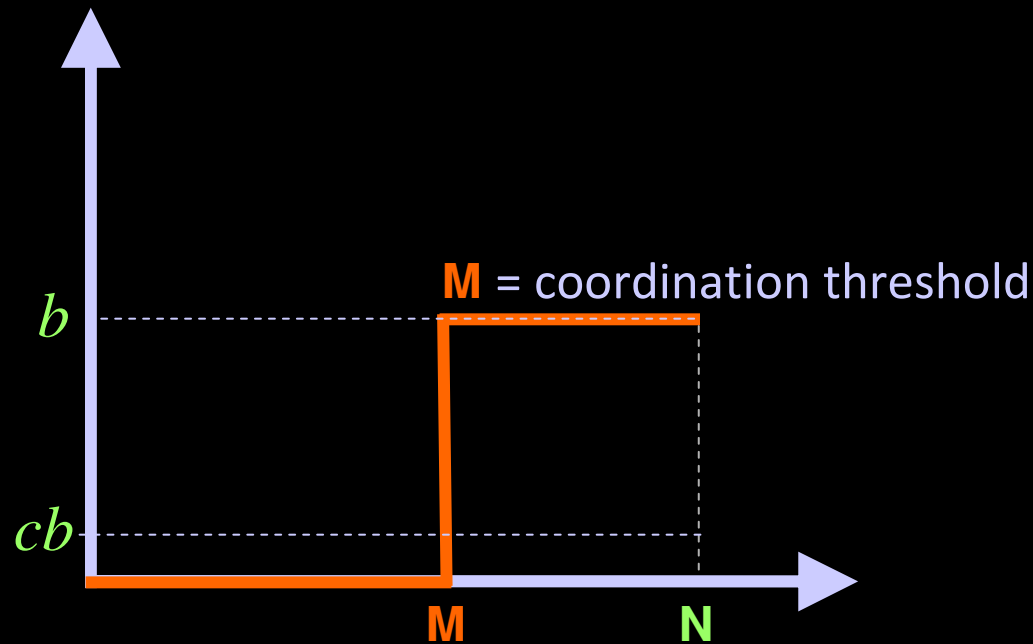
we can say nothing for different population sizes

we can say nothing for different group sizes

how does this apply to the world summits on climate change ?

an *evolutionary* approach to climate change

N-person Coordination game . . . with a risky twist



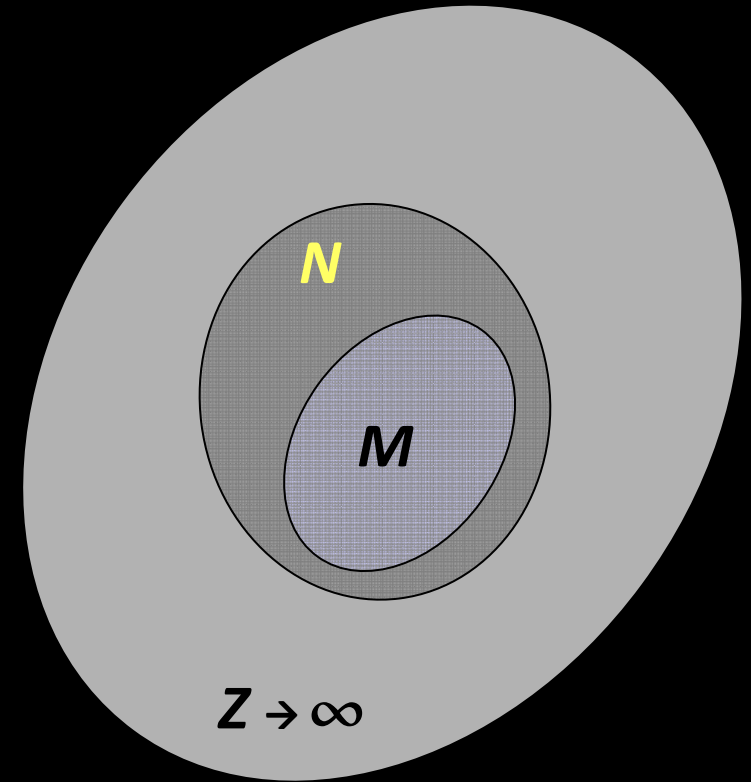
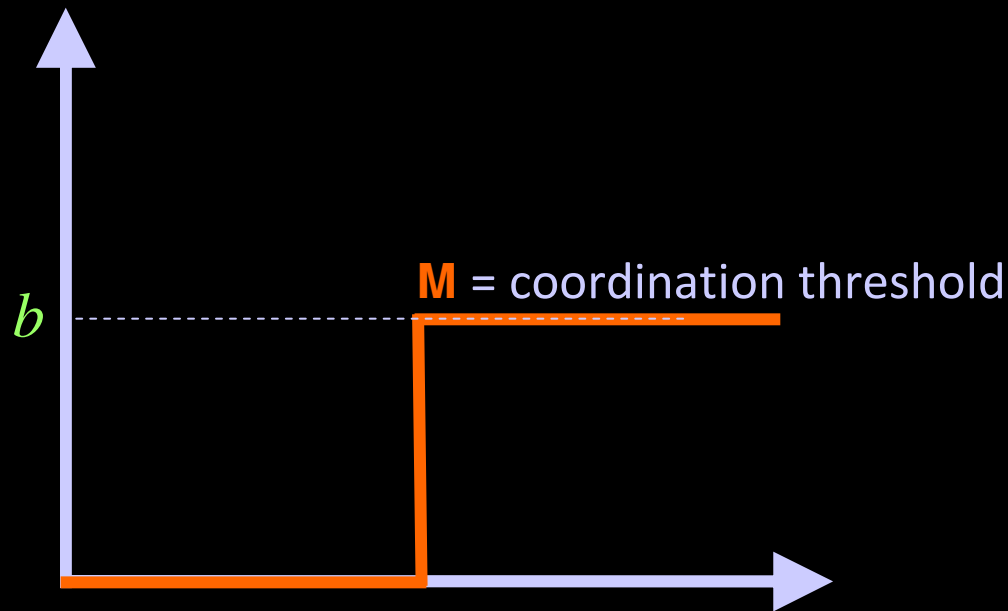
Cooperators contribute an amount cb (cost) to a *public good* which helps reducing GHG emissions

Defectors do not contribute; If $\sum cb < M$ all loose everything with probability r

otherwise : everyone keeps all they have

an *evolutionary* approach to climate change

N-person Coordination game . . . with a risky twist



◎ Evolution \longrightarrow **REPLICATOR DYNAMICS**

◎ Groups \longrightarrow **WELL-MIXED populations**

evolutionary dynamics of N-person coordination games

JmP, F. C. Santos, M. Souza, B. Skyrms, *Proc. Royal Society B* 276 (2009) 1655

M. Souza, F. C. Santos, *JmP*, *J. Theor. Biol.* 260 (2009) 581-588

$$\dot{x} = x(1-x)(f_C(x) - f_D(x))$$

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$$\dot{x} = x(1-x)(f_C(x) - f_D(x))$$

for N -person games in well-mixed populations we have

$$f_D(x) = \sum_{k=0}^{N-1} \binom{N-1}{k} x^k (1-x)^{N-1-k} P_D(k)$$

$$f_C(x) = \sum_{k=0}^{N-1} \binom{N-1}{k} x^k (1-x)^{N-1-k} P_C(k+1)$$

evolutionary dynamics of N-person coordination games

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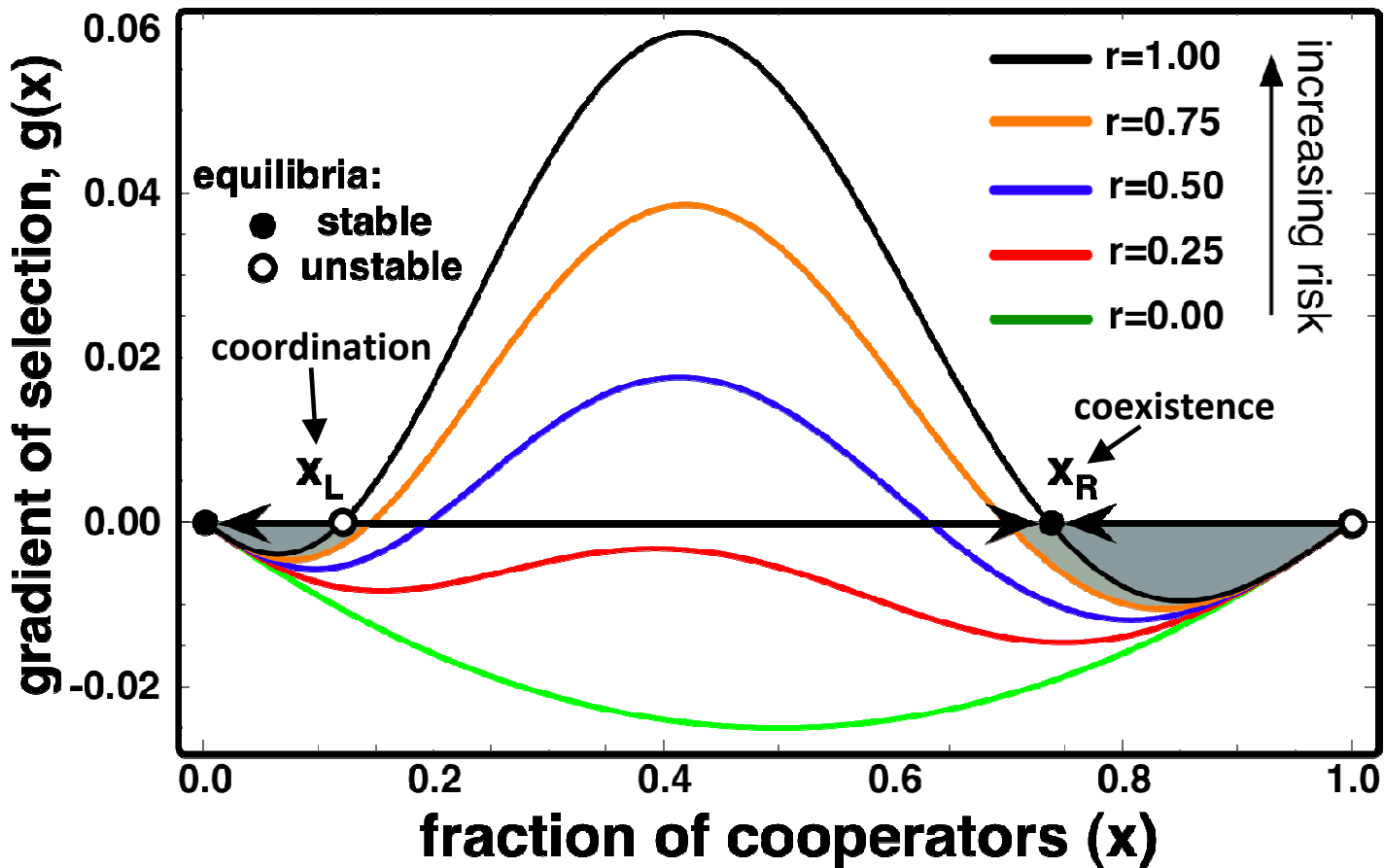
$$f_C(x) = \sum_{k=0}^{N-1} \binom{N-1}{k} x^k (1-x)^{N-1-k} P_C(k+1)$$

we are assuming **infinite populations**; whenever populations are **finite**, **binomial sampling** is replaced by **hypergeometric sampling** and the **replicator dynamics** is also replaced by its **finite population stochastic analogue**.

results

risk-dependence

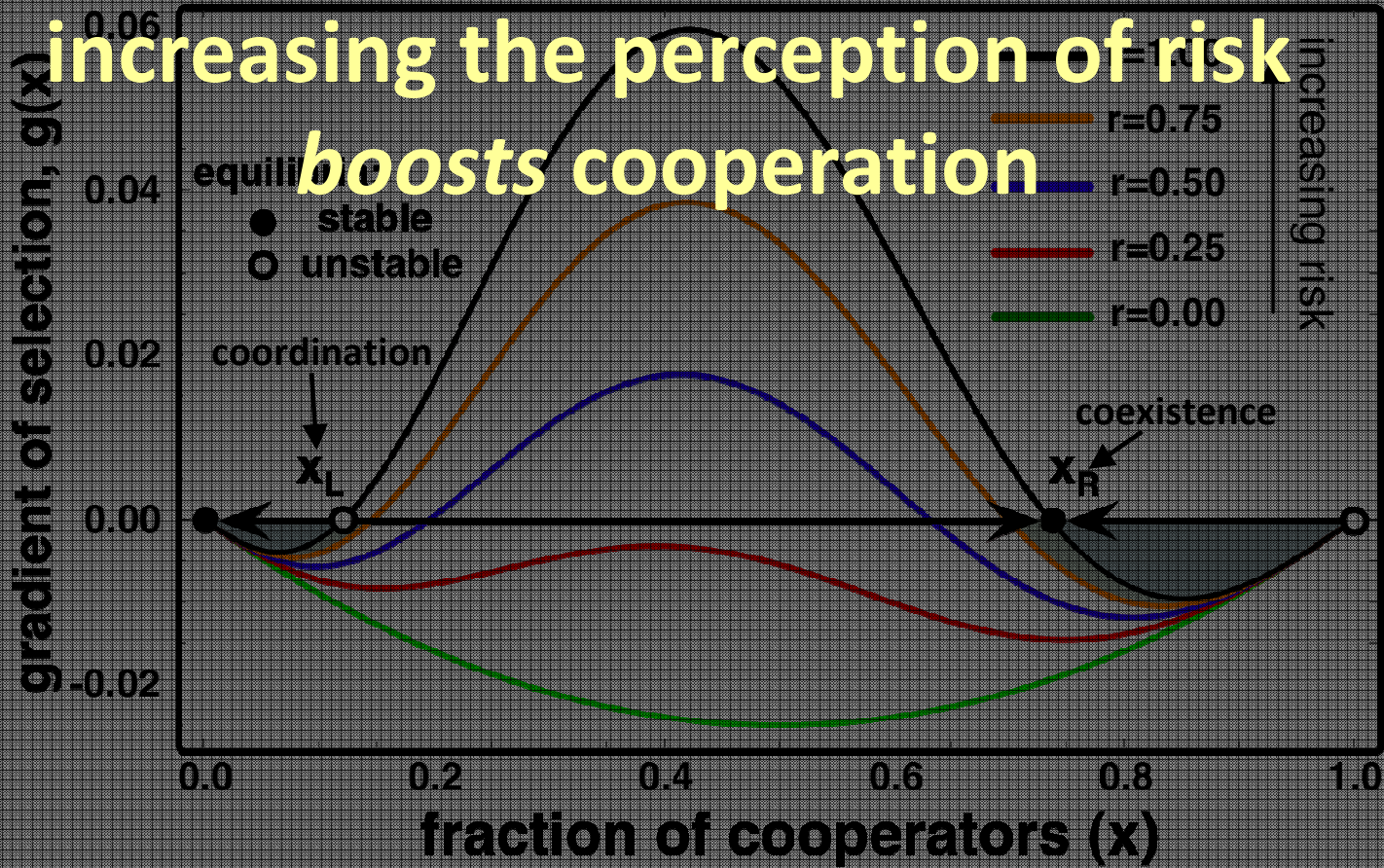
$$Z \rightarrow \infty; N = 6 = 2M; c = 0.1b$$



results

risk-dependence

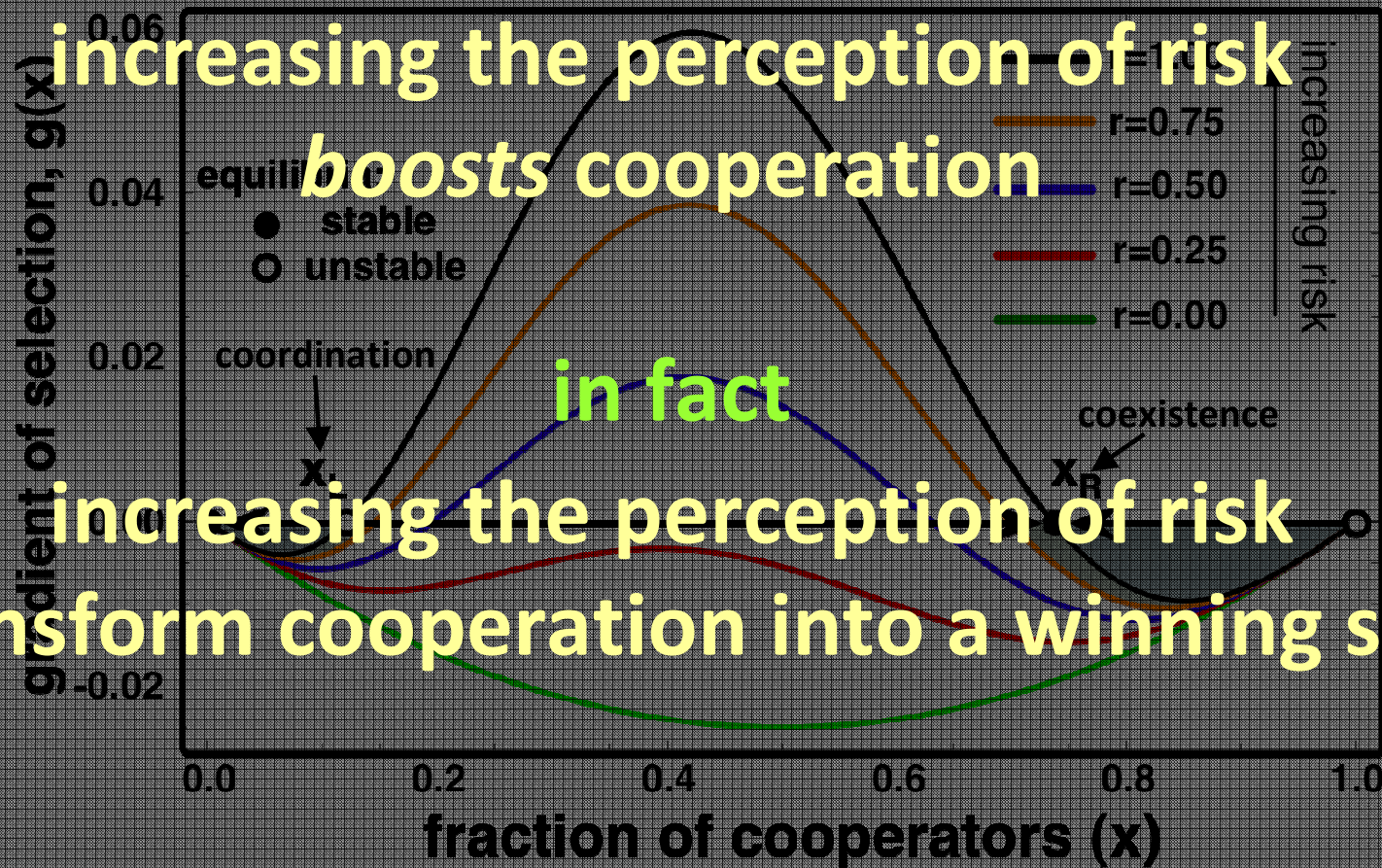
$$Z \rightarrow \infty; N = 6 = 2M; c = 0.1b$$



results

risk-dependence

$$Z \rightarrow \infty; N = 6 = 2M; c = 0.1b$$



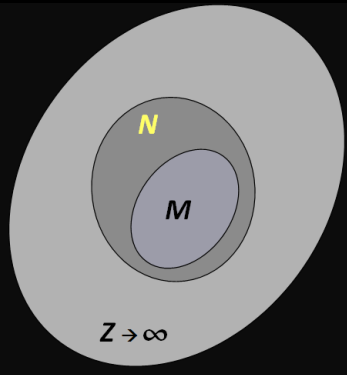
increasing the perception of risk

boosts cooperation

in fact

increasing the perception of risk

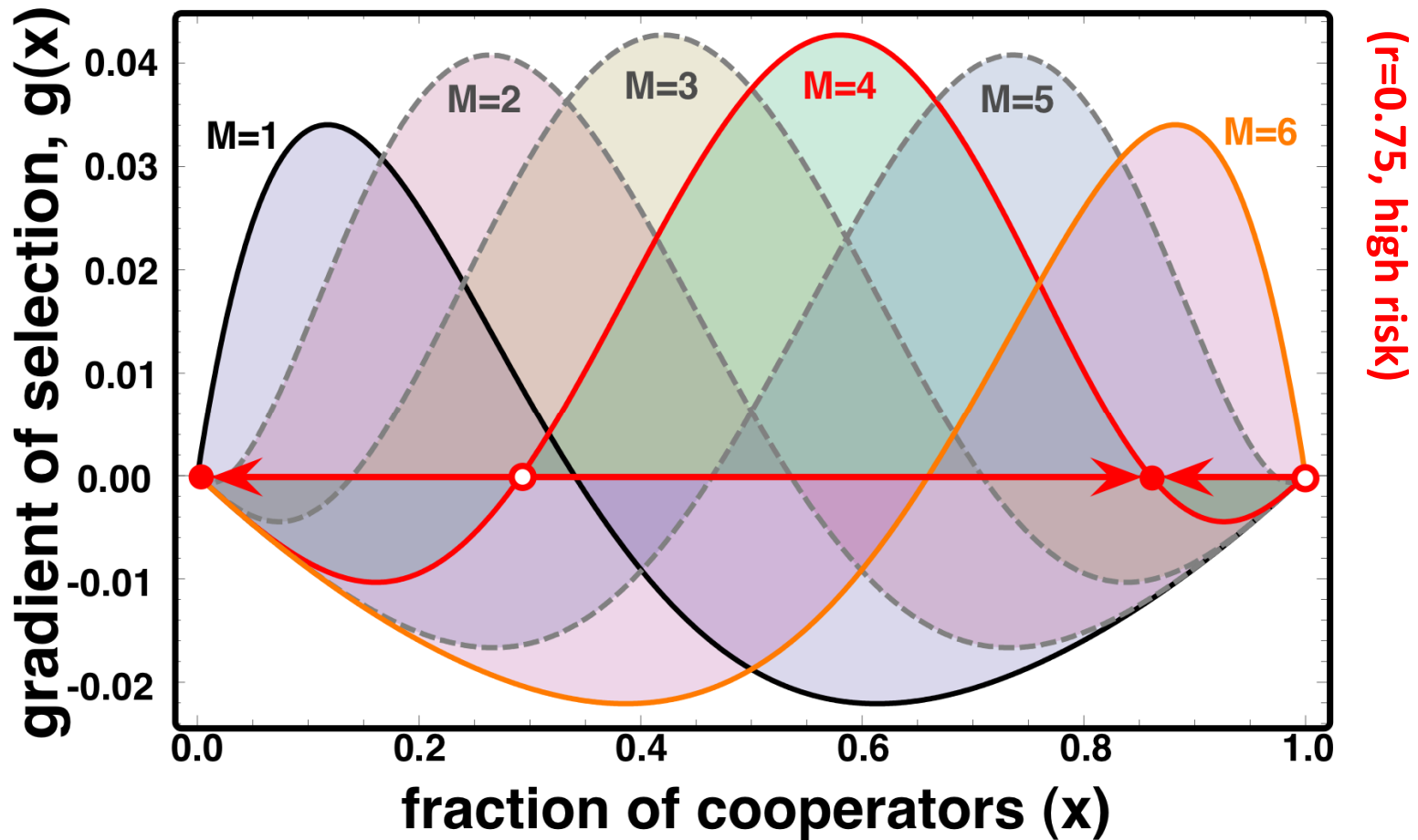
may transform cooperation into a winning strategy

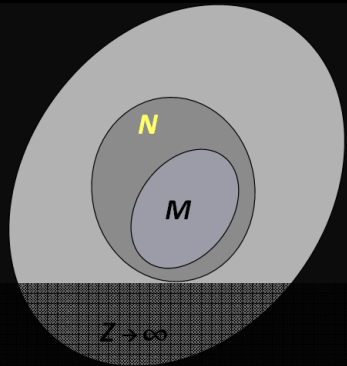


results

threshold-dependence

$$Z \rightarrow \infty; N = 6; c = 0.1b$$

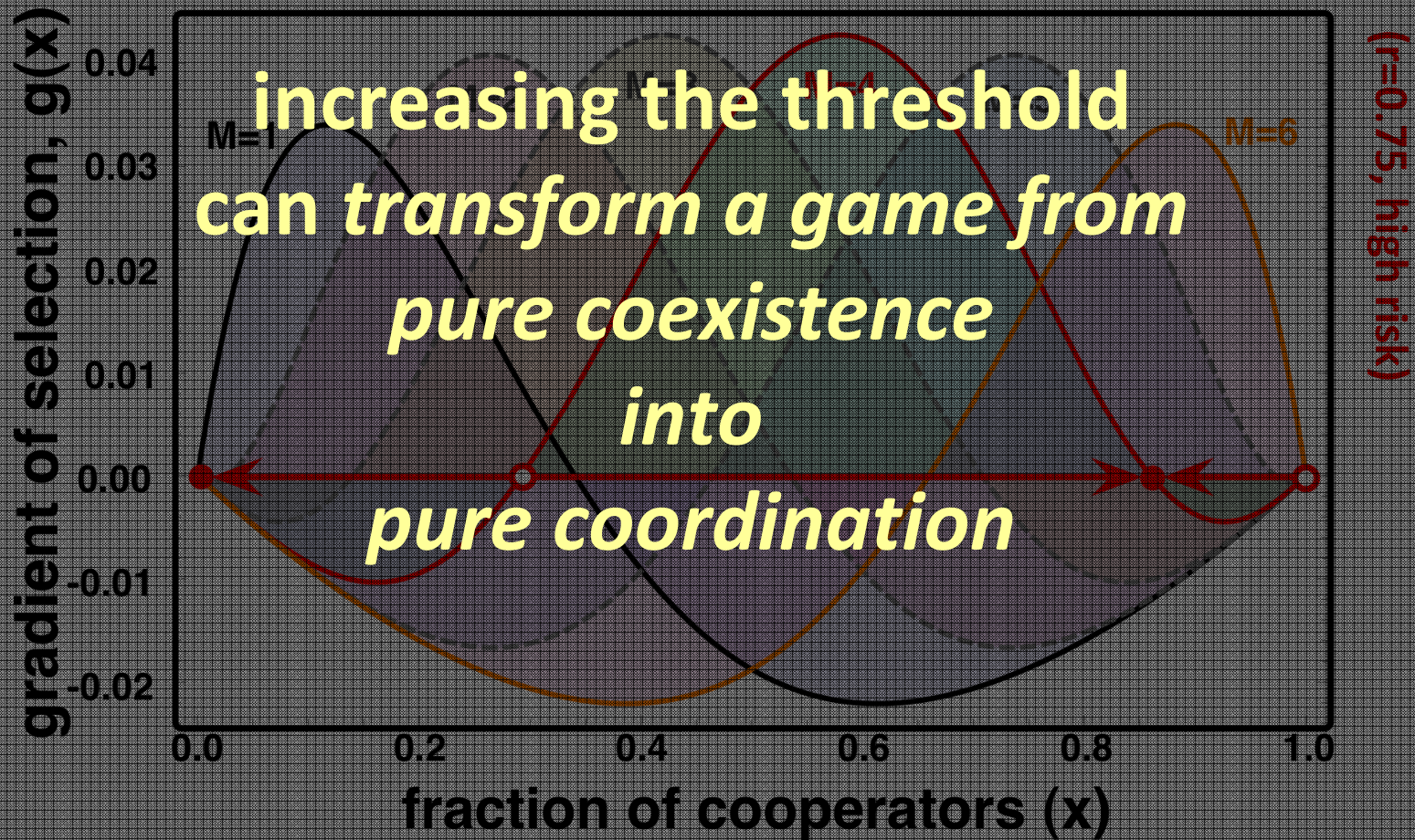


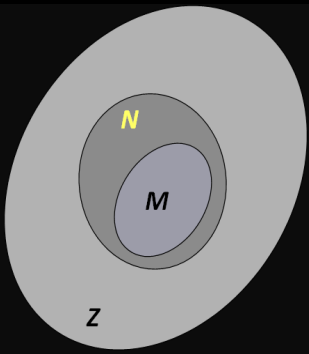


results

threshold-dependence

$$Z \rightarrow \infty; N = 6; c = 0.1b$$



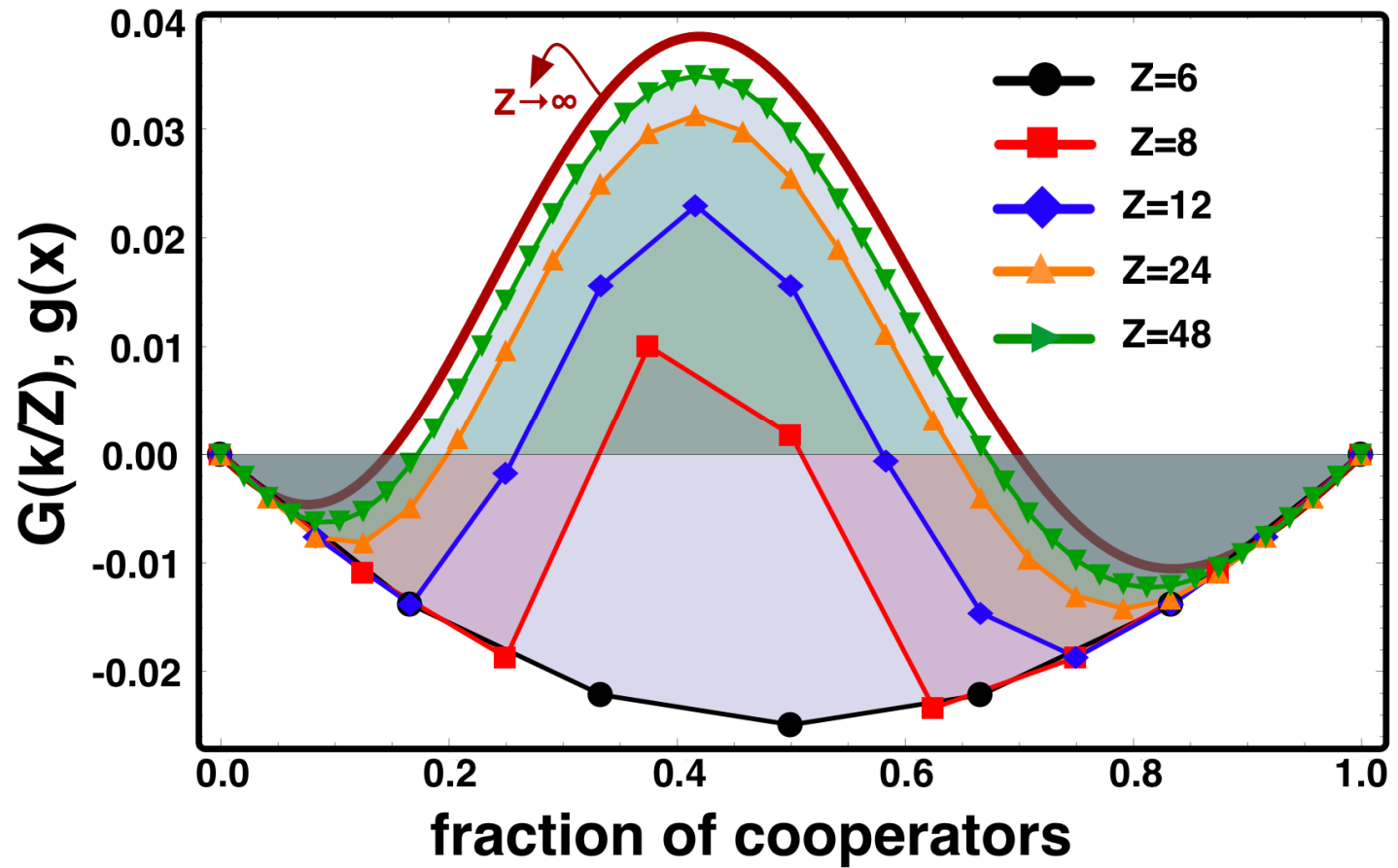


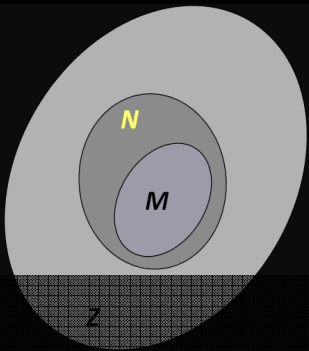
results

population-size dependence

$$N = 6 = 2M; c = 0.1b$$

($r=1.0$, highest risk)



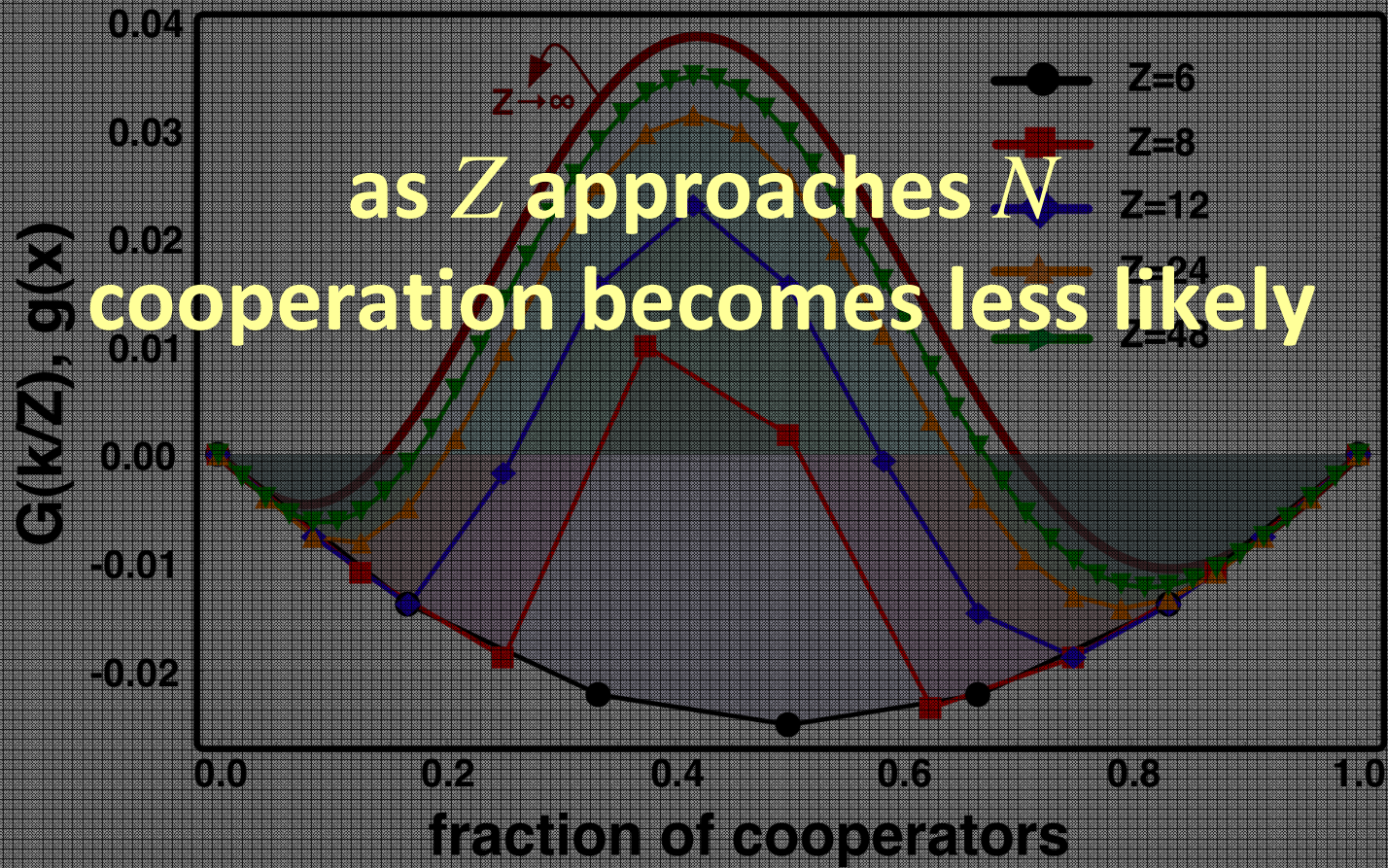


results

population-size dependence

$$N = 6 = 2M; c = 0.1b$$

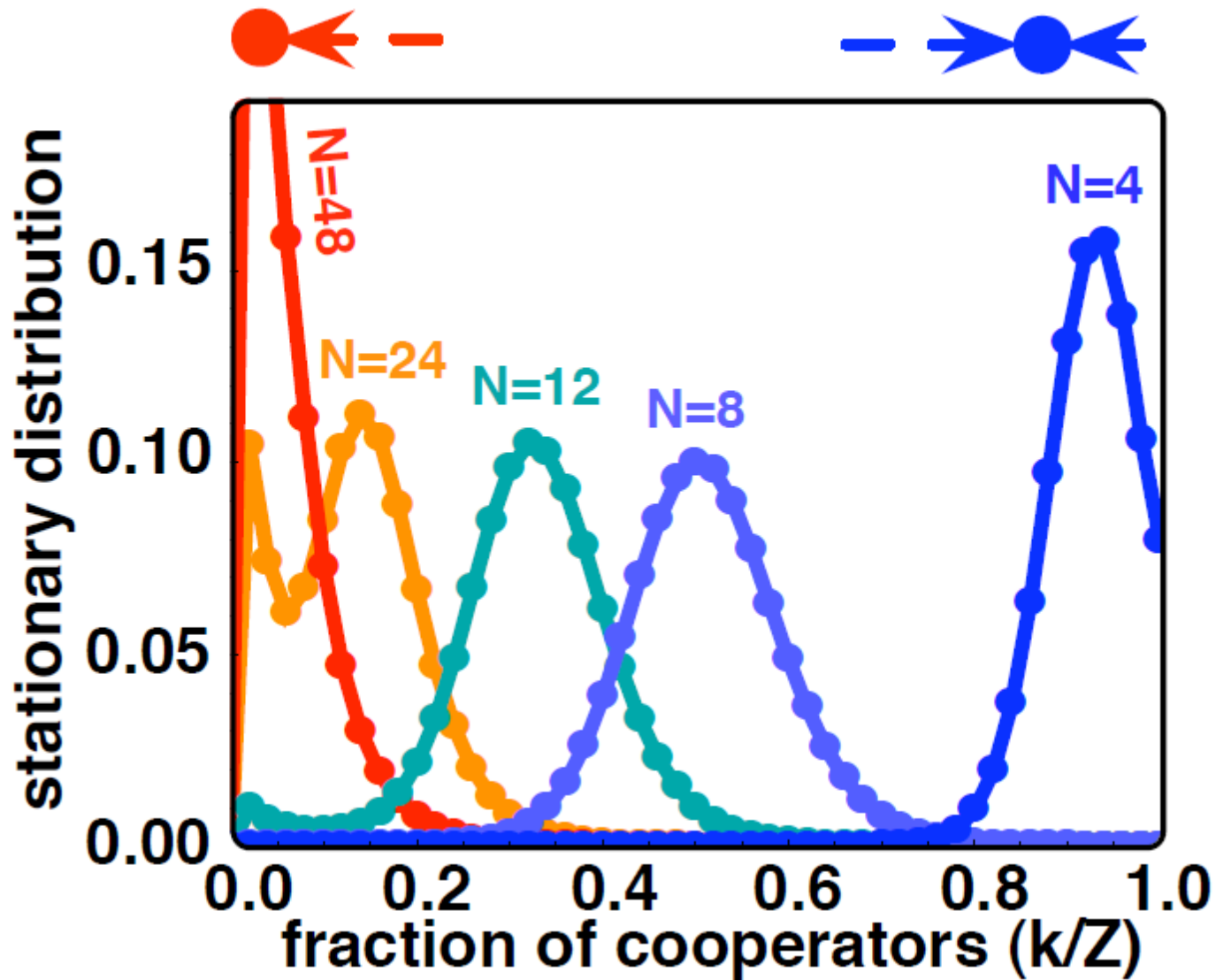
($r=1.0$, highest risk)



results

what about group size ?

$$Z = 50; M = 3; c/r = 0.15$$



summary

cooperation  when :

perception of risk 

group size 

threshold 

population size 

summary

cooperation  when :

perception of risk 

group size 

threshold 

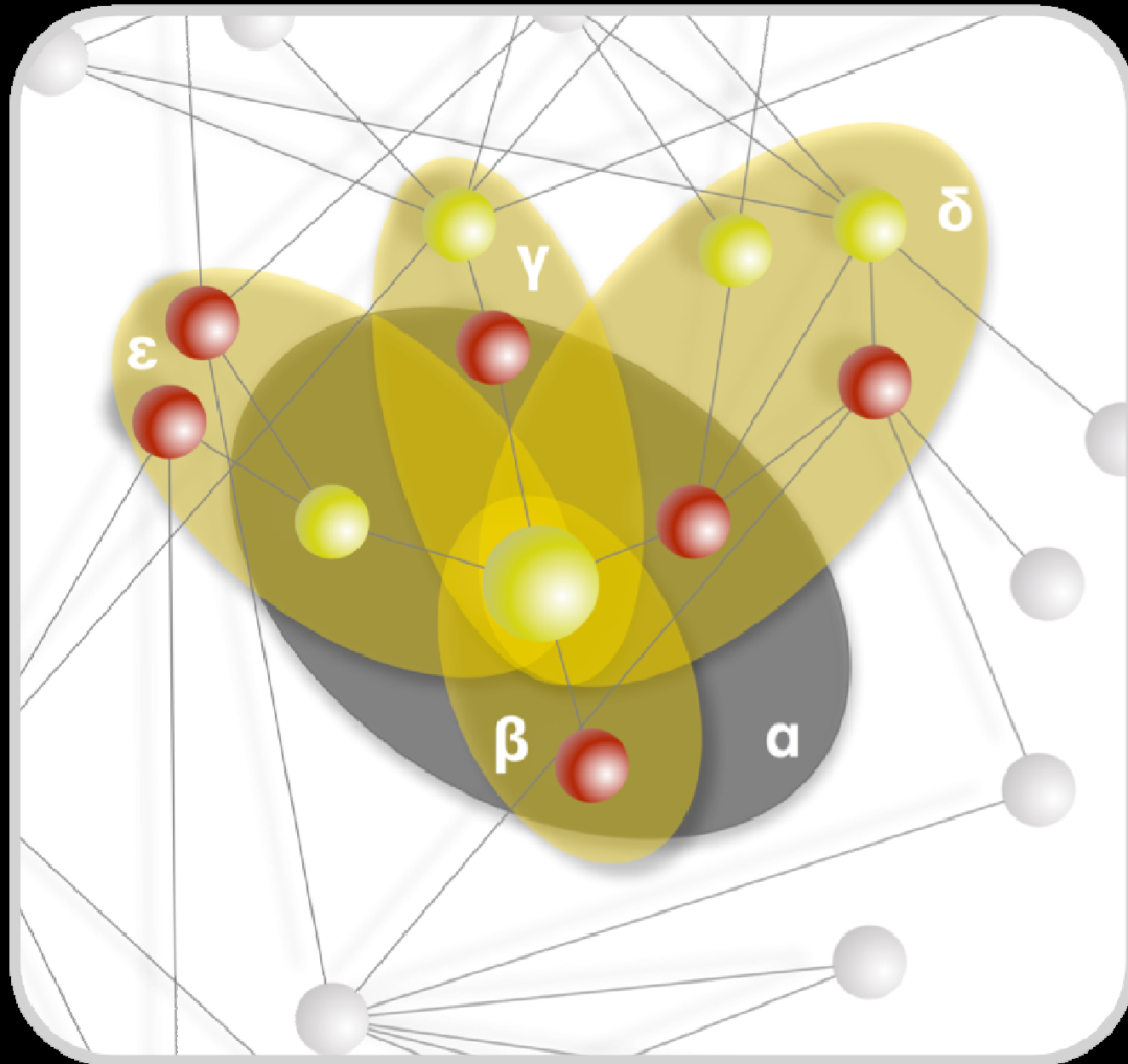
population size 

can we further improve cooperation ?

additional mechanisms

- ❖ *networked* public goods games of cooperation
- ❖ setting up *sanctioning institutions* – *in which way* ?

networked public goods games of cooperation



networked public goods games of cooperation

how to define the networks ? some ideas . . .

networks could be defined based on *groups of countries* bound by common interests, such as

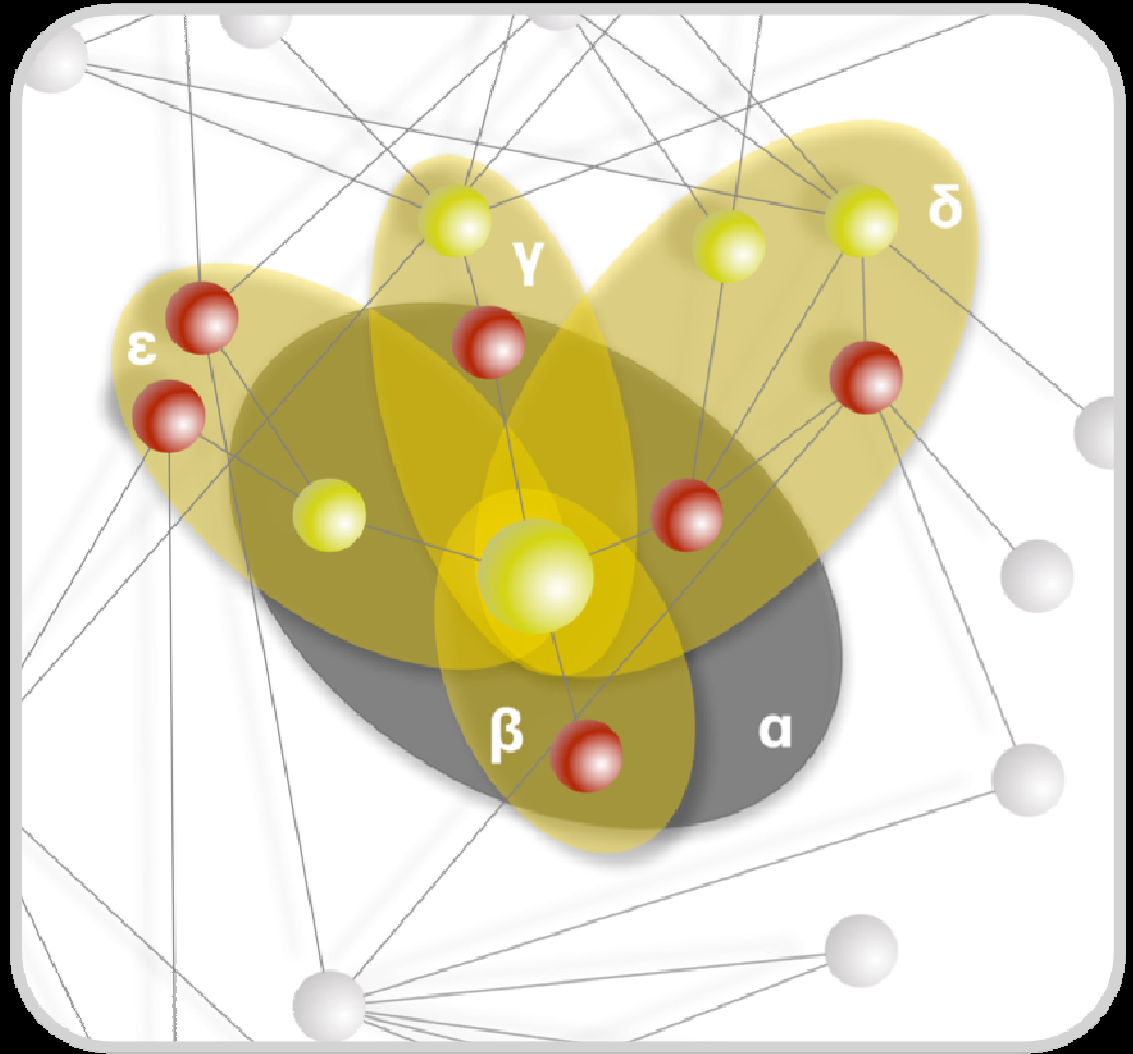
- **alternative forms of energy**
- **similar means of managing CO₂ emissions**
- **joint interest in local commons**
- *etc . . .*

or groups of regions bound by common interests
(ex: California in *USA*, Catalonia in *Spain*, Bavaria in *Germany*, etc.)

Introducing diversity

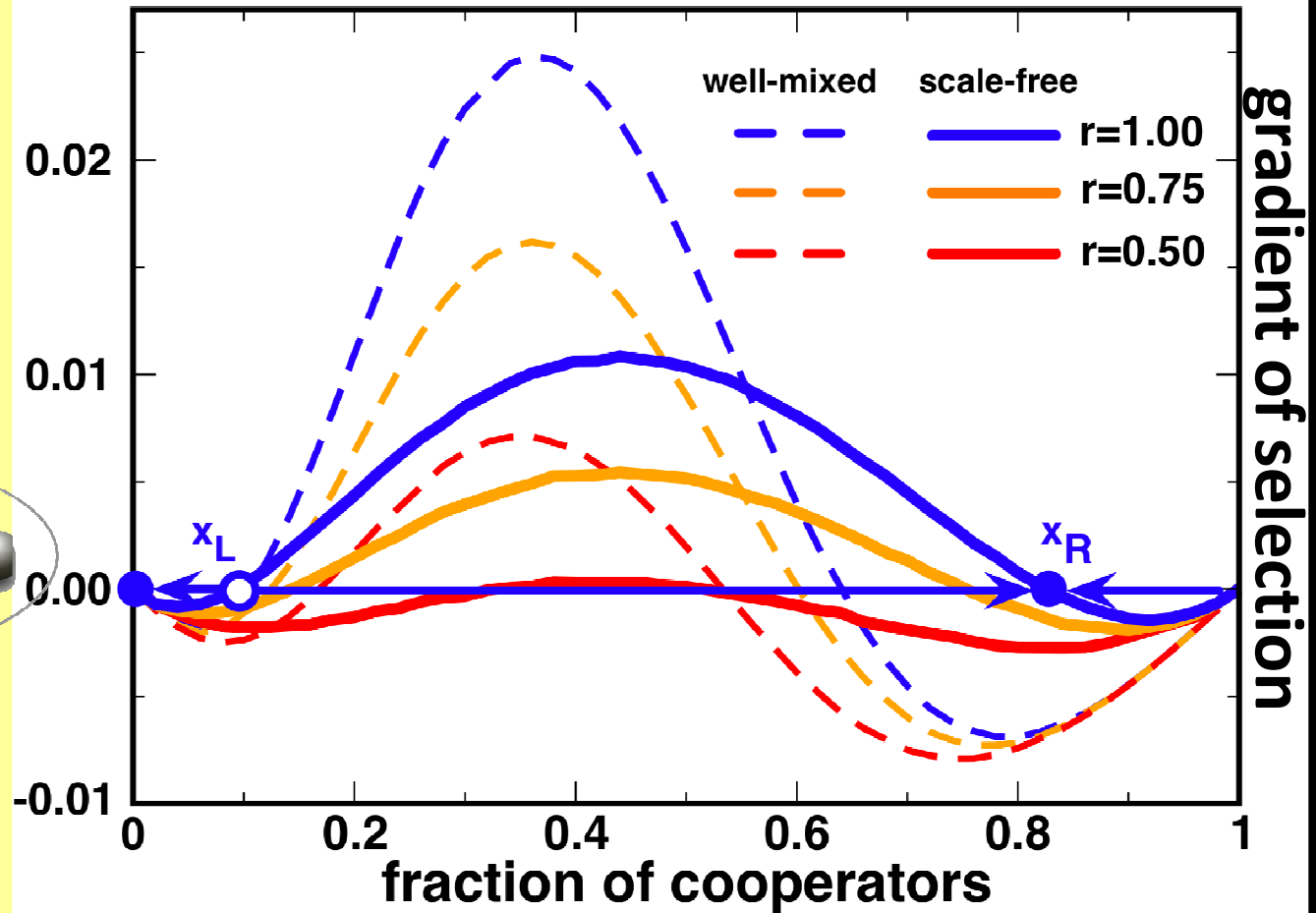
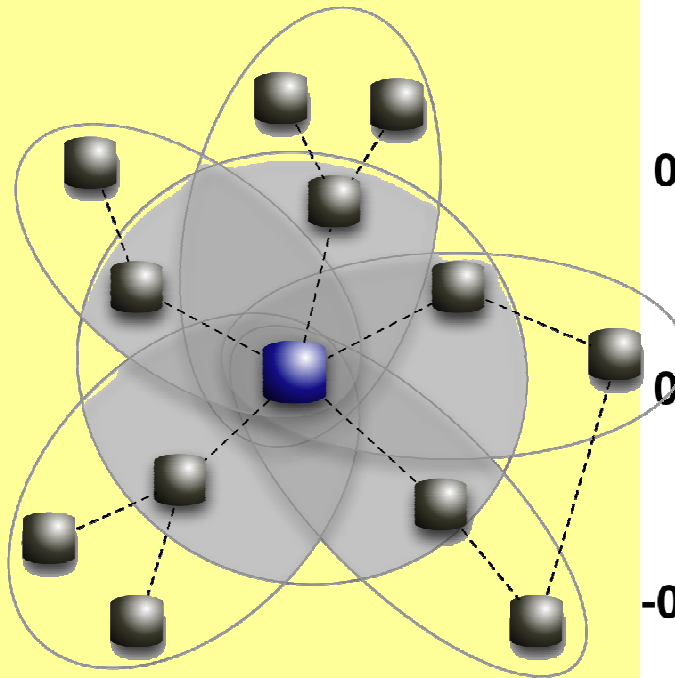
Collective risk games
in structured
populations

*each
neighborhood
defines a
game/group.*



results

The role of diversity (numerical results)



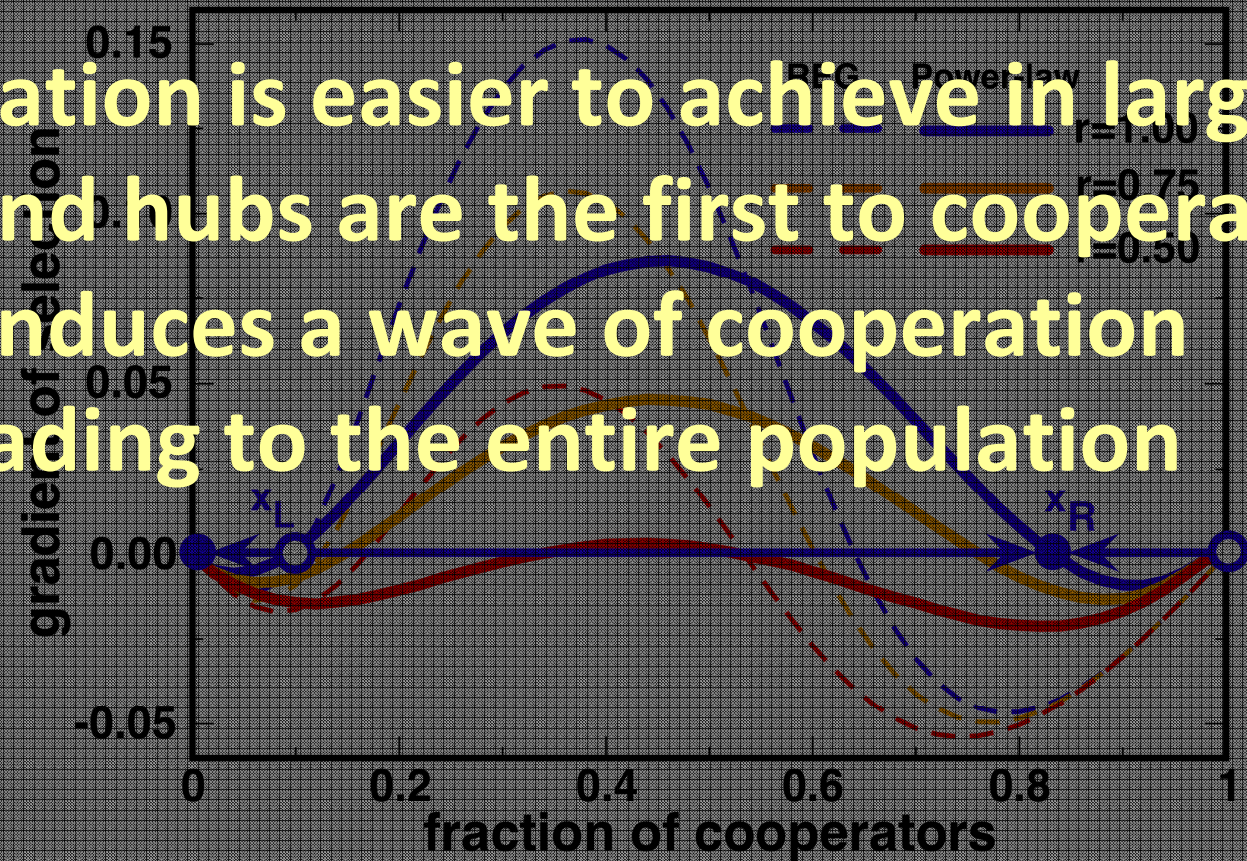
$$Z = 500; \langle N \rangle = 7; N_{\min} = 4; M = 3; c = 0.1b$$

results

The role of diversity (numerical results)



coordination is easier to achieve in large groups, and hubs are the first to cooperate; this induces a wave of cooperation spreading to the entire population



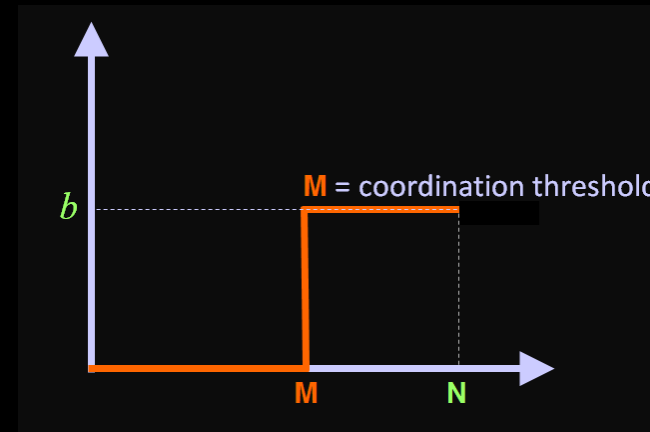
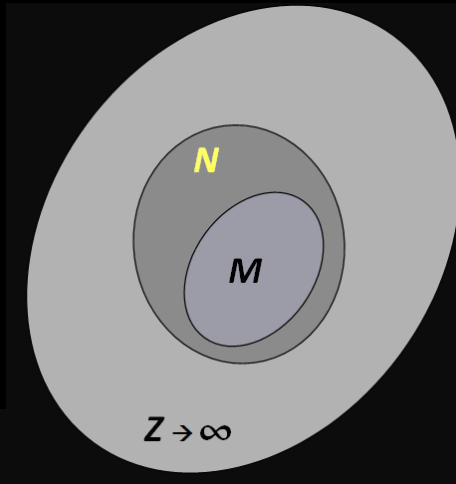
our EGT approach suggests

- ◎ many small groups (better: in a diverse set of groups)
- ◎ high perception of risk
- ◎ stringent thresholds to meet goals (high M)
- ◎ exploit the heterogeneous nature of the interaction structure.

and what about sanctioning institutions ?

same N-person Coordination game . . . with a risky twist

[Vasconcelos, Santos & Pacheco, Nature Climate Change (2013) in press]



group size is N ;

C s **always** contribute to the public good

D s **never** contribute to the public good

P s also contribute to the public good

also contribute a *punishment tax* π_t to an institution which will impose a fine Δ to all D s whenever the number of P s exceeds n_p

this, however, **does not tell the whole story** :

Institutions may be *local* or *global*, and this affects the way in which sanctions are applied.

global versus *local* institutions

global institution : in this case

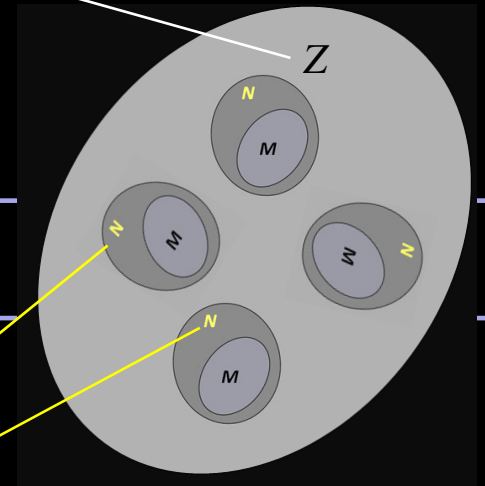
$$0 < n_p \leq Z$$

and sanctions affect *all* *D*s in the *population*

local institutions : in this case

$$0 < n_p \leq N$$

and sanctions affect *all* *D*s in the *group* in which the punishing thresholds were surpassed

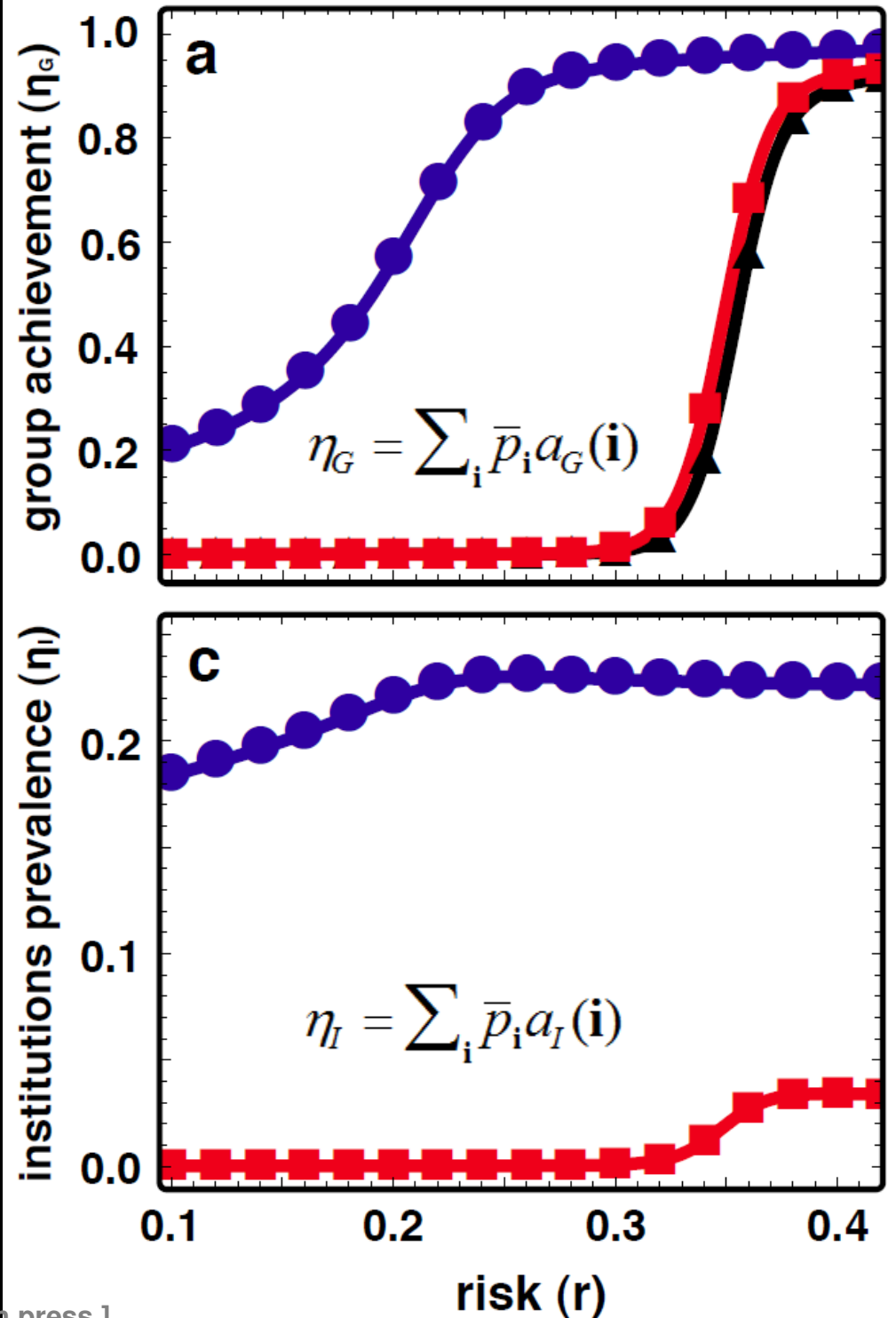


global versus
local versus
lack of
institutions

- local institutions
- global institutions
- ▲ without institutions

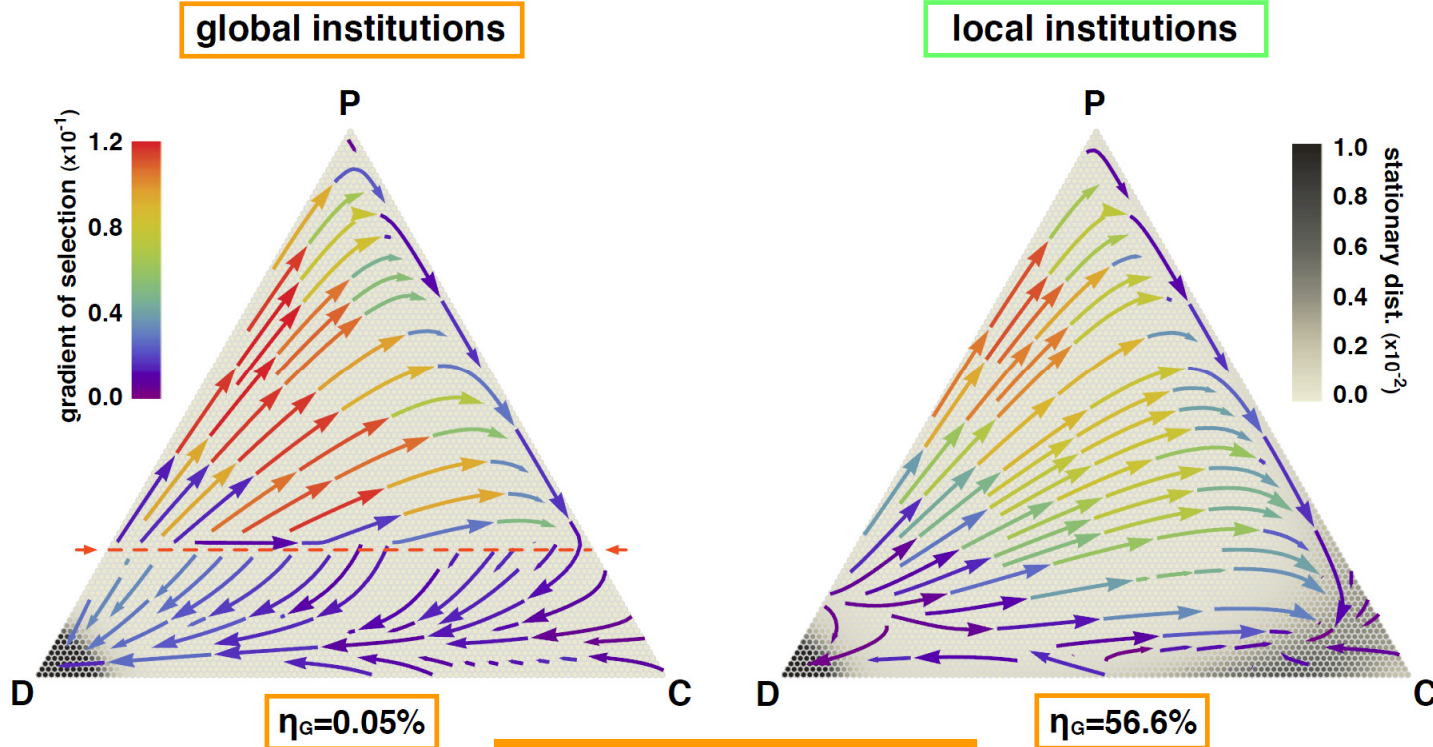
$a_G(\mathbf{i}) = 1$ whenever, for configuration \mathbf{i} ,
a group achieves the public good

$a_I(\mathbf{i}) = 1$ whenever, for configuration \mathbf{i} ,
an institution is formed

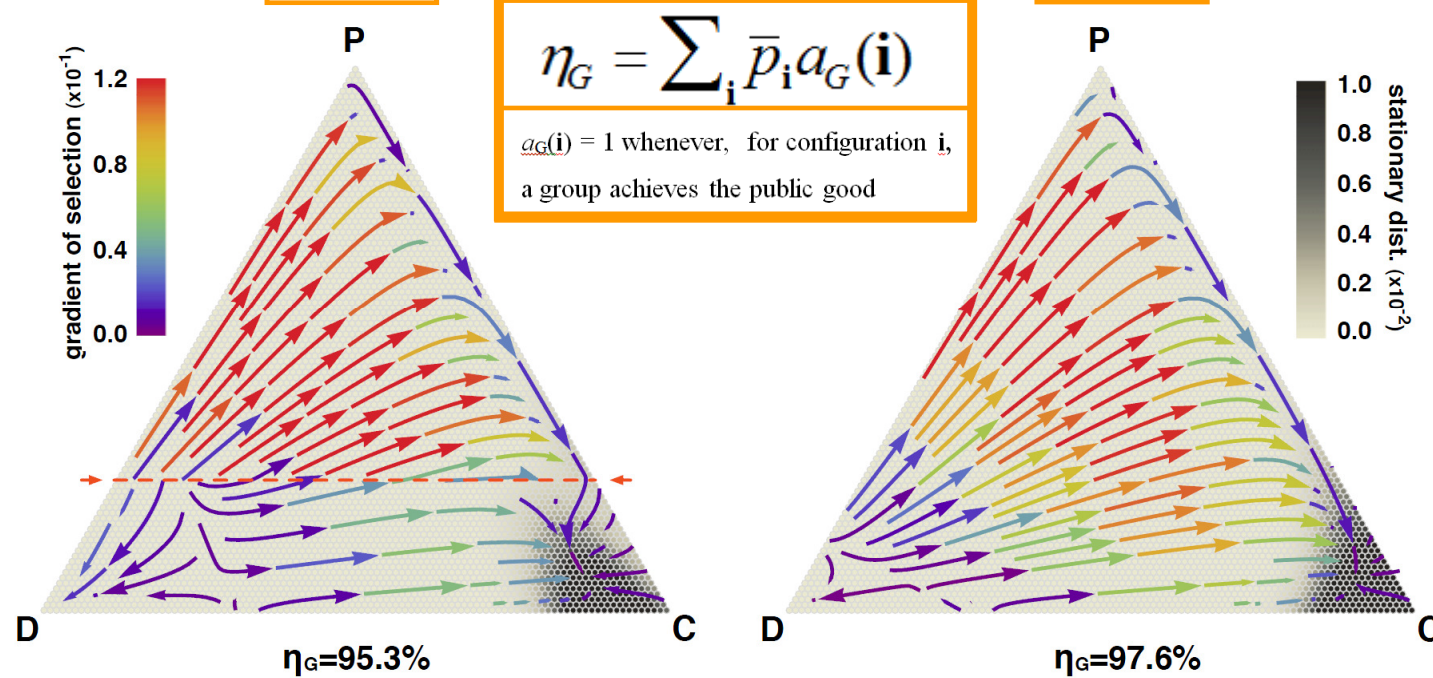


global versus local institutions

low risk



high risk



$$\eta_G = \sum_i \bar{p}_i a_G(\mathbf{i})$$

$a_G(\mathbf{i}) = 1$ whenever, for configuration \mathbf{i} ,
a group achieves the public good

conclusions

the results of our model suggest that coordinating for a common good is *best* achieved by

- ⊙ using a polycentric approach involving many small groups
- ⊙ making perception of risk (realistically) *high*
- ⊙ imposing stringent thresholds to meet goals
- ⊙ exploiting heterogeneous nature of the interaction network
- ⊙ setting up *local* institutions@group-level, which *play a crucial role* when perception of risk is small;

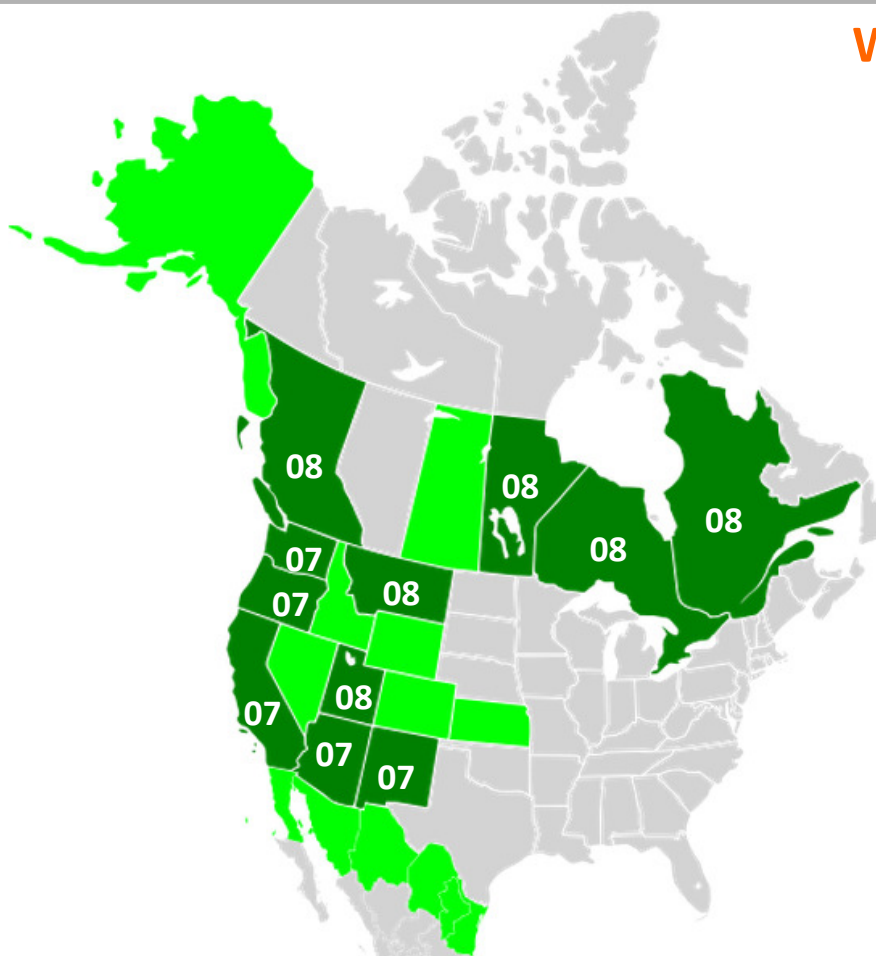
— *global* institutions (such as the **UN**) are essentially *ineffective* in promoting cooperation

— is this *utopia* ? any feasibility for *bottom-up* attempts ?

alternatives to minimize climate change impacts

WCI, ReGGle, MGA

WCI



(dangerous : increasing group size inhibits coordination)

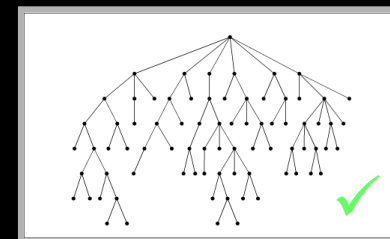
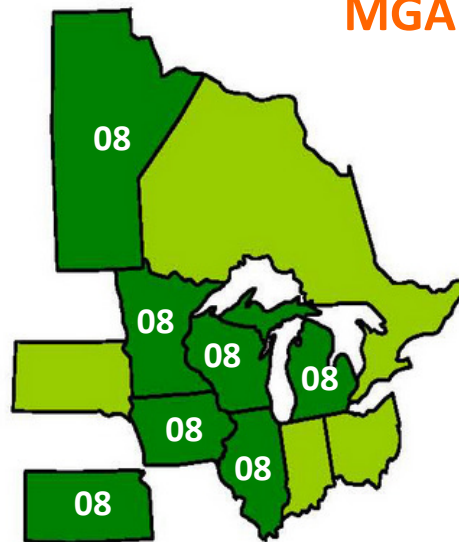
Legend for WCI:

- Partners (dark green)
- Observers (light green)

ReGGle

- 03 – 7 North-Eastern States
- 05 – MA & RI dropped out
- 07 – MA & RI rejoined
- 08 – MD & NH joined
- 11 – NJ dropped out

MGA



these state/province initiatives, regionally based, aim at aggregating into a wider and stronger structure, called **NORTH AMERICA 2050**



thank you!



<http://www.ciul.ul.pt/~ATP/>



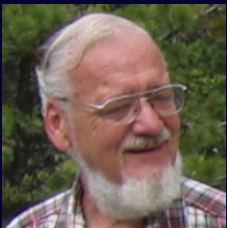
Francisco C. Santos
Sara Encarnação
Ana Ribeiro



Pedro Neves
Flávio Pinheiro
Vítor Vasconcelos

a melting pot of cooperation across disciplines

●●● atpgroup : collaborators

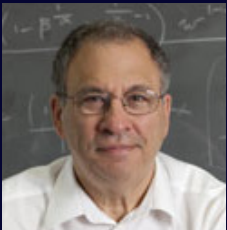


Brian Skyrms @Irvine & Stanford, USA

David Dingli @Mayo Clinic, USA

Robert Austin @ Princeton, USA

Lucio Luzzatto @ Inst. Tumori, Italy



Simon Levin @Princeton, USA

Tom Lenaerts @ULBrussels, Belgium

Juval Portugali @U-Telaviv, Israel

Martin Nowak @Harvard, USA