

Thin layers characterization by low frequency ultrasonic transmission

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ABSTRACT: A low frequency ultrasonic transmission test is proposed in which a P-wave is transmitted through the layered specimen and recorded. Standard characterization techniques like time-of-flight measurements require high frequency ultrasonics, which have a limited penetration in attenuating materials. On the contrary, the proposed technique is capable to measure using low frequency. A numerical simulation of the system is proposed using a linear finite element model of the ultrasonic propagation of the waves on the multilayered solid. The objective of the present study is to find the mechanical constants of a material composed of a sequence of isotropic layers by solving the model-based inverse problem, using an algorithm that minimizes the discrepancy between measured and simulated waveforms. Then, these mechanical constants can be correlated with the damage conditions. A sensitivity study to the uncertainties of the parameters is performed for establishing the feasibility of this technique. The technique experimentally proved to be highly robust to noise, but the technique admits further improvements at the modeling step.

1 INTRODUCTION

The conventional characterization methods like the pulse echo method, the pulse transference method and the resonance testing methods are avoided for characterization of thin layers, whose thickness are comparable or smaller than the wavelength (Zhang et al. 2001). High frequency ultrasonic waves can be used but they are also averted due to very high attenuation of the traveling wave and the methods continue to be quite expensive. Taking care of these difficulties, a low frequency ultrasonic transmission test is proposed in which a P-wave is transmitted through the layered sub-wavelength specimen and recorded (Cespedes et al. 1995, Nicholson et al. 2002, Wanner et al. 1998, Wear et al. 2000 & Zhao et al. 2004). Numerical simulation of the system is done by using a linear FEM model (Mackerle et al. 2004). The mechanical constants (thickness, elastic modulus, Poisson ratio, density and attenuation) of the different layers are identified by minimizing the discrepancy between the real and numerically predicted waveform which is done by regularly updating the FEM model throughout the iterative algorithm (Bonnet et al. 2005). A sensitivity study to the uncertainties of the parameters is performed for establishing the feasibility of this technique. To investigate the effect of noise, Gaussian noise is added as the percentage of the input signal (Rus et al. 2006); technique experimentally proved to be highly robust to this noise.

Similar work was done by Kinra et al. 1995, Lauwagie et al. 2004 & Zhang et al. 2001 to identify acoustical properties. However, the present technique is capable of identifying three parameters as thickness, attenuation and elastic modulus or density or poisson ratio at the same time assuming material to be isotropic. Anisotropic media is studied by Balasubramaniam et al. 1996, Balasubramaniam et al. 1998, Bruno et al. 2002, Reddy et al. 2005 & Rokhlin et al. 2002. Delaminations and cracks in multi-layered solid are studied by Bucur et al. 2005, Chona et al. 2003, Coulette et al. 1998, Panet et al. 2002 & Liu et al. 2002. Longitudinal and shear wave velocity (which is related to the elastic properties) are extracted by Bouhadjera et al. 2005; the data are correlated with the curing of concrete.

The influence of bonding layer thickness on the surface wave dispersion is clear and could be applied to the NDE of bonding properties. Tsai et al. 2001, Wu et al. 1999 & Zhang et al. 2005 have devised methods to calibrate the bonding layer thickness. The experimental setup used admits improvement for the thickness measurement of the bounding layer. As thickness of the bounding Vaseline layers used is assumed to be same at all interfaces for a particular specimen and hence is obtained just by measuring the full thickness of the specimen and subtracting the thickness of the material layers.

2 METHODOLOGY

2.1 Ultrasonics

Instead of the echogenic principle that is the base for most current techniques, a transmission setup (using a separate transmitter and receiver) is proposed where the complete waveform is recorded for its inversion in order to find out the elastic constants of the traversed media. The attenuation variation and velocity is dependent on the frequency and elastic constants of the layers that the wave travels through. These parameters are combined for the different layers and generate a waveform that needs to be processed by a complete inversion scheme. For best measuring the velocity and attenuation, a transmission setup with a low frequency (below the megahertz) ultrasonic pulse containing a wide range of frequencies and a high power of penetration is adopted.

2.2 Forward problem

To synthesize the RF recordings, a numerical simulation of the experiment is proposed using a linear FEM model of the ultrasonic propagation of the waves on the multilayered solid which is composed by the scheme in Figure 1. It is constructed using the research academic code FEAP by Taylor et al. 2003.

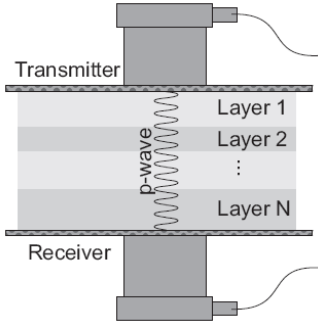


Figure 1. Scheme of the set-up for the experiments

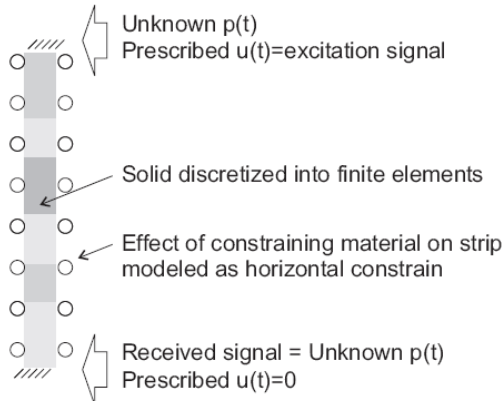


Figure 2. Scheme of the set-up for the FEM model

A 2D plain strain model is assumed, since the 3D effects are expected to be limited, at least for the purpose of this feasibility study. The transmitter is modeled by a prescribed displacement boundary condition by a normal displacement varying only with time which is uniform over the transducer contact area. The receiver is modeled by the integral of the normal pressure fields using a constant weight-

ing function over the transducer contact area. The recorded output waveform is compared with the waveform computed by FEM model.

2.3 Inverse problem

The characterization of inverse problem (search for the mechanical parameters) is carried out with an iterative strategy based on the minimization of some discrepancy between the measured and numerically predicted waveforms $\Phi^x(t)$ and $\Phi(t)$ respectively. The discrepancy is a vector of values or a function that can be discretized (represented by a vector).

$$\text{Discrepancy, } r = (\Phi^x - \Phi) \quad (1)$$

Since two vectors cannot be compared directly, a scalar number (called cost functional) is derived from them, in order to be able to minimize that discrepancy.

$$\text{Cost functional, } f = \frac{1}{2} \int_0^T |r(t)|^2 dt \quad (2)$$

The parameterization can be defined within the context of inverse problems as a description or characterization of the sought information (i.e. elastic constants characterization) with a reduced set of variables. The choice of parameters has crucial implications in the convergence, the sensitivity of the result and the decoupling of their dependence to the measurements. In this work parameters are adopted as the basic mechanical constants as well as number and thickness of the set of unknown layers. The inverse problem of mechanical constants evaluation can be therefore stated as a minimization problem of finding p such that,

$$\min_p f(p) \quad (3)$$

2.4 Description of Benchmark Problems

Different specimens have been used in this study with various combinations of the layers of materials, according to the number and thickness of layers, as well as their combination and sequence. All layers used in the specimens were square shaped (15cm×15cm) and of different thicknesses. Normal vaseline was used as the interfacial couplant. The values of the parameters were normalized using a logarithmic scale, in order to obtain a linear behaviour. For example, normalized value 1 will mean mechanical constant $\cdot e^1$. But for cost functional in inverse problem initial normalized value which is 1, corresponds to initial value of cost functional.

Table 1: The properties of different materials used

Material	Y.M. E(GPa)	Density $\rho(\text{kg/m}^3)$	R.Damping $\alpha (\text{s}^{-1})$	Poisson ratio ν
Couplant	000.001	0870	100000	0.4999
S. Steel	190.000	7850	150000	0.2307
Plastic	003.700	1190	300000	0.4084
Aluminium	085.000	2600	800000	0.3535

3 RESULTS

3.1 Forward problem

Comparison of Signals: Experimental & Simulated signals have been compared up to the time for which there is no reflection from the boundaries of specimens and a fairly good matching was obtained. The time at which the waveform starts, shows the time of arrival (time taken by the wave to reach the receiver). After time of arrival the signal obtained is superposition of direct waves and reflected waves from the interfaces.

Comparison of Energy Spectra: For all specimens, the highest peak corresponds to the central frequency of transducer which was 420 kHz. Small peaks in Energy spectrums correspond to natural frequencies & their higher order harmonics.

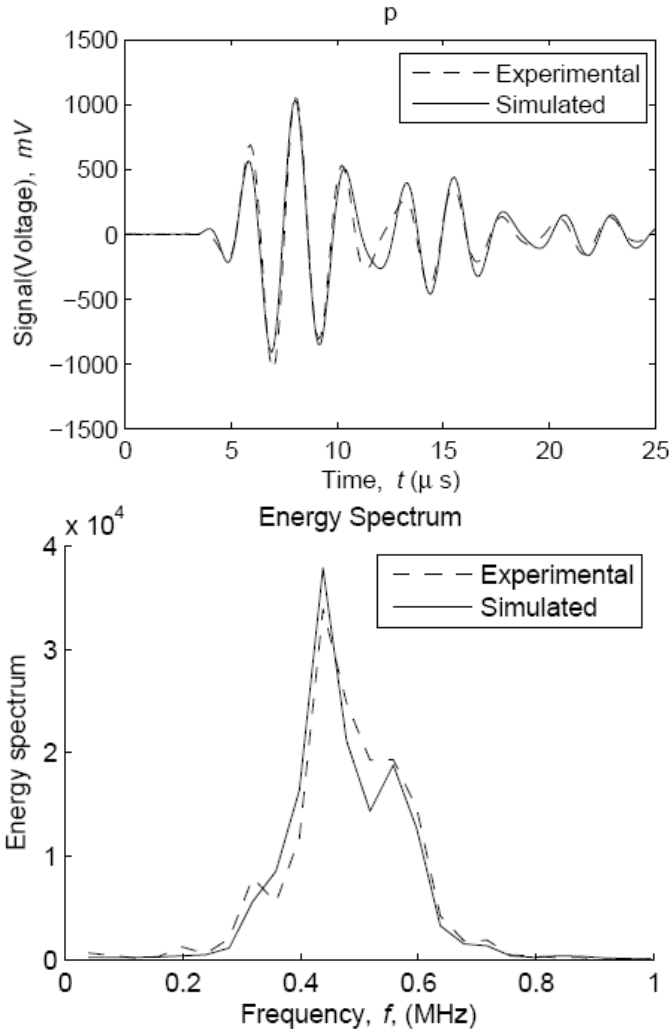


Figure 3. Signals for single plastic layer of thickness 9.95 mm

Table 2. Resonant frequencies for different layers

Material	Velocity of wave (m/s)	Thickness of layer (mm)	Natural frequency (kHz)
S. Steel (I)	5300	8.20	323
Plastic (P)	2600	9.95	130
Al (A)	7300	9.90	368

Even though the time of arrival is identical (which is the standard observation in ultrasonics), using this

approach, we can distinguish exchange of materials without exchange of time thickness (time of arrival), just because the relative amplitudes of different echoes will change. This means that materials with the same velocity (equal elasticity/density ratios) but different densities, will be distinguishable based on different acoustic impedance and hence transmission and reflection coefficients between layers. This is shown computationally in Figure 4, which compares the case of two configurations: S.Steel+Plastic (Original) versus Plastic+S.Steel (Interchange) modified to provide the same time of arrival of bangs.

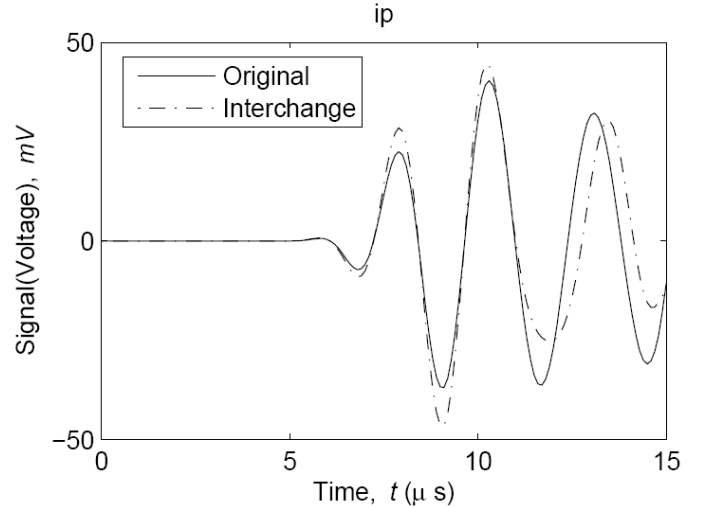


Figure 4. Comparison of signals for two specimens with the same time of arrival but different acoustic impedances.

3.2 Sensitivity study

For determining the feasibility of the above technique for finding out the parameters, sensitivity of Young modulus against Central frequency, Measurement noise, Rayleigh error, Thickness error, Elasticity error, Density error and Poisson error is simulated numerically. For studying the sensitivity, Cost functional f is plotted against Young modulus for different values of deviation in different parameters; hence this sensitivity study gives an idea about which parameters are predicted with more precision and which with less precision. For space restrictions, only the AIA sample results are reproduced in this paper.

Sensitivity to Central Frequency: The choice of central frequency of the signal should provide a balance between the penetration associated with low frequency, and the spatial resolution at high frequency. The proposed technique allows studying at a sub-wavelength resolution (lower frequency). The first plot shows the sensitivity of the algorithm for a range of frequencies. For this, the Cost functional f is plotted against the values of the input parameter Young modulus E , for an increasing frequency. The sensitivity is measured by observing the smoothness of the overall cost functional as well as the clarity of the minimum, as it should be found by an optimiza-

tion algorithm. As a conclusion, no major drawbacks are observed by varying the choice of frequency.

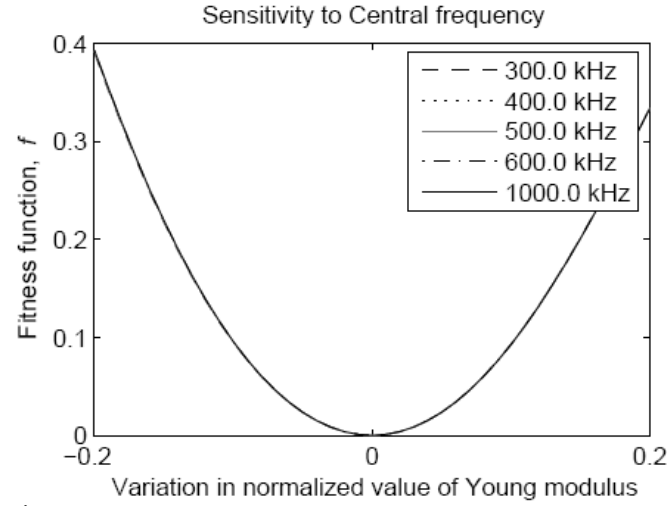


Figure 5.

Sensitivity to Measurement Noise: The sensitivity is measured by observing the capacity of the algorithm to show a minimum, and verifying its shifting from the true value. For this purpose, the cost functional f is plotted against the values of the input parameter Young modulus E , for an increasing level of noise. The Gaussian noise is simulated with zero mean and standard deviation as a percentage of the RMS of the measurement signal. The plot shows that the technique is highly robust against a high noise level.

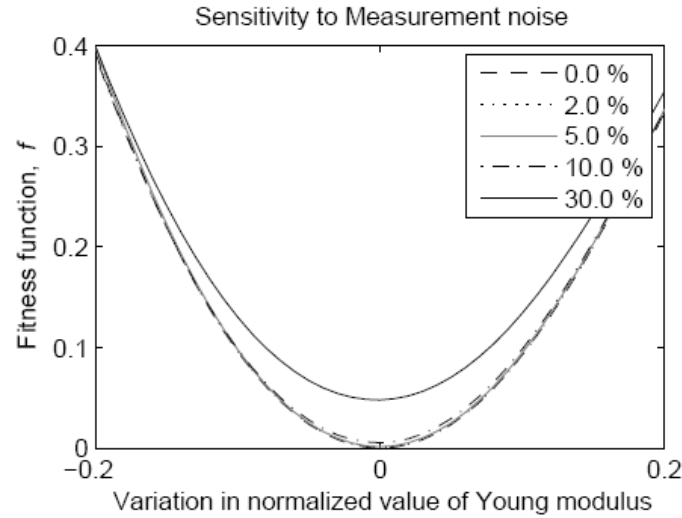


Figure 6.

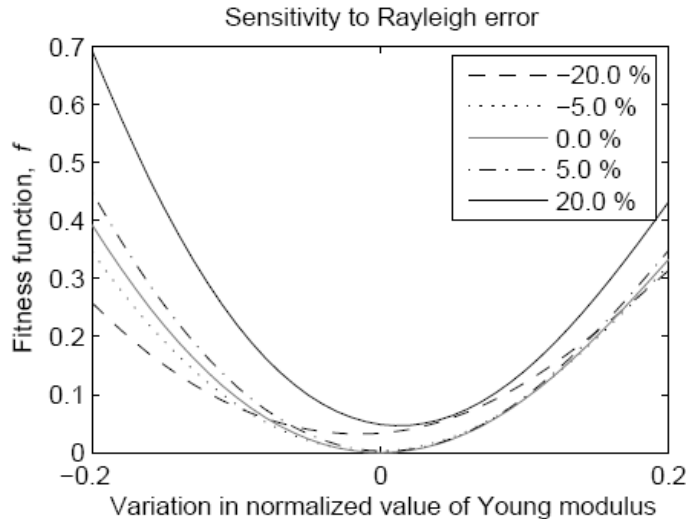


Figure 7.

Sensitivity to Rayleigh error: The plot below shows that the procedure appears to be robust to a wide range of uncertainty in Rayleigh damping value.

Sensitivity to Thickness, Elasticity, Density & Poisson error: The next three plots (density plot is omitted due to its relationship with elasticity) show that the procedure appears to be sensitive to these errors.

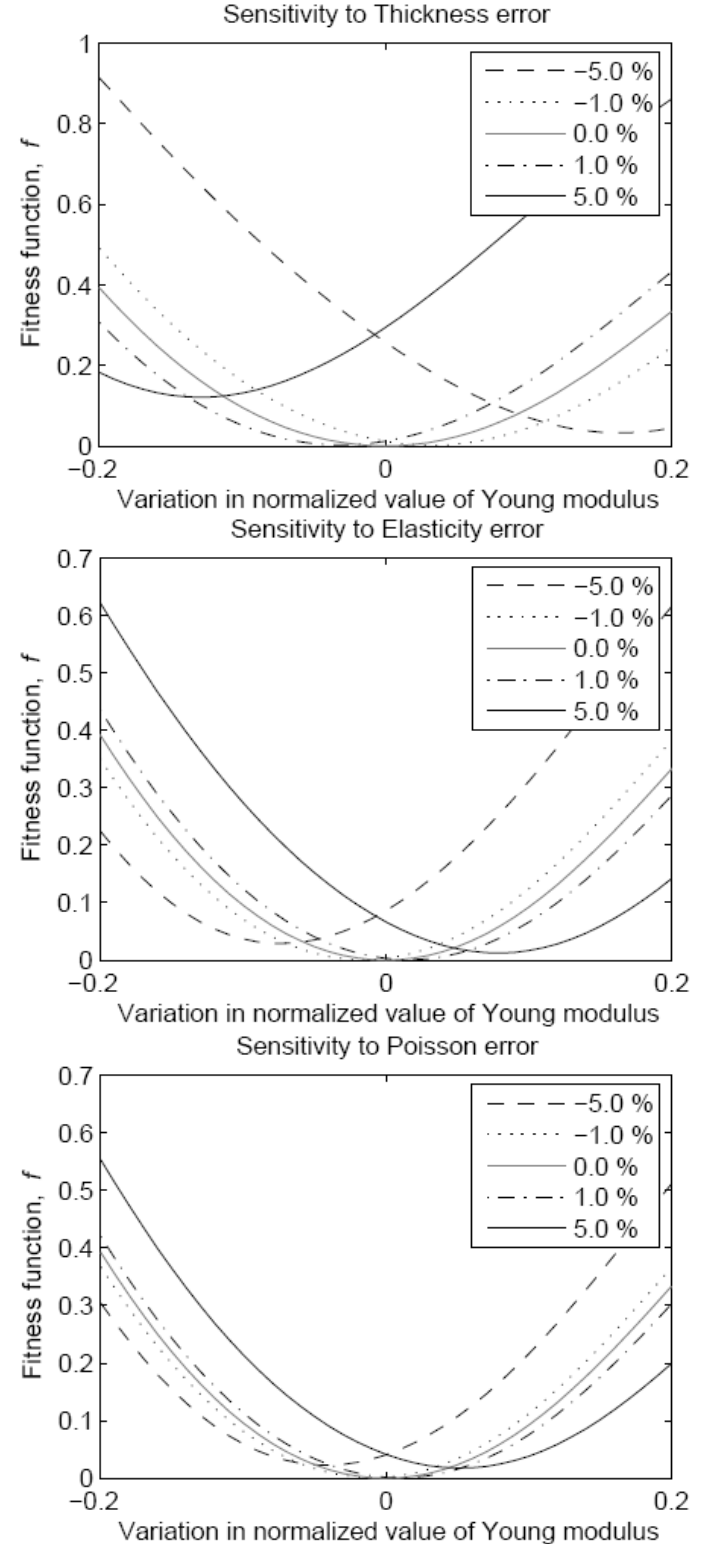


Figure 8.

Different combinations of materials have shown different sensitivities for various errors. For instance, the first plot of Figure 8 shows that for a 5% error in thickness convergence would be obtained for about -14% variation in Young modulus ($e^{-15}=0.86$). In a similar way rest of the figures can be observed for

the sensitivity of errors in Elasticity, Poisson ratio & Rayleigh damping.

3.3 Inverse problem

For solving inverse problem with only 1 parameter, curves for comparison between experimental & simulated measurements are plotted, where the cost functional is represented against normalized values of young modulus. These plots verify the final value of parameter computed by the optimization algorithm. In the figures showing iteration, the cost functional approaches zero, but due to limitations of the method it is unable to converge to exact zero. In every case, the optimization algorithm tends to match the signal from the initial guess towards the experimental signal.

Table 3. Inverse Problems elaborated in this paper

Specimen	Parameters	Initial guess
P	e	0.7
P	e + t + r	0.05
AIA	e(I) + e(A)	AAA

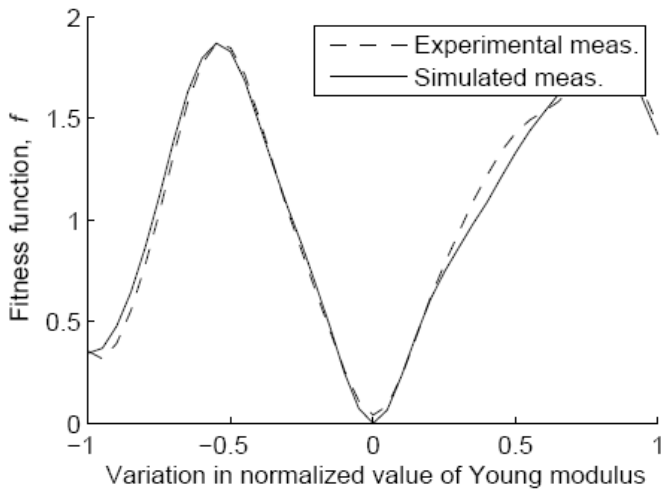


Figure 9. Comparison between Experimental & Simulated measurements of Fitness function by changing normalized value of Young modulus for Specimen-P.

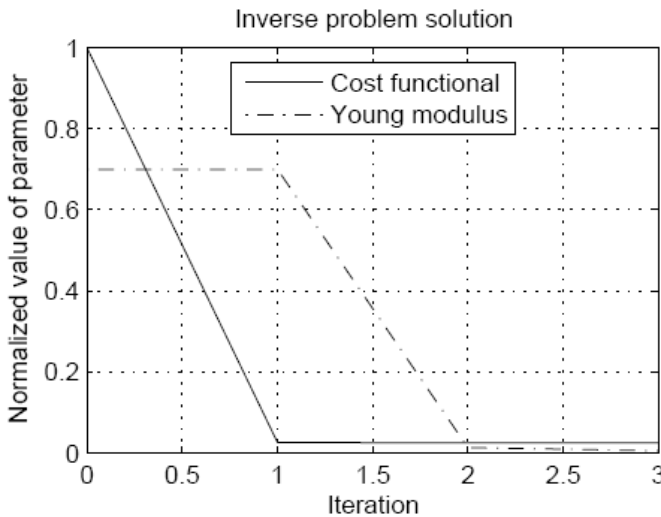


Figure 10. Inverse problem solution (with 1 parameter) for Specimen-P.

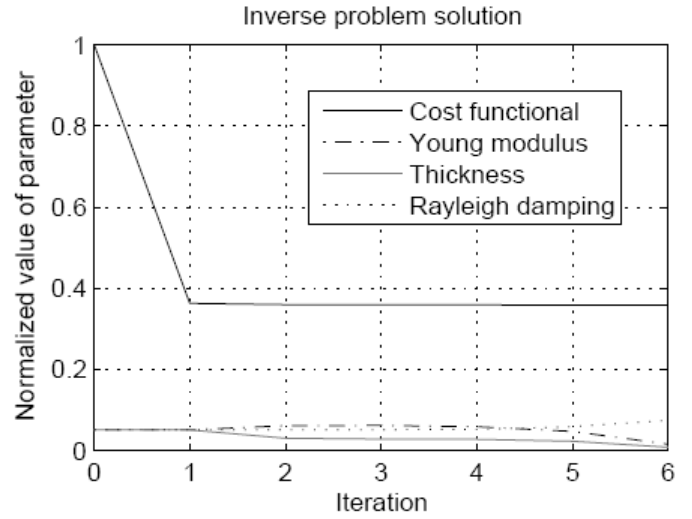


Figure 11. Inverse problem solution (with 3 parameters) for Specimen-P

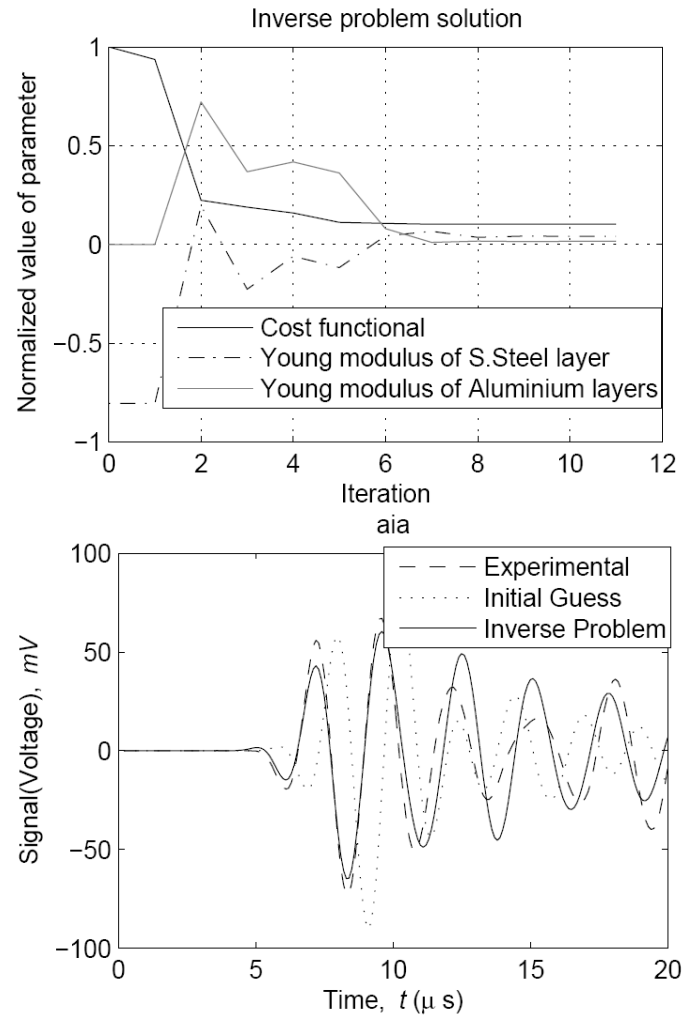


Figure 12. Inverse problem solution and signal (with 2 parameters) for Specimen-AIA. This figure shows how inverse problem try to approach from AAA to AIA. Note: $\ln(85/190) = -0.8044$; thicknesses 9.90+8.20+9.90mm, and couplant of thickness 0.08mm.

Nevertheless, the technique has shown some limitations, due to incoherence in signal phase after interface reflections matching of signals are poor after some time. Also, from the Figure 9 it can be concluded that due to local minima, the inverse problem cannot converge to absolute minima for normalized initial guess beyond the range $[-.5 .7]$. Figure 12 shows how the approach allows determining correct

values (to 5% error) of different layer properties by starting from a uniform material as the initial guess.

4 CONCLUSIONS

A technique is proposed to determine elastic properties, attenuation and thickness of different layers of layered materials, which involves solving the reconstruction inverse problem based on a FEM model of the ultrasound propagation and using as input data the experimental waveforms obtained from a transmission setup at low frequency (in comparison with the natural frequencies of the layers). This technique is proved experimentally consistent, but is still limited in that results are sensitive to uncertainties of interfacial couplant, transducer response & transducer coupling with specimen (boundary conditions: free or fixed), as well as a priori information that provides the initial guess.

An extension of this work may be applicable to detect damaged layers or delaminations in composites by stiffness reduction, or for medical diagnosis of layered tissue, whose stiffness variations (nodules) can be correlated with their pathological conditions.

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