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Energy balance closure at FLUXNET sites

Kell Wilson ^a, Allen Goldstein ^b, Eva Falge ^c, Marc Aubinet ^d, Dennis Baldocchi ^{b,*}, Paul Berbigier ^e, Christian Bernhofer ^f, Reinhart Ceulemans ^g, Han Dolman ^h, Chris Field ⁱ, Achim Grelle ^j, Andreas Ibrom ^k, B.E. Law ^l, Andy Kowalski ^g, Tilden Meyers ^a, John Moncrieff ^m, Russ Monson ⁿ, Walter Oechel ^o, John Tenhunen ^c, Riccardo Valentini ^p, Shashi Verma ^q

^a Atmospheric Turbulence and Diffusion Division, NOAA, P.O. Box 2456, Oak Ridge, TN 37831, USA

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b ESPM, University of California at Berkeley, Berkeley, CA 94720, USA
c Pflanzenökologie, University Bayreuth, 95440 Bayreuth, Germany
d Unité de Physique, Faculté des Sciences Agronomiques de Gembloux, B-50 30 Gembloux, Belgium
c Unité de Bioclimatologie, INRA Bourdeaux, Gazinet, France
f Insitute für Hydrologie und Meteorologie, 01737 Tharandt, Germany
g Free University, Amsterdam, The Netherlands
h INRA Ecophysiology, Pierroton, France
i Department of Plant Biology, Carnegie Institution of Washington, Stanford, CA 94305, USA
J Department of Ecology and Environmental Research, Swedish University of Agricultural Sciences, S-750 07 Uppsala, Sweden
k Institut für Bioklimatologie, Georg-August University, Göttinen, Germany
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Abstract

A comprehensive evaluation of energy balance closure is performed across 22 sites and 50 site-years in FLUXNET, a network of eddy covariance sites measuring long-term carbon and energy fluxes in contrasting ecosystems and climates. Energy balance closure was evaluated by statistical regression of turbulent energy fluxes (sensible and latent heat (LE)) against available energy (net radiation, less the energy stored) and by solving for the energy balance ratio, the ratio of turbulent energy fluxes to available energy. These methods indicate a general lack of closure at most sites, with a mean imbalance in the order of 20%. The imbalance was prevalent in all measured vegetation types and in climates ranging from Mediterranean to temperate and arctic. There were no clear differences between sites using open and closed path infrared gas analyzers. At a majority of sites closure improved with turbulent intensity (friction velocity), but lack of total closure was still prevalent under most conditions. The imbalance was greatest during nocturnal periods. The results suggest that estimates of the scalar turbulent fluxes of sensible and LE are underestimated and/or that available energy is overestimated. The implications on interpreting long-term CO₂ fluxes at FLUXNET sites depends on whether the imbalance results primarily from general errors associated

College of Forestry, Oregon State University, Corvallis, OR 97331, USA
 Department of Ecology and Environmental Research, University of Edinburgh, Edinburgh, UK
 DEPOB, University of Colorado, Boulder, CO 80309, USA

^o Global Change Research Group, San Diego State University, San Diego, CA 92182, USA

P Department of Forest Science and Resources, University of Tuscia, 1-01100 Viterbo, Italy

^q School of Natural Resource Sciences, University of Nebraska, Lincoln, NE 68583, USA

^{*} Corresponding author. Tel.: +1-510-642-2874; fax: +1-510-643-5098. E-mail address: baldocchi@nature.berkeley.edu (D. Baldocchi).

with the eddy covariance technique or from errors in calculating the available energy terms. Although it was not entirely possible to critically evaluate all the possible sources of the imbalance, circumstantial evidence suggested a link between the imbalance and CO_2 fluxes. For a given value of photosynthetically active radiation, the magnitude of CO_2 uptake was less when the energy imbalance was greater. Similarly, respiration (estimated by nocturnal CO_2 release to the atmosphere) was significantly less when the energy imbalance was greater. Published by Elsevier Science B.V.

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1. Introduction

The global proliferation of long-term eddy covariance sites measuring carbon and energy fluxes (FLUXNET) provides a unique contribution to the study of the environmental, biological and climatological controls of net surface exchange between vegetation and the atmosphere (Baldocchi et al., 2001). Independent methods of evaluating the reliability of the eddy covariance measurements at FLUXNET sites are highly desirable. One method of independently evaluating scalar flux estimates from eddy covariance is energy balance closure. Energy balance closure, a formulation of the first law of thermodynamics, requires that the sum of the estimated latent (LE) and sensible (*H*) heat flux be equivalent to all other energy sinks and sources

$$LE + H = R_n - G - S - Q \tag{1}$$

where R_n is the net radiation, G the heat flux into the soil substrate, S the rate of change of heat storage (air and biomass) between the soil surface and the level of the eddy covariance instrumentation, and Q the sum of all additional energy sources and sinks. Typically, Q is neglected as a small term, and an imbalance between the remaining independently measured terms on the left- and right-hand sides of Eq. (1) may indicate inaccurate estimates of scalar fluxes.

Energy balance closure is directly relevant to the evaluation of latent and sensible heat fluxes and not to other scalar fluxes (e.g. CO₂ fluxes, the primary constituent for FLUXNET). However, at least four considerations make an analysis of energy balance closure at FLUXNET sites relevant and functional. First, although the source—sink distributions for water, heat and CO₂ are different from each other in an ecosystem, the atmospheric transport mechanisms within and above the canopy, which are measured by

eddy covariance, are similar for all scalars. Second, the computation of all scalar fluxes using the eddy covariance technique is founded on similar theoretical assumptions in the conservation equations and their Reynolds decomposition (Paw U et al., 2000). Thirdly, at FLUXNET sites all the terms in Eq. (1) are typically measured and recorded continuously at a high temporal resolution, providing a data set for independently evaluating eddy covariance fluxes across multiple time scales. Finally, an independent evaluation of energy balance closure across FLUXNET sites is useful for its own purposes, especially in view of the close biophysical coupling between carbon, energy and water fluxes (Collatz et al., 1991; Baldocchi and Meyers, 1998).

Historically, energy balance closure has been accepted as an important test of eddy covariance data (Anderson et al., 1984; Verma et al., 1986; Mahrt, 1998), and a number of individual sites within the FLUXNET network report energy balance closure as a standard procedure (e.g. Hollinger et al., 1999; Anthoni et al., 1999; Aubinet et al., 2000; Goldstein et al., 2000; Wilson and Baldocchi, 2000; Schmid et al., 2000). From these studies and many others, a general concern has developed within the micrometeorological community because surface energy fluxes (LE + H) are frequently (but not always) underestimated by about 10-30% relative to estimates of available energy $(R_n - G - S)$. The imbalance is often present, though often to a lesser extent, even over flat, homogeneous surfaces and short vegetation (Stannard et al., 1994; Mahrt, 1998; Twine et al., 2000), which are presumably ideal conditions for the eddy covariance method.

An energy imbalance has implications on how energy flux measurements should be interpreted and how these estimates should be compared with model simulations (Liu et al., 1999; Twine et al., 2000; Culf et al., 2002). Within the FLUXNET community, the

consequence of a possible widespread energy imbalance on the interpretation of CO₂ fluxes is somewhat less certain and is dependent on the mechanisms creating the imbalance. General hypotheses have been suggested to account for the lack of energy balance closure, including: (1) sampling errors associated with different measurement source areas for the terms in Eq. (1), (2) a systematic bias in instrumentation, (3) neglected energy sinks, (4) the loss of low and/or high frequency contributions to the turbulent flux and (5) neglected advection of scalars. If the energy imbalance results from different measurement source areas for the terms in Eq. (1), or bias errors in net radiation, or neglected energy sinks and sources, there may be no reason to suspect that the measured CO2 fluxes are systematically inaccurate. However, if the mechanisms creating the imbalance result from inappropriate assumptions made from the scalar conservation equation, such as neglecting mean advection (Paw U et al., 2000), or result from low or high frequency loss of flux, the estimated CO2 flux may contain similar errors in relation to the actual terrestrial exchange. An overall evaluation of site characteristics and meteorological conditions associated with the energy imbalance may provide circumstantial evidence for its cause, and also suggest whether similar errors are likely in the CO₂ flux estimates.

Because of the large geographic and biological variability at the contributing sites, FLUXNET offers a unique data set to compare energy balance closure for different vegetation types, terrain features and climates. Previous studies have focused on energy balance closure at multiple sites (Stannard et al., 1994; Barr et al., 1994; Aubinet et al., 2000; Twine et al., 2000), but FLUXNET encompasses a larger quantity of sites and with extensive variability in site characteristics. Although diverse instrumentation and processing methods in FLUXNET increase the possible sources affecting energy balance closure, instrumentation differences also present an opportunity to examine the effect of available techniques, especially potential differences between open and closed path infrared gas analyzers (IRGAs). Because FLUXNET sites typically measure continuously over annual cycles, an evaluation of closure over different seasons is possible, which has not generally been reported in other synthesis studies of energy balance closure (Stannard et al., 1994; Mahrt, 1998; Twine et al., 2000).

The goals of this study are: (1) to evaluate energy balance closure at all FLUXNET sites, and (2) to evaluate the potential source of differences in the imbalance within and between sites. Based on these considerations, (3) we will also discuss the relationship between energy balance closure and the consequences for interpreting CO₂ fluxes.

2. Materials and methods

Methodology and review papers for many of the FLUXNET eddy covariance sites are published in Aubinet et al. (2000) and Baldocchi et al. (2001). Eddy covariance and the supporting environmental and meteorological data were contributed by individual investigators to the FLUXNET database at Oak Ridge National Laboratory's Data Archive Center. The data set contains annual files of half-hourly flux and meteorological data at eddy covariance stations across Europe and North America (Table 1) and includes a range of vegetation types and climates. A 'site-year' was accepted for analysis if more than 10% of the half-hours (approximately 1750 half-hours) in a year contained non-missing values for each of the following: net radiation (R_n) , ground heat flux (G), canopy heat storage (S), latent heat (LE) flux and sensible heat flux (H). Because the importance of canopy heat storage is expected to be small in short canopies with minimal biomass, half-hourly data were still accepted for analysis when canopy heat storage was missing, provided that the vegetation height was less than 8 m. However, the canopy heat storage requirement was maintained for tall, forested sites because of its potential importance (McCaughey, 1985; Moore and Fisch, 1986), which eliminated several sites in this analysis. Twenty-two FLUXNET sites and 50 site-years (out of 90 available) met these requirements and were evaluated for energy balance closure. The mean energy balance data coverage (the percent of all half-hours with all energy balance terms) of the accepted site-years was 48%, ranging from 11 to 90%. Either because of protocol or instrument malfunctions, a number of the 'site-years' do not include data uniformly distributed throughout the year. Table 1 also contains a qualitatively brief description of terrain for each site that was available from the FLUXNET data archive.

Table 1 Summary of the FLUXNET sites in this analysis^a

Location	Country	Vegetation	Height	Max LAI	Terrain	IRGA	Yrs
Atqasuk, AK	United States	Tundra	0.5	1.5	Flat	0	1
Blodgett, CA	United States	Conifer	4	7.8	Flat	C	4
Bondville, IL	United States	Agriculture	2	6	Flat	O	4
Barrow, AK	United States	Tundra	0.3	1.5	Flat	O	2
Happy Valley, AK	United States	Tundra	0.3	1.5	Gentle slope	O	2
Little Washita, OK	United States	Rangeland	1	2.5	Flat	O	2
Metolius, OR	United States	Conifer	20	1.5	Hilly	O	2
Niwot Ridge, CO	United States	Conifer	20	4.2	Hilly	C	1
Ponca, OK	United States	Agriculture	1	5.3	Flat	C/H	1
Shidler, OK	United States	Grassland	0.7	2.8	Flat	C/H	2
Sky Oaks, CA	United States	Chaparral	2	3.0	Hilly	O	2
Sky Oaks, CA	United States	Chaparral	0.5	1.1	Hilly	O	2
Walker Branch, TN	United States	Deciduous forest	26	5.5	Hilly	O	4
Aberfeldy	United Kingdom	Conifer	6	8	Gentle slope	C	2
Bordeaux	France	Conifer	18	5.5	Flat	C	3
Brasschaat	Belgium	Conifer	22	3	Flat	C	3
Castelporziano	Italy	Evergreen	13	3.5	Flat	C	2
Loobos	Netherlands	Conifer	15	3	Flat	C	2
Norunda	Sweden	Mixed conifer	25	5	Flat	C	3
Tharandt	Germany	Conifer	28	6	Gentle slope	C	4
Vielsalm	Belgium	Mixed forest	32	4.5	3% slope	C	3
Bayreuth	Germany	Conifer	19	5	Hilly	C	2

^a 'Height', 'Max LAI' and 'Yrs' are the vegetation height (m), maximum leaf area index of the vegetation and the number of years with data. 'O' denotes an open path system used for measuring both water and CO₂ fluxes, a 'C' denotes a closed path system used for measuring both water and CO₂ fluxes, and 'C/H' denotes that a closed path IRGA used for measuring CO₂ fluxes and a krypton hygrometer used for measuring water vapor.

Energy balance closure was evaluated for each site-year using four different methods. The first method, and the principal method discussed in this study, was to derive linear regression coefficients (slope and intercept) from the ordinary least squares (OLSs) relationship between the half-hourly estimates of the dependent flux variables (LE + H) against the independently derived available energy $(R_n - G - S)$; see Eq. (1)). Ideal closure is represented by an intercept of zero and slope of 1. The OLS regression is technically valid only if there are no random errors in the independent variable (Meek and Prueger, 1998), which would incorrectly imply that the measurements of R_n , G and S contain no random errors. Two alternative methods were used to address the effects of this random error on the linear regression statistics (Meek and Prueger, 1998). The reduced major axis (RMA) method switches the independent and dependent variables and evaluates the slope as the geometric mean of the OLS and switched regressions. A second alternative method used to account for random errors in available energy was the method of moments (MMs), which requires that the random error in $R_n - G - S$ be specified. Because the random error is associated with instrumentation, sampling methods and natural variability, this error is unknown and variable between sites. Therefore, several hypothetical error estimates (10, 20, 40 and 50%) were used in the MM approach to evaluate the possible effect of random error on the linear regression slope. A fourth method to evaluate closure was to cumulatively sum $R_n - G - S$ and LE + H over specified time periods, such as over an entire year or during nocturnal periods, and calculate the energy balance ratio (EBR) (Mahrt, 1998; Gu et al., 1999)

$$EBR = \frac{\sum (LE + H)}{\sum (R_n - G - S)}$$
 (2)

The advantage of EBR is that it gives an overall evaluation of energy balance closure at longer time scales by averaging over random errors in the half-hour measurements. A disadvantage of EBR is the potential to overlook biases in the half-hourly data, such as the tendency to overestimate positive fluxes during the day and underestimate negative fluxes at night (Blanken et al., 1998; Mahrt, 1998).

3. Results

3.1. Overall energy balance closure

Regression coefficients of LE+H against $R_{\rm n}-G-S$, using OLSs on all the half-hour data for each of the 50 site-years, are shown in Table 2. The slope was less than 1 for all site-years, ranging from 0.53 to 0.99, with a mean of 0.79 ± 0.01 . The intercept ranged from -32.9 to 36.9 W m⁻², with a mean of 3.7 ± 2.0 W m⁻². There were more positive (31) than negative intercepts (19). The mean coefficient of determination (r^2) was 0.86, ranging from 0.64 to 0.96.

Using the RMA approach, which accounted for random errors in available energy, increased the mean slope to 0.83 ± 0.01 . The increase in slope ranged from 2 to 10% for 43 of the 50 site-years (not shown). The remaining seven site-years increased by more than 10%, with one site increasing by 25%. The sites with the largest increase in slope using the RMA approach had the lowest correlation (r^2 values less than 0.80). The mean intercept using the RMA method was slightly less than using the OLS method ($-1.4 \pm 1.8 \,\mathrm{W\,m^{-2}}$).

A second method to account for random errors in the independent variable was the MMs approach. The MM approach requires a quantitative estimate of the random error in the measurement of the independent variable $(R_n - G - S)$. Setting hypothetical estimates of the random error in $R_n - G - S$ of 10, 20, 40 and 50% resulted in mean slopes of 0.78, 0.82, 0.99 and 1.17, respectively. Random errors of greater than 20% in available energy would be required for substantial improvements in energy balance closure. The mean intercept of the site-years decreased as the random error increased: $2.7 \, \mathrm{W \, m^{-2}}$ (for a 10% random error), $-0.4 \, \mathrm{W \, m^{-2}}$ (20%), $-16.3 \, \mathrm{W \, m^{-2}}$ (40%) and $-33.5 \, \mathrm{W \, m^{-2}}$ (50%).

The bias in the energy imbalance is still evident at most sites when it is evaluated as the annual ratio of total annual turbulent heat flux to available energy (i.e. annual value of EBR, Table 2). The mean EBR for

Table 2 Ordinary linear regression (OLR) coefficients for energy balance closure for all site-years^a

n	Intercept	Slope	r^2	EBR
5129	3.5	0.55	0.80	0.56
3771	7.1	0.58	0.87	0.70
3324	16.8	0.60	0.64	0.77
3495	20.9	0.62	0.74	b
6197	29.7	0.64	0.74	0.82
6144	-10.1	0.65	0.83	1.00
8738	-0.8	0.68	0.85	0.68
14418	-0.7	0.69	0.85	1.20
11459	2.5	0.70	0.84	0.72
10227	6.0	0.70	0.83	0.74
9267	-12.3	0.71	0.87	1.03
7952	-18.3	0.72	0.86	0.59
9621	-6.9	0.72	0.86	0.66
3918	12.7	0.73	0.92	0.84
10712	-32.9	0.73	0.80	0.39
11267	7.7	0.74	0.88	0.82
12727	36.9	0.74	0.76	1.00
13834	11.3	0.75	0.84	0.86
14468	9.6	0.75	0.85	0.88
11561	8.4	0.75	0.86	0.83
9649	31.1	0.75	0.89	1.16
12016	3.1	0.75	0.88	0.78
9005	16.6	0.76	0.92	0.88
11789	-6.0	0.77	0.83	0.76
11058	-16.2	0.78	0.81	0.53
4032	2.6	0.78	0.87	0.81
4039	-5.4	0.79	0.85	0.62
4181	4.5	0.80	0.88	0.87
6848	-8.7	0.82	0.83	0.69
3846	16.3	0.83	0.92	0.93
4370	5.0	0.83	0.89	0.79
4896	7.4	0.84	0.96	0.93
14760	6.4	0.85	0.92	0.97
4150	4.1	0.85	0.85	0.92
12751	-1.2	0.85	0.90	0.84
5193	-12.5	0.85	0.95	0.73
15638	-5.3	0.85	0.87	0.69
2594	-2.1	0.85	0.94	0.83
13891	2.6	0.86	0.90	0.89
14198	-7.7	0.86	0.91	1.00
6357	28.6	0.87	0.86	1.09
3850	3.6	0.89	0.90	0.93
3864	6.6	0.89	0.87	0.34
14324	8.9	0.90	0.91	1.69
7993	-18.7	0.90	0.89	0.79
12064	31.5	0.91	0.91	1.17
14545	-15.2	0.92	0.92	0.77
13655	7.1	0.95	0.91	0.89
4670	-23.8	0.97	0.90	0.71
	32.6	0.99	0.79	b

^a 'EBR' refers to the annual ratio of $(H + LE)/(R_n - G - S)$; n is the number of half-hours.

^b A spurious EBR ratio because the summed available energy was close to zero.

all the site-years was 0.84, ranging from 0.34 to 1.69. The ratio of total turbulent heat flux to total available energy across all 50 site-years was similar, 0.82.

3.2. Role of canopy and ground heat storage

Twenty-six site-years with tall vegetation (height > 8 m) reported an estimate of canopy heat storage (S). Including S in the regressions for these sites increased the slope of the OLS regression by an average of 7%, which is why forested sites were required to report S in this study. The mean intercept decreased from 2.1 to $-0.8 \,\mathrm{W\,m^{-2}}$. Soil heat flux (G) increased the average OLS slope for grasslands, agricultural and chaparral sites by about 20%. Soil heat flux had much less impact at the forested sites, where the average OLS slope increased by only 3%.

3.3. Vegetation type, vegetation height and IRGA type

Fig. 1 shows the slope of the OLS regression against vegetation height, differentiating between sites using open and closed path IRGAs. There were no obvious differences in the slope for sites using the open and closed path designs. There was also no obvious effect of vegetation height on the OLS slope.

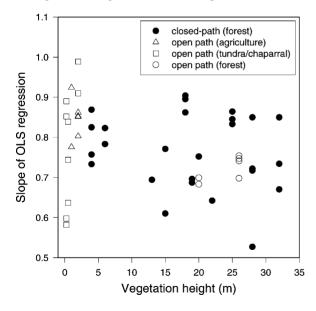


Fig. 1. The slope of the OLS regression against vegetation height for sites using closed (closed symbols) and open (open symbols) path IRGAs. Symbol shapes represent different vegetation types.

3.4. Diurnal variation in closure

The OLS regression statistics during periods of positive net radiation (not shown) were similar to the statistics using all the data that are shown in Table 2. The mean slope was 0.80 ± 0.02 , ranging from 0.56 to 0.97. The mean intercept was $-0.3\pm3.0\,\mathrm{W\,m^{-2}}$ and r^2 was 0.81. The 'site-year' mean annual EBR during 'daytime' periods was 0.80, and EBR was equal to or greater than 1 at only two site-years. The ratio of total daytime turbulent heat flux to total daytime available energy for all 50 site-years was similar, 0.79.

The mean OLS slope during nighttime periods (net radiation less than zero) was only 0.35 ± 0.03 , ranging from -0.04 to 0.69. The mean intercept was $-5.5 \pm 1.4 \,\mathrm{W}\,\mathrm{m}^{-2}$ and the correlation was typically weak (mean $r^2 = 0.11$). In some cases, the 'site-year' annual nocturnal EBR was negative or was much less or much greater than 1. The ratio of total turbulent flux to the total available energy summed over all the sites was 0.54 during the night, which is less than during the day. The magnitude of the imbalance at night was strongly dependent on turbulent mixing, as shown in the following section.

Data from all the site-years were combined to compute the diurnal course of the EBR. For each of the 24 h the half-hourly LE + H and $R_n - G - S$ were summed over entire site-years using the entire data set. The ratio between these two sums (Eq. (1)) was the hourly EBR. Fig. 2 shows the diurnal course of the EBR, along with the mean magnitudes of LE + Hand $R_n - G - S$. During morning and evening transition periods, when the mean value of $R_n - G - S$ was close to zero, the EBR is not especially meaningful. Between these two transition periods there was a general increase in the EBR from the morning to afternoon. This pattern of a greater EBR in the afternoon relative to the morning was observed in both the warm and cold seasons and was typical for most of the individual site-years (not shown).

3.5. Effect of turbulent mixing

The effect of turbulent mixing was evaluated between and within sites by analyzing closure with respect to friction velocity. The slope of the OLS regression was not a function of the mean annual friction velocity across all the site-years (not shown).

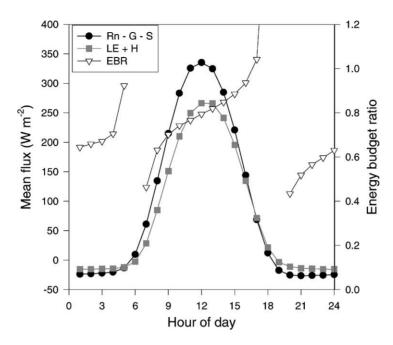


Fig. 2. The mean diurnal energy budget ratio (EBR) using all the site-years in this study. Also shown are the mean diurnal values of $R_n - G - S$ and LE + H.

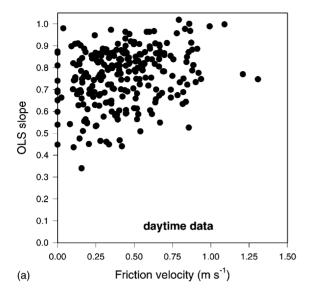
The effect of friction velocity was also evaluated within each of the site-years. Friction velocity typically changes with stability and time of day. Therefore, the change in energy balance closure between night and day (shown above) could also be the direct result of changes in friction velocity. Nevertheless, a simple method was used to partially isolate the effects of friction velocity from the effects of time of day (and presumably to some extent, stability). Data for each of the site-years were separated into 48 groups, representing the 48 half-hours in a day. The data in each of the 48 groups were segregated into two large groups, each containing half the data. One group contained data when the friction velocity was above the annual median for that half-hour, and the second group contained data when the friction velocity was below the annual median for that half-hour. OLS regressions were performed for both groups of half-hour data for each site-year.

The slope was typically greater when the friction velocity was above the half-hourly medians, but the intercept was slightly less. The mean slope for all site-years was 0.73 when the friction velocity was below the median, with an intercept of 7.1 and $r^2 =$

0.86. Above the median friction velocity, the slope was 0.81, with intercept of 1.0 and $r^2 = 0.87$. The slope was significantly (P < 0.05) greater for data above the mean friction velocity in 41 of the 50 site-years. A similar result was obtained when data were separated into five friction velocity categories instead of two, but the largest differences were between the lowest friction velocity groups. The OLS slope increased from 0.69 for winds in the lowest 20% to 0.73, 0.77, 0.80 and 0.80 in the four remaining groups.

The effect of friction velocity on energy balance closure was analyzed separately for daytime and nighttime data using the same methods that were just described using all the data. For both daytime and nighttime, data from each site-year were segregated by friction velocity into five percentile groups (five sets, each with 20% of the site-year data). There was a very weak trend ($r^2 = 0.08$) for the OLS slope to increase with friction velocity during daytime hours (Fig. 3a). A slightly more obvious trend was evident when EBR was plotted against friction velocity ($r^2 = 0.14$) (Fig. 3b).

The OLS slope was smaller and was more dependent ($r^2 = 0.43$) on friction velocity during nocturnal



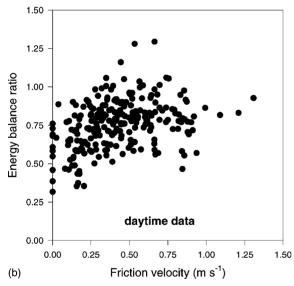


Fig. 3. The (a) OLS slope and (b) EBR against friction velocity during daytime periods. Each site-year is represented by five points on these plots, representing data sorted by friction velocity into five 20 percentile groups of half-hour data. The points showing a friction velocity of zero are the result of an inadequate number of significant figures in the FLUXNET data archive.

periods than during the daytime (Fig. 4). When the mean friction velocity was below $0.25 \,\mathrm{m\,s^{-1}}$, the slope of the OLS regression was less than 0.50 for all site-years. When the mean friction velocity exceeded $0.50 \,\mathrm{m\,s^{-1}}$ the slope was greater, but was still typically less than 1.0.

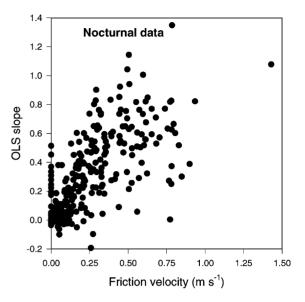


Fig. 4. The OLS slope against friction velocity (u_*) during nocturnal periods (net radiation less than zero). Each site-year is represented by five points, representing data sorted by friction velocity into five 20 percentile groups of half-hour data.

Fig. 5 shows the effect of friction velocity on the OLS slope during nocturnal periods in more detail at specific FLUXNET sites. The sites shown in Fig. 5 represent a range of vegetation types, IRGA types and terrain. The nocturnal OLS slope usually increased with friction velocity within (Fig. 4) and across (Fig. 5) sites, but the mean r^2 was only 0.15, ranging from 0.00 to 0.51. In some cases the slopes were not statistically different from zero, or the intercept changed perceptibly with friction velocity. To help address this issue, the effect of friction velocity on nighttime closure was also analyzed using the EBR method (Fig. 6). The general relationship between EBR and friction velocity was similar to that using the OLS slope (increasing with friction velocity), except EBR often exceeded 1 at high friction velocities.

3.6. Effects of seasonality and the Bowen ratio

Nineteen site-years had sufficient data within all months of the year to analyze seasonality in energy balance closure. Within each of these 19 site-years, data was segregated into six 2-month increments, and OLS regressions were performed for each 2-month period. Fig. 7 shows the OLS slope of the six 2-month

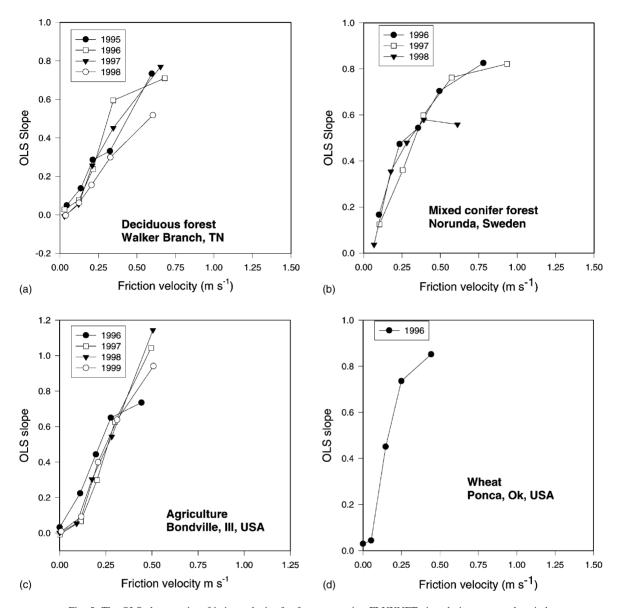


Fig. 5. The OLS slope against friction velocity for four contrasting FLUXNET sites during nocturnal periods.

increments for each site-year, with the line depicting the mean of all site-years. All sites are in the Northern Hemisphere and the mean slope increased from winter to summer months, averaging 0.66 in January and February to 0.80 in July and August. The mean intercept was also lower in winter $(-3.5 \,\mathrm{W\,m^{-2}})$ than in summer $(4.0 \,\mathrm{W\,m^{-2}})$. The coefficient of determination (r^2) ranged from 0.68 to 0.89 and was generally larger in summer than in winter. The EBR method indicated

smaller differences between seasons (not shown), with the mean ratio ranging from only 0.81 to 0.87, with the exception of first 2-month period (January and February) when the mean ratio was 0.72. Total available energy, and the denominator in the EBR calculations, was an order of magnitude greater in the peak summer period relative to the winter period.

Data were also analyzed to determine if the energy imbalance varied with Bowen ratio. For each of the 50

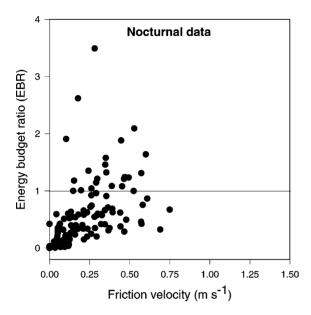


Fig. 6. EBR against friction velocity (u_*) during nocturnal periods (net radiation less than zero). Each site-year is represented by five points, representing half-hour data sorted by friction velocity into five 20 percentile groups.

site-years, the daytime data were segregated by Bowen ratio into four percentile groups, with the requirement that both H and LE exceed 10 W m⁻² to avoid periods of very small fluxes. For each of the sites, the Bowen ratio changed by nearly an order of magnitude between the first and last percentile groups. No overall trend in the OLS slope with Bowen ratio was observed for the sites. Isolating sites with closed path sensors, the mean slope was least in the lowest Bowen ratio category (0.67 versus 0.77 for other categories) (Fig. 8a); isolating sites with open path sensors, the mean slope was least for the highest Bowen ratio category (0.67 versus 0.74 for other categories) (Fig. 8b). The mean intercept decreased with Bowen ratio for sites employing the open path sensors and increased with Bowen ratio for sites using the closed path sensors. The EBR did not change with Bowen ratio for either closed or open path sensors.

3.7. Link between energy balance closure and CO₂ fluxes

To evaluate a possible link between the energy imbalance and the fluxes of CO₂, data for each site-year were sorted into three groups based on the normalized

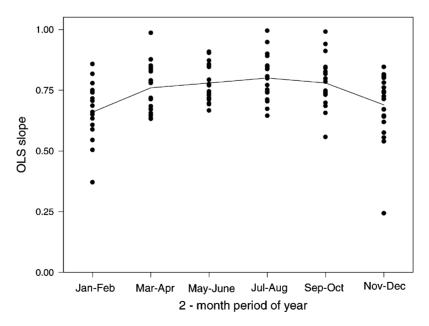
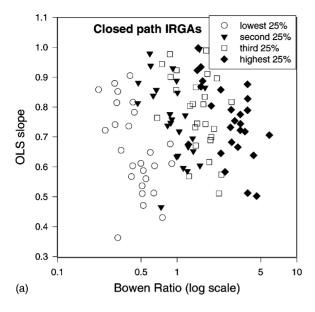


Fig. 7. The OLS slope, evaluated over 2-month increments, for the 19 site-years that had data over the entire annual cycle. The line shows the mean for the 2-month increments.



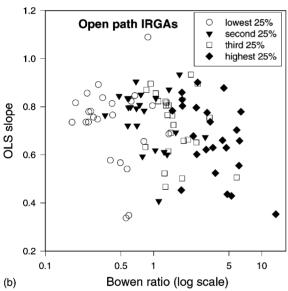


Fig. 8. The OLS slope versus Bowen ratio for site-years with (a) closed and (b) open path IRGAs. Daytime half-hour data was segregated into four 25 percentile groups for each site.

residual in the energy imbalance (δ_e)

$$\delta_{\rm e} = \frac{R_{\rm n} - G - S - {\rm LE} - H}{R_{\rm n} - G - S}$$

One group (labeled 'AC' for 'acceptable closure') contained only half-hourly data when energy balance

closure was 'acceptable' ($|\delta_e| \leq 0.10$). The second group (labeled 'LF' for 'low fluxes') contained data when $\delta_e > 0.10$ (turbulent heat fluxes underestimated relative to available energy) and the third group (labeled 'HF' for 'high fluxes') contained data when $\delta_e < 0.10$ (turbulent heat fluxes overestimated relative to available energy). Daytime data, defined by photosynthetically active radiation (PAR) > 0, was further segregated into five sub-groups based on PAR (50 < PAR < 300; 300 < PAR < 600; 600 < PAR < 1000; 1000 < PAR < 1500; PAR > 1500) (units of PAR in μmol m⁻² s⁻¹). To avoid spurious ratios, half-hour data was not included in this analysis if $R_n + G + S < 20 \,\mathrm{W \, m^{-2}}$. Only data between day 160 and day 240 (mostly summer season) were used to limit the analysis to periods when assimilation and CO₂ uptake are important and when PAR is expected to be a forcing variable for CO₂ fluxes. Therefore, this evaluation only applies to the warm season.

Fig. 9 shows the mean CO₂ flux (negative values indicate uptake by vegetation) for each of the five

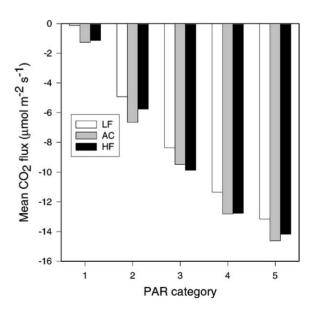


Fig. 9. The mean CO₂ flux between days 160 and 240 across all available site-years for the five PAR groups (see text). Data was segregated into one of the three groups based on energy balance closure (LF for low turbulent energy fluxes relative to available energy; AC for acceptable closure and HF for high turbulent energy fluxes relative to available energy). The means shown were estimated after estimating each of the site-year means (i.e. each site-year contributed equally).

Table 3
The results of the t-test to check for significant differences in the mean CO_2 flux with energy balance closure for each of the five PAR categories (see text)^a

PAR group	LF < AC	NS	LF > AC	HF < AC	NS	HF > AC
PAR 1	12	14	2	2	23	3
PAR 2	18	15	2	9	25	1
PAR 3	17	16	5	6	23	6
PAR 4	16	14	8	5	29	4
PAR 5	12	9	4	3	19	3

^a Columns 2–4 give the number of site-years that fall within one of the three categories in the test between groups LF and AC (LF < AC: magnitude of mean CO₂ flux in group LF was less (less negative) than AC; NS: not significant; LF > AC: magnitude of mean CO₂ flux in group LF greater (more negative) than in AC). The last three columns show number of site-years that fall within one of the three similar categories between groups HF and AC (symbols have similar meaning as for the *t*-test between LF and AC). A *t*-test was performed only if more than 30 half-hours of data were available in the PAR/energy balance closure category.

PAR categories across all sites, differentiating between data with 'acceptable' energy balance closure (AC) and data when turbulent heat fluxes were underestimated (LF) or overestimated (HF) relative to available energy. For all PAR categories, the magnitude of the mean CO₂ was lowest (less negative) during periods when the turbulent heat fluxes were underestimated relative to available energy (group LF). Taking the mean across all PAR categories the magnitude of the CO₂ flux was approximately 15% lower for group LF relative to AC. Alternatively, there was little change in the mean CO2 flux between data with AC and data when the imbalance occurred because of an 'overestimate' of turbulent heat fluxes relative to available energy (between groups HF and AC).

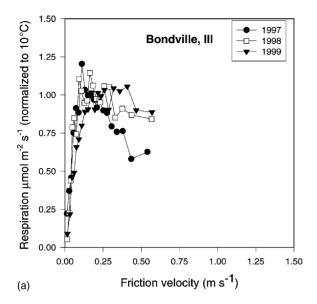
For each site-year, a t-test was performed within each of the five PAR categories to determine if there were statistical differences in the mean CO₂ flux across the energy imbalance groups (i.e. AC, LF, and HF). Table 3 summarizes the number of site-years for groups LF and HF when there was not a significant difference in the mean CO2 flux relative to AC data for the given PAR group, and when the magnitude of the CO_2 flux was either significantly (P < 0.05) lower or higher than data in the AC group. For each PAR group, between 42 and 48% of the site-years had a significantly lower net CO₂ uptake (less negative flux) when the turbulent energy flux was underestimated compared to when the imbalance was within 10% (group LF relative to AC in Table 3). There were far fewer differences in the mean CO₂ fluxes between group HF and AC (Table 3).

Nighttime data were also separated into three similar groups based on energy balance closure. The mean CO_2 flux across all sites when energy balance closure was acceptable (group AC) was almost twice $(4.72 \, \mu \text{mol m}^{-2} \, \text{s}^{-1})$ that compared to periods when turbulent heat fluxes were underestimated (group LF, $2.39 \, \mu \text{mol m}^{-2} \, \text{s}^{-1})$. There was no difference in the mean air temperature between these two groups of data (both were $16.2 \,^{\circ}\text{C}$). Of the $36 \, \text{site-years}$ with sufficient nocturnal energy balance and $CO_2 \, \text{flux}$ data available, the nocturnal $CO_2 \, \text{flux}$ was significantly greater (P < 0.05) in group AC relative to LF for 27 of the site-years. The quantity of nocturnal data in the group HF was minimal, and it was not included in the analysis.

To further demonstrate a possible link with the nocturnal carbon dioxide flux, Fig. 10 shows the relationship between ecosystem respiration at 10 °C, estimated from nocturnal data using the methods detailed by Falge et al. (2001), for two of the sites shown in Fig. 5. At the agricultural site (Fig. 10a), there appears to be a threshold friction velocity in carbon dioxide flux, although no threshold is apparent in the energy balance closure (Fig. 5c). At the forest site in Norunda, Sweden, a threshold friction velocity for carbon fluxes (Fig. 10b) and energy balance closure (Fig. 5b) is not obviously apparent.

4. Discussion

Although the intercepts of the OLS regressions for the site-years were typically non-zero, the OLS slope



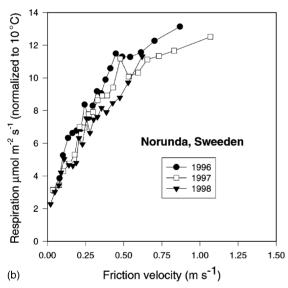


Fig. 10. The mean nocturnal respiration, normalized to $10\,^{\circ}$ C, against friction velocity sorted into 20 five percentile friction velocity groups using the method of Falge et al. (2001): (a) data from agricultural field in Bondville, IL; (b) data from a mixed forest in Norunda, Sweden.

(for positive and negative intercepts) was always less than 1. The EBR was less than 1 for over 80% of the site-years, further suggesting a general lack of closure. The general lack of complete energy balance closure at FLUXNET sites (linear regression slope and EBR typically less than 1) is consistent with historical evidence that the energy balance is often not closed using the eddy covariance technique (Mahrt, 1998; Gu et al., 1999; Twine et al., 2000). Explanations for the imbalance have been hypothesized in previous studies (Stannard et al., 1994; Mahrt, 1998; Aubinet et al., 2000; Twine et al., 2000; Culf et al., 2002) and can generally be summarized by the list in Table 4. This list is not totally comprehensive, but covers the primary reasons usually suspected for the energy imbalance: (1) systematic errors associated with the sampling mismatch between the flux footprint and the sensors measuring other components of the energy balance, (2) a systematic instrument bias, (3) neglected energy sinks, (4) low and high frequency loss of turbulent fluxes, and (5) horizontal and/or vertical advection of heat and water vapor. Table 4 also summarizes how these sources of error may affect energy balance closure and carbon dioxide fluxes. Each of these problems will be discussed and related to the FLUXNET data set. Errors in the eddy covariance approach are also summarized in Businger (1986) and Folken and Wichura (1996).

4.1. Sampling errors

Random errors associated with averaging a subset of turbulent eddies at one location to estimate ensemble mean turbulent fluxes (Moncrieff et al., 1996; Mahrt, 1998) will reduce r^2 , but should not affect the OLS slope, the long-term EBR or long-term flux estimates. Accounting for random errors in the dependent variable $(R_n - G - S)$ using two statistical approaches (Meek and Prueger, 1998) reduced the slope of the OLS regression, but the errors would need to approach 40% to obtain a mean slope of 1 across sites, and with these hypothetical errors the intercepts became highly negative. Furthermore, random errors larger than 40% are possible for G and S in some conditions, but they are less likely for R_n , which has a larger source area and is frequently the dominant available energy term. Furthermore, the overall long-term bias in closure at most sites, indicated by the annual values of EBR, suggests a low probability that the imbalance is primarily a statistical artifact.

A second type of sampling error is associated with the inability to match the source areas of the eddy covariance measurements (the flux footprint) with the source area of the instrumentation measuring R_n , G

Table 4
General list of possible reasons for energy imbalance at FLUXNET sites^a

Cause of imbalance	Examples	LE + H	$R_{\rm n}-G-S$	Ratio	Affects CO ₂
Sampling	Source areas differ				No
Instrument bias	Net radiometer biased				If sonic or IRGA
Neglected energy sinks	Storage above soil heat plates		+	_	No
High/low frequency loss	Sensor separation/large eddies	_		_	Yes
Advection	Regional circulation				Yes

^a Also shown is whether this effect is expected to underestimate (negative sign) or overestimate (positive sign) the turbulent fluxes (LE+H), available energy ($R_n - G - S$) and the energy balance closure ratio (LE+H)/($R_n - G - S$). The last column indicates whether this effect is relevant to interpretations of the CO₂ flux.

and S. Schmid (1997) provides a detailed discussion of the issues involved in matching scales of observations, particularly the different geometry and dynamics of the source areas for net radiometers and flux footprints. The source area for a net radiometer has a radius related to sensor height that is fairly constant with time and is centered below the instrument. The instrument typically protrudes horizontally off a tower, and in some cases the tower structure or removal of vegetation near the tower may influence the sensor. Alternatively, the spatial dimension of the flux footprint is not fixed in space and is dependent on atmospheric conditions, typically approximating an ellipse that is distorted in the mean upwind direction. In theory and practice, the source areas for a net radiometer and eddy covariance flux footprint never match.

The assumption of equivalent source areas is even more problematic when relating *G* to *H* and LE. The ground area influencing the soil heat flux plates or thermocouples (if using the calimetric method) (Buchan, 1989) is one to several orders of magnitude smaller than the associated source areas of the net radiometers and the eddy covariance flux footprint. A similar daunting problem exists for the estimate of *S* in tall vegetation, especially the component associated with sampling biomass temperature, which is a complex function of aspect, depth into woody tissue and canopy height.

The most obvious effect on energy balance closure occurs when the measurement source area of one of the energy balance components is representative of a systematically different surface or climate than the source area sensed by the other energy balance components. This systematic error would generally be greatest in open canopies or in canopies with large gradients in biophysical characteristics, where hetero-

geneity is present at multiple scales (Culf et al., 1993; Stannard et al., 1994; Baldocchi et al., 2000; Kustas et al., 2000). FLUXNET sites are not generally designed to evaluate spatial variability in the available energy components at the spatial scale of the turbulent flux footprint. However, R_n is typically the largest component of available energy and several studies have found little spatial variability of R_n above uniform (Twine et al., 2000) and complex patchy landscapes (Schmid et al., 1991; Stannard et al., 1994; Anthoni et al., 2000) (but also see Culf et al., 1993). Although measurement source errors are present at FLUXNET sites, this type of error is not expected to consistently present a positive systematic bias in available energy relative to turbulent scalar fluxes. Other studies investigating multiple sites have deduced a similar hypothesis (Stannard et al., 1994; Mahrt, 1998; Twine et al., 2000; Anthoni et al., 2000).

4.2. Instrument biases

A second group of errors that can affect energy balance closure involves instrument biases, inaccurate calibrations and data processing errors. These comments will focus on a few general aspects of instrumentation, because it is assumed that all sites are processing data and computing fluxes correctly. Cross calibration of instrumentation and processing methods have probably reduced some of these uncertainties between selected sites (Aubinet et al., 2000; Baldocchi et al., 2001).

Soil heat flux plates can be inaccurate because the thermal conductivity of the heat flux plate and surrounding soil may be unequal (VanLoon et al., 1998). Heat flux plates typically have a conductivity similar to soil, but thermal properties vary temporally because of changes in soil water content and temperature (Verhoef et al., 1996). Soil heat flux plates also can alter the environment they are measuring, especially by limiting water movement in soils (Mayocchi and Bristow, 1995). AmeriFlux sites generally use REBS (Radiation Energy Balance Systems) heat flux plates, and EUROFLUX sites use heat flux plates and calimetric methods (Aubinet et al., 2000).

Several studies have addressed calibration methods and the accuracy of various brands of net radiometers (Field et al., 1992; Halldin and Lindroth, 1992; Hodges and Smith, 1997; Stannard et al., 1994; Kustas et al., 1998; Culf et al., 2002; Halldin, 2002). Some of the differences in closure between FLUXNET sites are probably the result of bias errors in net radiometers. A majority of the AmeriFlux sites have used REBS net radiometers; EUROFLUX sites have used a variety of net radiometers, with many sites using instruments manufactured by REBS and Schulze/Daeke. Bias errors up to 15% have been noted between older versions of net radiometers, which includes some of the manufactures used in FLUXNET (Field et al., 1992; Stannard et al., 1994), although the commercial instrumentation and calibration methods have been subsequently updated. Some versions of the REBS net radiometers, which are common at AmeriFlux sites, are known to have been calibrated incorrectly (Kustas et al., 1998; Twine et al., 2000), creating a low bias (15% during the daytime) in net radiation and possibly erroneously improving energy balance closure. In fact, recent improvement in design and calibration of net radiometers appears to have increased the energy imbalance (Wilson and Baldocchi, 2000; Culf et al., 2002) Calibration procedures, either performed by the manufacturer or site operators, differ among FLUXNET sites, making it difficult to quantify bias errors. Recent inter-comparisons of independently calibrated sensors at several sites showed only small differences in sensor type (unpublished data using Didcot DRN-305 and REBS Q7 at Brasschaat, Germany, and REBS Q7 and Kipp and Zonen NR LITE at Walker Branch, TN).

Although there can be differences between types of net radiometers, nearly all the net radiometers used in FLUXNET would have to be biased high during the day and low at night to account for the energy imbalance. Twine et al. (2000) concluded that in the ARM (Atmospheric Radiation Measurement) project, which has a primary goal of accurately measuring

radiation components, an energy imbalance persisted despite careful net radiation calibrations. Estimates of net radiation using independently derived satellite estimates also indicated a lack of closure across BOREAS sites (Gu et al., 1999).

Instrument errors can also occur with the eddy covariance instrumentation used to compute velocities (sonic anemometer), temperature (sonic anemometer) and water vapor (usually IRGA, either open or closed). Mounting equipment and instrumentation may shadow sonic anemometers (Wyngaard, 1981) and degrade data quality and energy balance closure in certain wind directions, but this effect does not explain the consistent lack of closure across most wind directions at the sites. A second source of error occurs when turbulent fluctuations are of insufficient magnitude to be resolved by the instrumentation (Mahrt, 1998). Errors concerning possible insufficient sampling frequency and loss of high frequency flux and other errors associated with time and space assumptions used in the eddy covariance technique are addressed subsequently.

4.3. Other energy sinks

An assumption in the analysis of energy balance closure is that the energy in the system can be approximated from the five measured components (LE, H, $R_{\rm n}$, G, and S), and that all energy stored beneath the sensor (G and S) is estimated properly. Even when soil heat flux plates are used, as at a number of FLUXNET sites, a heat storage term is needed to account for the soil above the sensors (Mayocchi and Bristow, 1995). In open canopies, this storage can be large even when heat plates are buried near the surface (Stannard et al., 1994; Mayocchi and Bristow, 1995), and it is assumed that this storage is correctly accounted for at the FLUXNET sites. The FLUXNET data suggests that inaccuracies in G have a greater impact on energy balance closure in agricultural, chaparral and grassland sites than in forests.

A correction to the soil heat flux calculation that is commonly neglected and difficult to estimate is the 'isothermal' LE component (Buchan, 1989; Mayocchi and Bristow, 1995). If soil heat flux plates are near the surface and above the region where subsurface evaporation typically occurs, the isothermal LE flux is proportional to the subsurface evaporation beneath the heat flux plates. Published estimates of soil evap-

oration indicate that the magnitude of this term for FLUXNET sites is probably less than 5% of R_n in closed forest canopies with dense litter layers (Wilson et al., 2000), but may be several times greater in more open canopies (Baldocchi et al., 2000) or above bare soil or bare soil covered by crops (Villalobos and Fereres, 1990). For the majority of FLUXNET sites, which use soil heat flux plates, consideration of this term will typically decrease the estimated G (Mayocchi and Bristow, 1995) and increase the estimated total available energy, which may further degrade energy balance closure.

Heat storage between the soil surface and level of flux measurements (S) can also be difficult to estimate, because a full accounting requires air temperature and humidity measurements at multiple heights, as well as estimates of biomass temperature. The number of temperature probes used at FLUXNET sites varies from just a few to dozens (Aubinet et al., 2000). Gradients of stem temperature, both with height and aspect in the canopy and with depth in woody tissue, can be a source of important sampling errors (Aston, 1985; Moore and Fisch, 1986). Estimating total canopy biomass is particularly challenging, and an estimate of the canopy specific heat constant is also required. Consideration of canopy heat storage generally decreased the magnitude of the imbalance at FLUXNET sites. Because of rapid temperature changes, the change in canopy heat storage (S) was a greater fraction of net radiation early in the day, which is also when the mean imbalance was greater. Better energy balance closure during the afternoon, when temperature changes and S are usually smaller, may be a clue that storage components are frequently underestimated at FLUXNET sites.

Careful examination of storage terms at the FLUXNET site in Bordeaux, France, dramatically improved energy balance closure (Lamaud et al., 2001) and this site has an OLS slope approaching 1 (3-year mean of 0.94). Nevertheless, the general lack of closure, even in very short and sparse vegetation, seems to suggest that canopy heat storage is not likely the only important source of imbalance across all sites. Furthermore, because storage components should nearly vanish when integrated over an annual basis, storage errors would not explain the low EBR over longer periods (i.e. site-years).

Even if each of the five components is accurately measured, additional energy sinks (Q) are present in

the canopy, although these are typically neglected because they are considered small. Photosynthesis is a form of biochemical energy storage that is typically in the order of 1–2% of the available energy (Oke, 1987), but may be several times greater in agricultural plants with high quantum yields, such as at the maize site in Bondville, IL.

Based on thermodynamic considerations, additional terms in the energy balance equation have been suggested by Sun et al. (1995) and Paw U et al. (2000). Along with other small correction terms investigated by Sun et al. (1995), the correction associated with the specific heat of moist air is expected to be less than 1%. A second sink of energy that has been neglected in energy balance calculations is the expansion of air during evaporation under constant pressure (Paw U et al., 2000), which is implied if one accepts the corrections of Webb et al. (1980). The suggested method to correct for this effect is to use the sonic temperature in calculating sensible heat flux instead of the estimated 'dry' air temperature (a value that is derived from the sonic temperature or measured independently using temperature sensors) in energy balance computations, which is a correction of about 7-8% of LE. Over deciduous forests, agricultural sites and many coniferous forests in FLUXNET, LE is close to or in excess of one-half R_n during the growing season, suggesting that this correction could approach 5% of $R_n - G - S$ during the daytime and may improve energy balance closure by a similar magnitude.

4.4. Low and high pass filtering

Independent of other considerations, the eddy covariance technique underestimates the total mean turbulent flux to some extent because of high frequency loss (low pass filters). Unintentional low pass filters result from practical issues such as instrumentation that necessarily measures with finite response times, and at finite sampling increments and within finite volumes (Moore and Fisch, 1986). Spatial separation of sonic anemometers and scalar concentration instrumentation (i.e. IRGA) acts as a low pass filter. Additional high frequency losses, associated with tube attenuation and time lags, are present in systems using closed path IRGAs (Leuning and Judd, 1996). The averaging period used to define mean fluxes can

cut-off low frequency contributions (high pass filter) (Moore, 1986; Aubinet et al., 2000).

Theoretical (Moore, 1986) analytical (Massman, 2000) and empirical (Goulden et al., 1997) approaches have been proposed to account for low and high frequency loss of flux. However, no standard method for estimating frequency response corrections is used across all FLUXNET sites, and the different correction methods do not always agree (Aubinet et al., 2000). Individual sites typically correct their data for high frequency losses based on personal preferences before submitting to the FLUXNET archive. For closed path IRGAs, corrections are often based on the assumption that *H* defines the expected frequency distribution of mass and energy-transporting eddies (Ribmann and Tetzlaff, 1995).

One hypothesis is that some portion of the energy imbalance may result from underestimates in water vapor (LE) flux, as suggested by Dugas et al. (1991). Sensible heat flux is estimated using sonic anemometry, but the water vapor sensor is separated from the sonic anemometer (i.e. sensor separation acts as a low pass filter). Additional LE loss may occur using closed path systems because of tube attenuation or water vapor interactions with tubes and chamber walls (Goulden et al., 1997; Leuning and Judd, 1996). At the FLUXNET sites, there were no obvious differences in the energy imbalance between open and closed path IRGAs, which may indicate that these problems are small or that the frequency response corrections were applied appropriately. However, it is possible that the slightly lower OLS slope at low Bowen ratios using closed path sensors indicates an underestimate of water vapor fluxes.

High frequency corrections are expected to be less at tall-forested sites because turbulent time scales increase (Anderson et al., 1984; Baldocchi and Meyers, 1988). Energy balance closure was not generally superior at sites with tall vegetation, which may imply that the loss of high frequency flux was not the major source of the energy imbalance. FLUXNET sites that have closed path sensors often show correction terms as large as 15–30% (Goulden et al., 1997; Berger et al., 2001), but there was no obvious difference in the imbalance between sites with both types of sensors. It was not possible to evaluate the effect of averaging time on the energy imbalance across all sites, but Goulden et al. (1997) found that averaging time

did not change energy balance closure at a FLUXNET site in a spruce forest.

4.5. Advection

At nearly all FLUXNET sites, it is assumed that advection of scalars (including CO₂), can be neglected (Paw U et al., 2000). Vertical advection is neglected by rotating the coordinate system so that the mean vertical velocity is always zero (McMillen, 1988). However, non-zero values of mean vertical velocity and vertical advection are realistic and can be induced by horizontal heterogeneity or mesoscale and synoptic scale forcing (Lee, 1998; Sun et al., 1998). Two types of flows may make the assumption of negligible mean vertical advection problematic at FLUXNET sites. First, horizontal heterogeneity in surface fluxes, even at scales much larger than typically required in micrometeorological studies, can promote local circulations and vertical motions that seriously compromise the zero vertical velocity assumption (Vidale et al., 1997; Sun et al., 1998; Leclerc et al., 2000). Similarly, even slight elevation gradients over a range of spatial scales can induce nocturnal drainage flows and advection near the surface during periods of strong static stability (Mahrt and Larsen, 1990; Lee, 1998).

The poor energy balance closure during nocturnal periods at FLUXNET sites, especially when turbulence was weak (low friction velocity), is consistent with the establishment of drainage flows that advect heat and water vapor (and CO₂) to low terrain. Aubinet et al. (2000) and Blanken et al. (1998) have also shown that the energy imbalance during nocturnal periods is usually greatest when friction velocity is small. Lee and Hu (2002) hypothesized that the lack of energy balance closure during nocturnal periods was often the result of mean vertical advection.

If terrain-induced flow is the primary source of the energy imbalance, it would be expected that sites on 'flat' terrain should have better energy balance closure, especially during nocturnal periods. Although previous research suggests that terrain can affect the extent of closure (Kustas et al., 1991; Stannard et al., 1994) these studies also find a lack of closure at sites across a range topographic variations. In this study, closure was not obviously superior at sites reported to be on 'flat' terrain across the FLUXNET sites. However, the evaluation of terrain is highly subjective

and can depend on spatial scales. Even at sites with locally flat terrain, larger scale elevation gradients may promote terrain-induced circulations.

Although nocturnal flows likely augment the relative energy imbalance compared to the daytime, the daytime imbalance suggests that daytime advection or other processes are also potentially important. It is also reasonable to suspect that the lack of closure may result from small but multiple issues that reduce the magnitude of the estimated fluxes.

4.6. Implications for CO₂ flux

A primary motivation for the FLUXNET network is to quantify carbon cycling over specific ecosystems around the globe. A general lack of energy balance closure in the network may be a concern that CO₂ flux estimates may be in error; however, it is not a conclusive test. Errors in the energy balance calculations can be independent of CO₂ flux estimates and vice versa, implying that the consequences of the imbalance on interpreting CO₂ fluxes are largely dependent on the reasons for the imbalance at FLUXNET stations (Table 4).

Sampling errors associated with differences in source area among the energy balance terms would not have direct implications on the quality of CO₂ flux measurements. An inaccurate account of G, S and Q, which is probable at some sites in FLUXNET, was also not expected to have direct implications on CO₂ measurements, but different CO₂ sinks may be present, such as diffusion into groundwater (Jones and Mullholland, 1998). Instrument biases in energy measurements (net radiation, soil heat flux) would not have implications on the quality of CO₂ measurements, but biases associated with sonic anemometers or IRGAs could also bias CO2 fluxes. If low or high pass filters are the primary source of the energy imbalance, then errors in the CO₂ flux should be expected, especially because the CO₂ measuring device (IRGA) and sonic anemometer are separated spatially. Similarly, if mean horizontal or vertical advection are affecting energy balance closure, advection of CO₂ should also be suspected. However, because there are spatial and temporal differences in source strengths between heat, water and CO2, the magnitude of advection fluxes can be different for the different scalars. For example, although the transport mechanisms for heat, water and CO₂ are similar, the CO₂ flux is more susceptible to nocturnal drainage. The integrated CO₂ flux is the difference in two large terms, carbon uptake associated with photosynthesis, and respiration. Systematic errors in nocturnal respiration can have large implications on long-term estimates of carbon sequestration (Moncrieff et al., 1996). Alternatively, the nocturnal water vapor flux is typically of relatively minor quantitative importance to the long-term water balance. This may be one reason why the catchment water budget (Barr et al., 1994; Wilson et al., 2001) is easier to close than the carbon budget, although the estimated carbon budget may also be nearly closed on an annual basis at some sites (Curtis et al., 2002).

Because the magnitude of the mean CO2 flux at a given PAR was approximately 15% lower when the turbulent energy fluxes are low relative to available energy, there is some reason to suspect that the daytime energy imbalance is also affecting CO₂ fluxes at FLUXNET sites. Mean warm season differences in the nocturnal CO₂ fluxes of nearly 2.5 μ mol m⁻² s⁻¹ (50%) between periods with acceptable and poor energy balance closure also suggests a link between the imbalance and CO₂ flux estimates. Using chamber estimates as a reference, Twine et al. (2000) also found evidence that eddy covariance estimates of the CO₂ flux were underestimated during periods of energy imbalances. It is still possible that the energy imbalance and the lower CO₂ fluxes occur during calmer periods when both energy and carbon storage terms are large and underestimated, but these responses may also suggest advection, drainage flows or some other problem associated with the eddy covariance technique.

Previous studies have indicated that nocturnal respiration estimates are in better agreement with chamber measurements during periods of greater turbulent intensity (friction velocity) (Goulden et al., 1997; Law et al., 1999). This study and Blanken et al. (1998) suggests similar improvement in energy balance closure with friction velocity. These corresponding relationships with friction velocity may support the notion that data quality is improved during periods of higher turbulent mixing (Goulden et al., 1997). However, there is little evidence that nocturnal energy balance closure is acceptable above a 'threshold' friction velocity, even within particular sites, which may have implications on using this technique for accepting or rejecting nocturnal CO₂ fluxes (Goulden et al., 1997; Jarvis et al.,

1997; Hollinger et al., 1999; Aubinet et al., 2000). The large intercepts and poor correlation of the OLS energy balance regressions during nocturnal periods at all values of friction velocity are also a concern.

5. Conclusions

- There was a general lack of energy balance closure at FLUXNET sites, with the scalar fluxes of sensible and LE being underestimated and/or available energy being overestimated. The mean imbalance was in the order of 20%.
- Energy balance closure is typically poor during nocturnal periods, especially when the turbulent mixing is weak. On average, energy balance closure was better in the afternoon than in the morning, possibly suggesting the underestimation of storage terms, which are usually larger in the morning.
- 3. No conclusive differences were observed between sites using open and closed path IRGAs or on sites with 'flat' or sloping terrain.
- 4. The energy imbalance persisted during all seasons of the year and at all Bowen ratios, but the regression slope was typically closer to 1 during the warm season
- 5. The mean relationship between CO₂ and PAR, as well as nocturnal respiration, were affected by the extent of energy balance closure. This evidence suggests a link between CO₂ fluxes and energy balance closure, it is still uncertain if the mechanisms creating the imbalance and the lower CO₂ flux estimates are similar.

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