An analytic disc is a holomorphic map from the unit disc in \mathbb{C} into some target space, for example \mathbb{C}^n , which extends continuously up to the boundary. I will solve approximately a nonlinear Riemann-Hilbert boundary value problem and then I will present its applications in constructing analytic discs with certain properties.